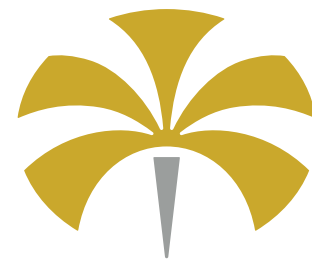


Third Workshop on Density Functional Theory:
Fundamentals, Developments, and Applications (DFT2025)

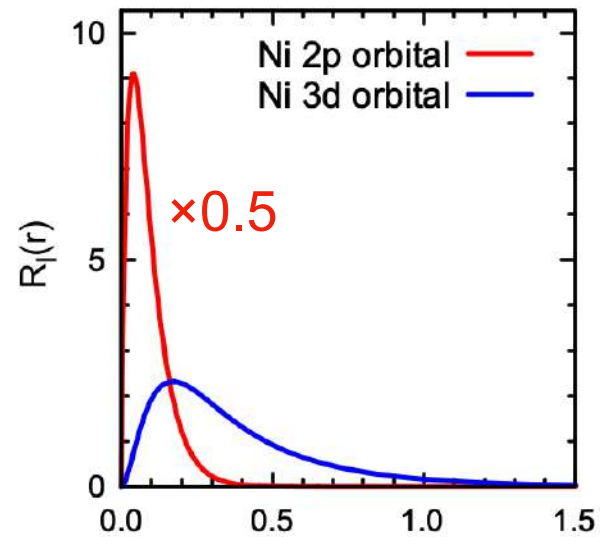
DFT-Based Quantum Embedding Approach for X-ray Spectroscopy Calculations

Atsushi Hariki



Osaka
Metropolitan
University

Atomic radial function
(from atomic Hartree-Fock calc.)



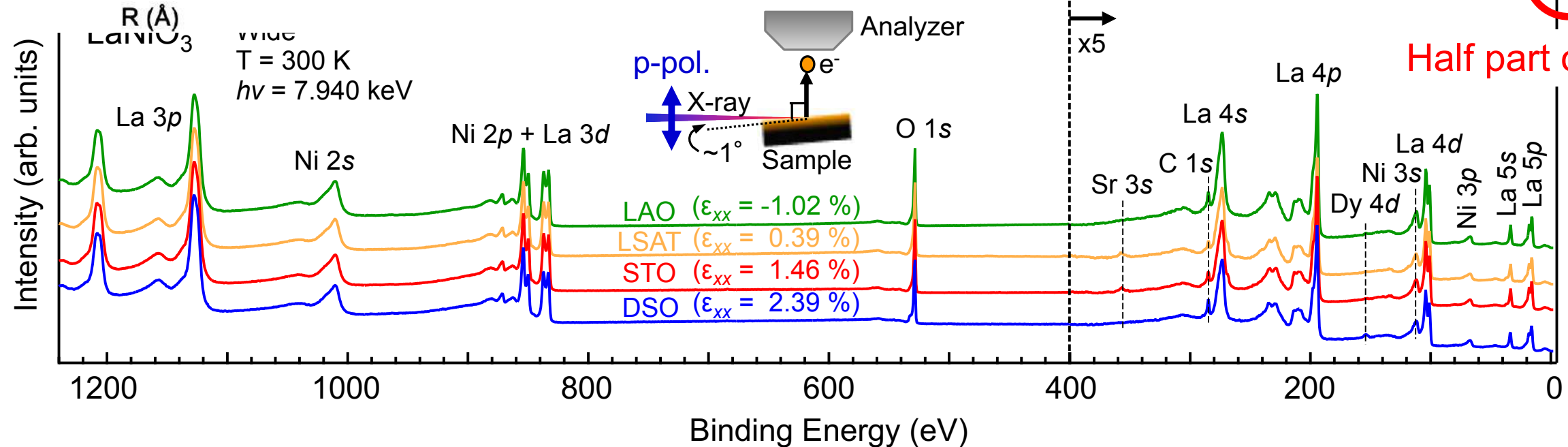
3d, 4d, 5d transition metal, 4f, 5f lanthanide actinide

X-ray spectroscopy and correlated electron physics

Energy spectroscopy
Low energy excitations (1-10 eV)

Elementary excitations, magnetism,
metal-insulator transition (near $E_F < 1$ eV)

I also discuss the core-level “spectral function”



XPS spectrum in LaNiO_3

K. Yamagami et al., Appl. Phys. Lett. 118, 161601 (2021)

1. Why core-level excitation to study material properties (low-energy excitations)?
2. Why DFT (+many-body theory) is needed for simulating core-level excitations?

Note. Our Interest is NOT element dependence of the core binding energies

Calc. LDA+DMFT Anderson model

A. Hariki et al., PRB **96**, 045111 (2017)

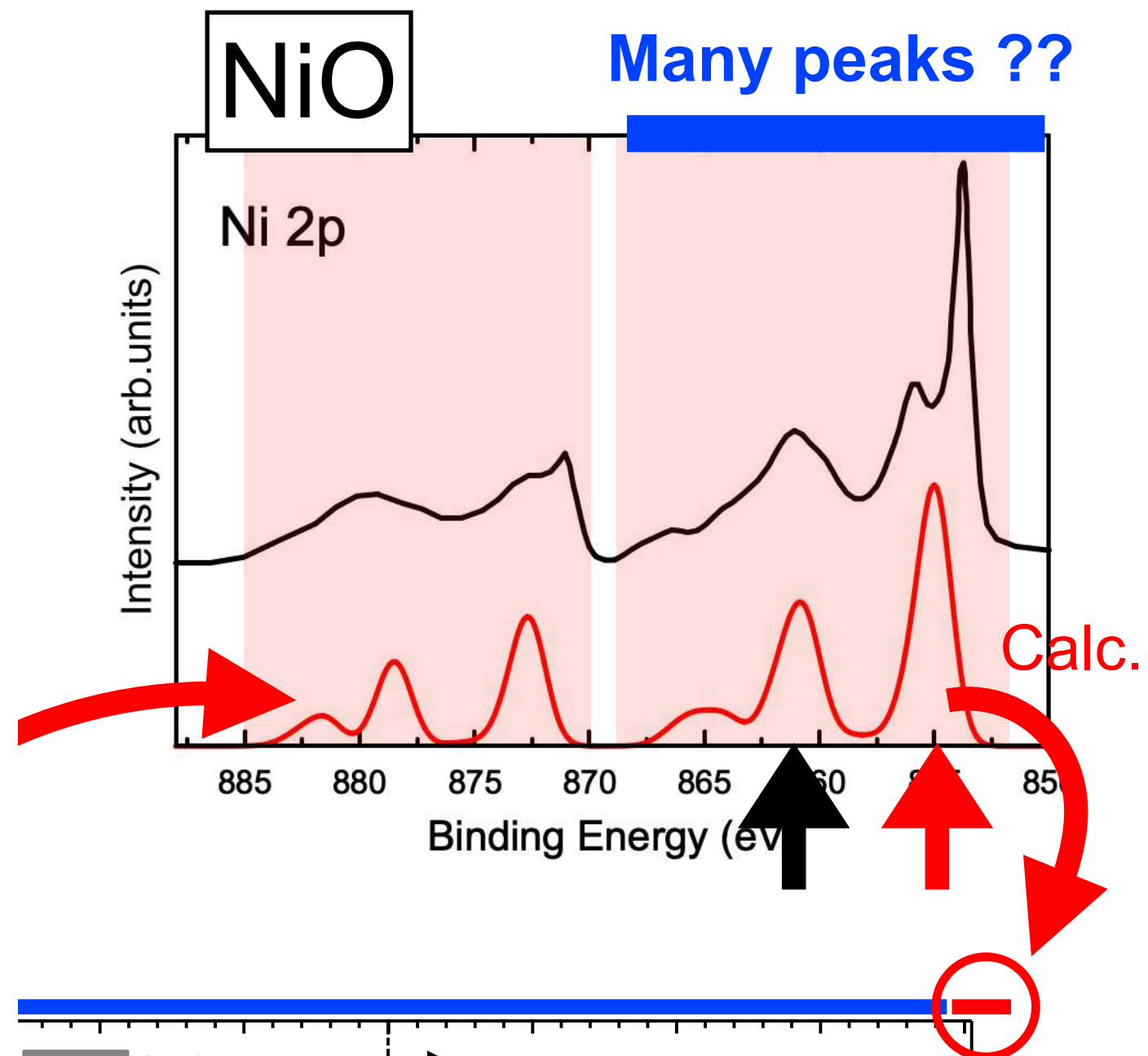
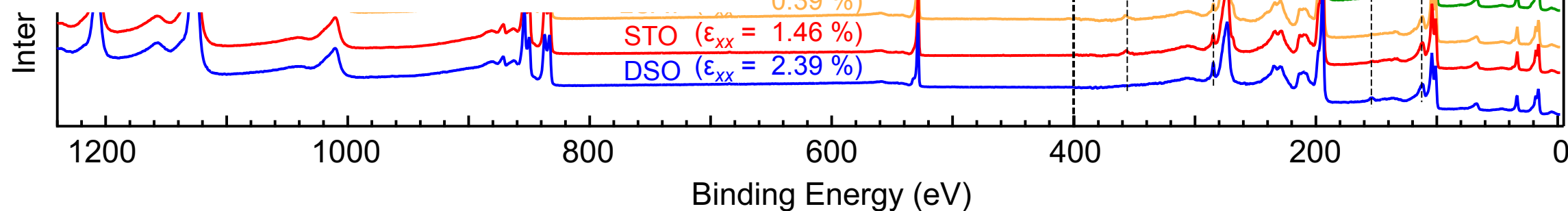
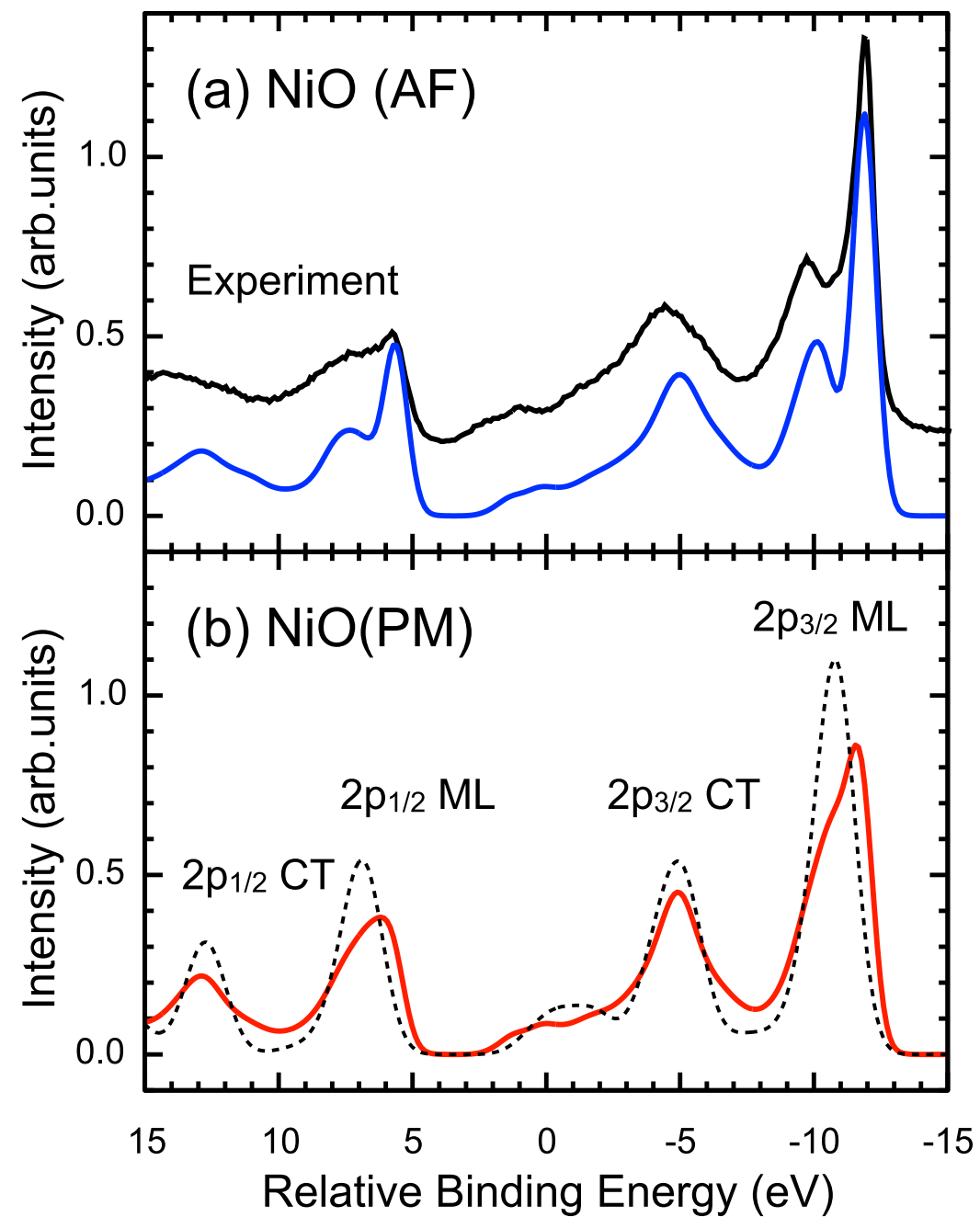


Table of contents

1. Core-level X-ray spectroscopy and DFT-based embedding approach

★ **Method.** DFT+ dynamical mean-field theory (DMFT)

A. Hariki, T. Uozumi, and J. Kuneš, Phys. Rev. B **96**, 045111 (2017)

A. Hariki, M. Winder, and J. Kuneš, Phys. Rev. Lett. **121**, 126403 (2018)

A. Hariki, M. Winder, T. Uozumi, and J. Kuneš, Phys. Rev. B **101**, 115130 (2020)

2. Application to various optical processes and compounds

★ **Excitations.** XPS, XAS, RIXS ★ **Materials.** *d*, *f* electron systems

★ **Physics.** Magnetism, valence structure, elementary excitations

K. Higashi, M. Winder, J. Kuneš, and A. Hariki, Phys. Rev. X **11**, 041009 (2021)

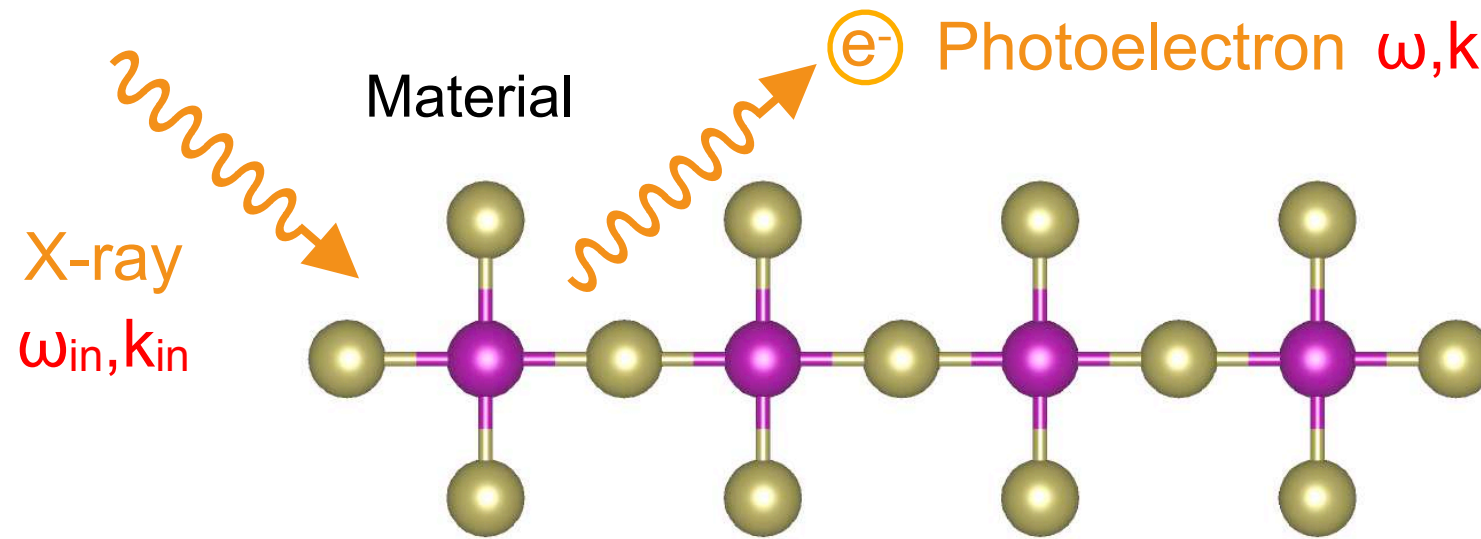
D. Takegami, A. Hariki et al., Phys. Rev. X **12**, 011017 (2022)

M. C. Rahn, K. Kummer, A. Hariki, et al., Nat. Commun. **13**, 6129 (2022)

J. Li, A. Hariki et al., Phys. Rev. X **13**, 011012 (2023)

A. Hariki et al., Phys. Rev. Lett. **132**, 176701 (2024)

X-ray photoemission spectroscopies and DFT theory



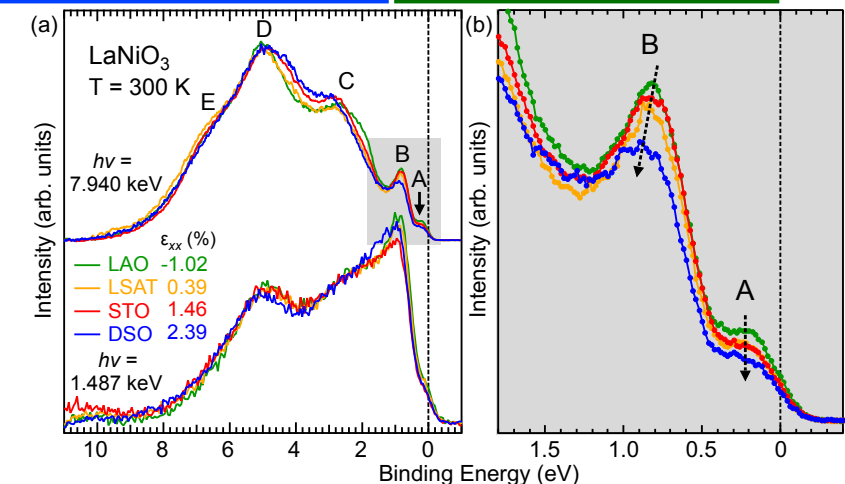
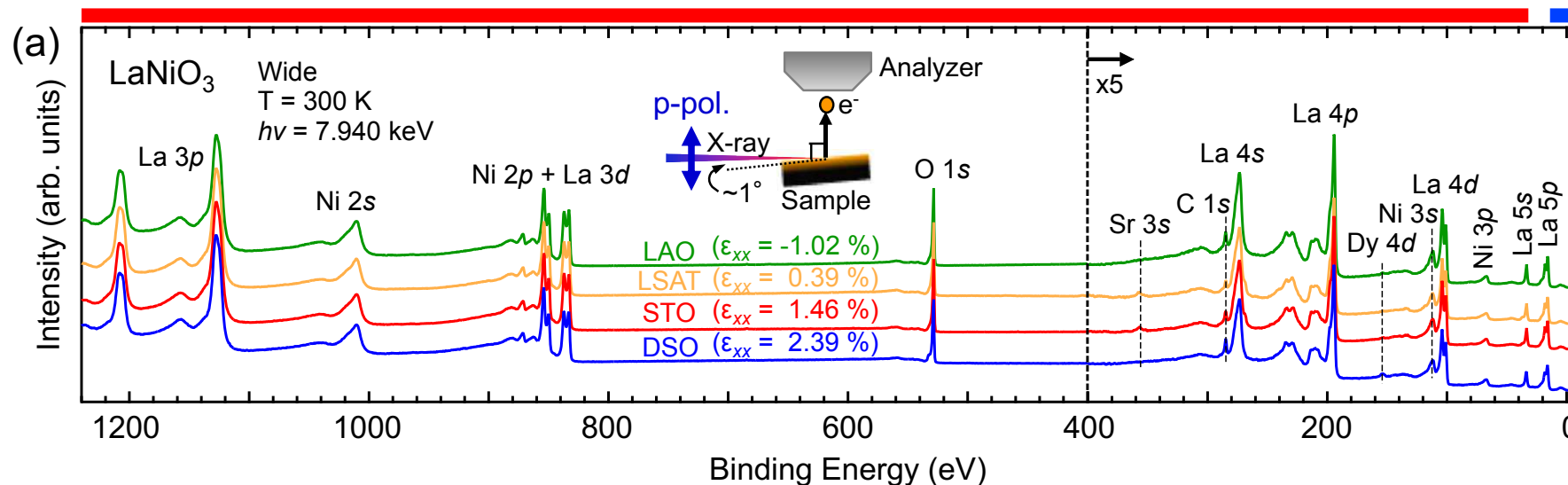
X-ray photoemission spectroscopy:

- Valence-band XPS (ARPES)
directly measure the low-energy states
- Core-level XPS
Site/element specific excitation

XPS spectrum in LaNiO_3 K. Yamagami et al., Appl. Phys. Lett. 118, 161601 (2021)

Core levels

Valence bands Near Fermi (QP)



1-particle
Green's function

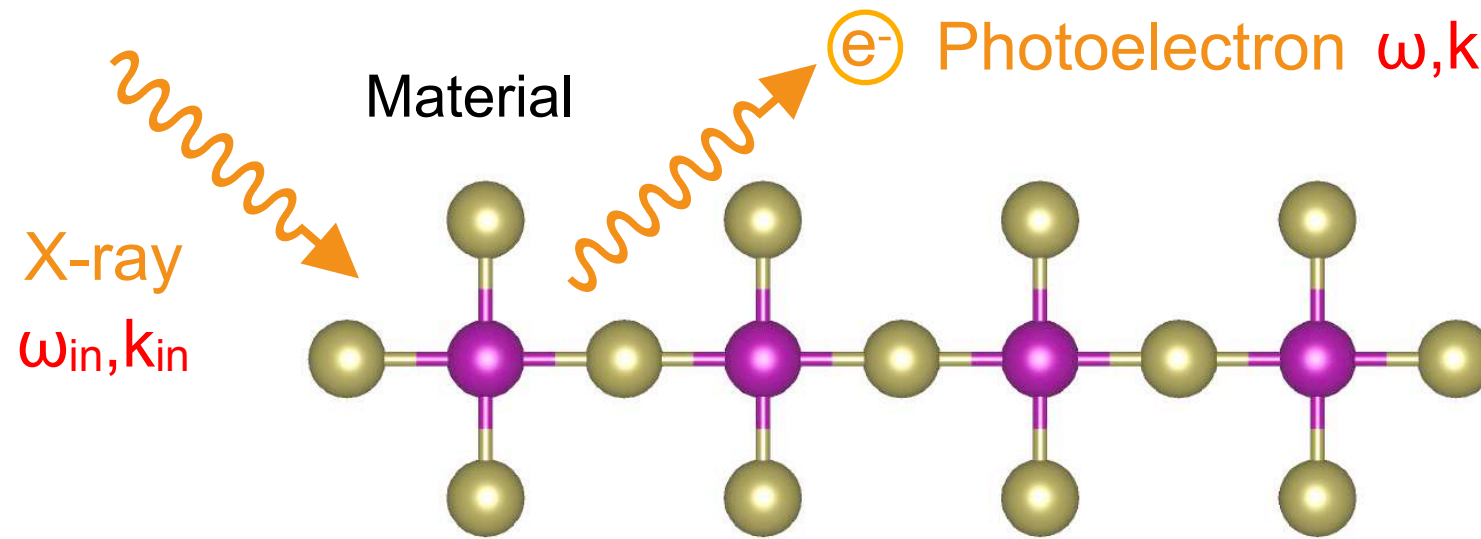
$$G_r(\epsilon) = \langle \Phi_0^{(N)} | c_r^\dagger \frac{1}{\epsilon - (E_0^{(N)} - \mathcal{H}) + i\delta} c_r | \Phi_0^{(N)} \rangle + \langle \Phi_0^{(N)} | c_r \frac{1}{\epsilon - (\mathcal{H} - E_0^{(N)}) + i\delta} c_r^\dagger | \Phi_0^{(N)} \rangle$$

photoemission

$$= \sum_n \left[\frac{|\langle \Phi_n^{(N-1)} | c_r | \Phi_0^{(N)} \rangle|^2}{\epsilon - (E_0^{(N)} - E_n^{(N-1)}) + i\delta} + \frac{|\langle \Phi_n^{(N+1)} | c_r^\dagger | \Phi_0^{(N)} \rangle|^2}{\epsilon - (E_n^{(N+1)} - E_0^{(N)}) + i\delta} \right]$$

Inverse photoemission

X-ray photoemission spectroscopies and DFT theory



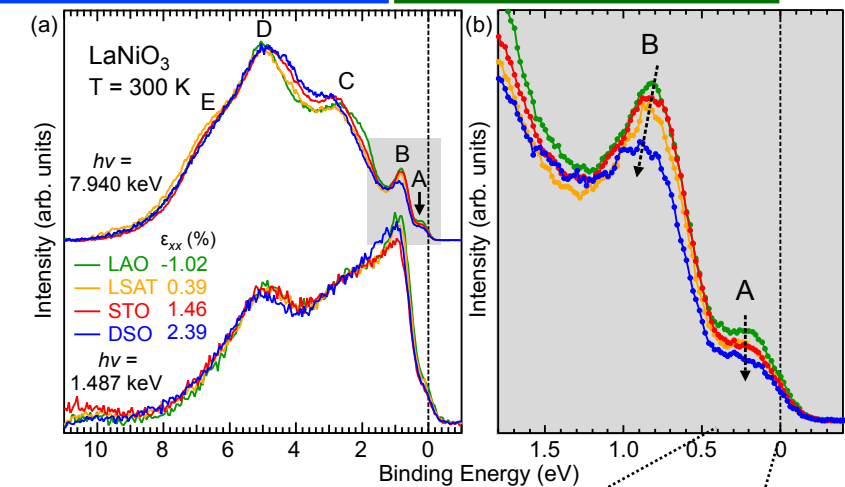
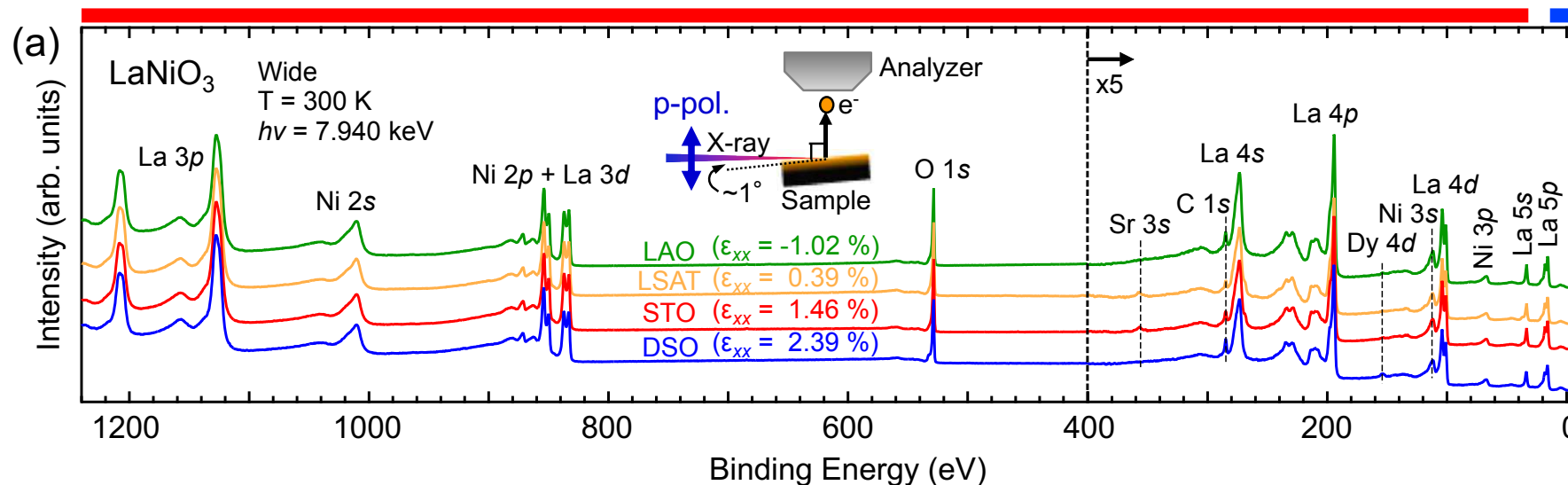
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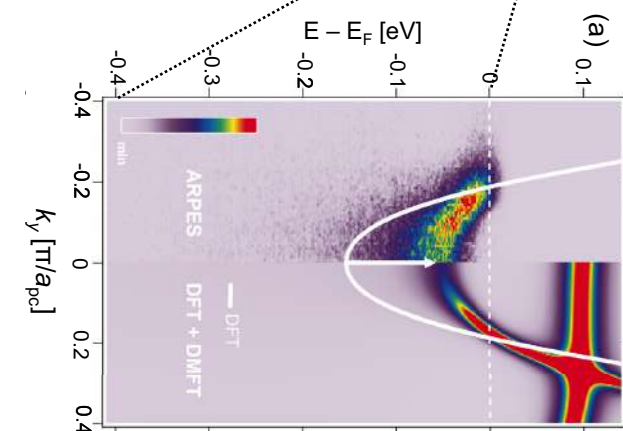
Core levels (no momentum dependence)

Core electrons (holes) completely localized at each ion

- Element specific information (valency)
- Local electronic structure
(Hund's multiplet, crystal field, and more ...)

ARPES: resolve the momentum

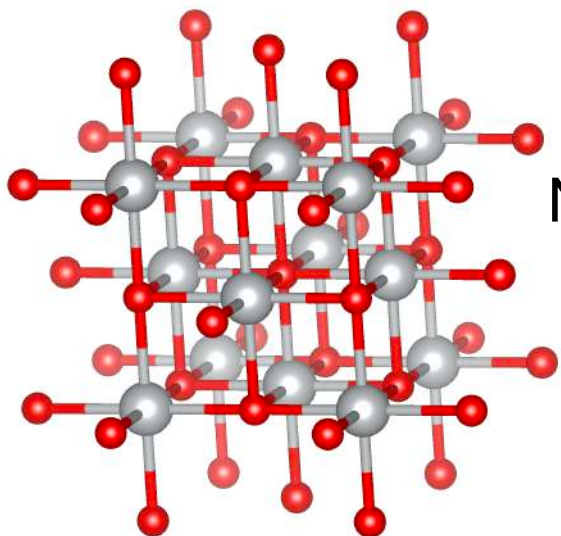
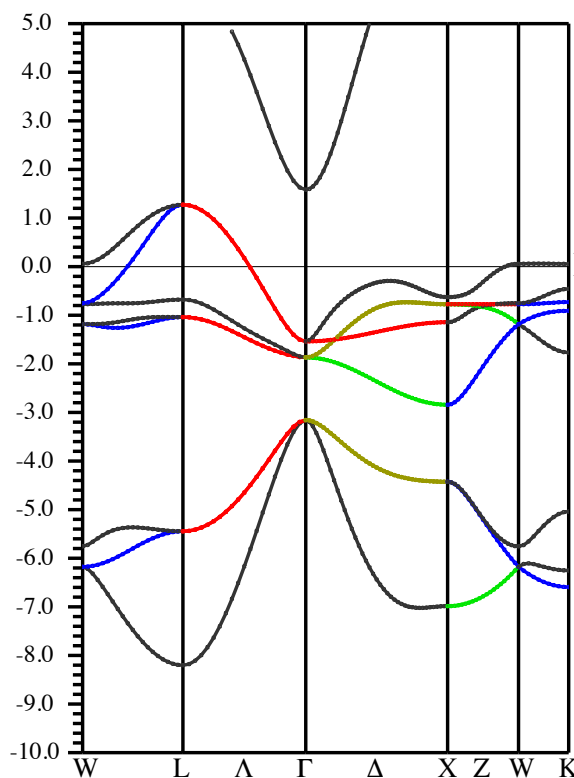
E. A. Nowadnick et al.,
Phys. Rev. B **92**, 245109 (2015)



X-ray photoemission spectroscopies and DFT theory

DFT calculation; indispensable for understanding the material dependence of the valence electronic structure (valence spectra, i.e. valence band PES)

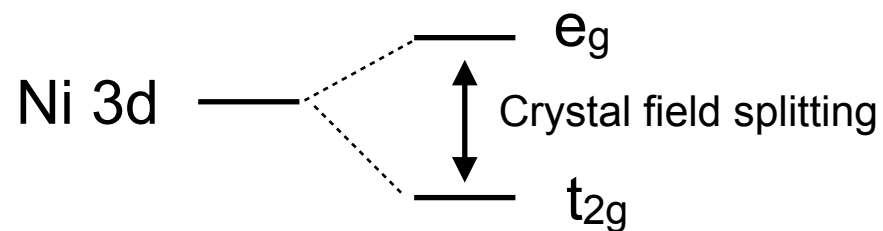
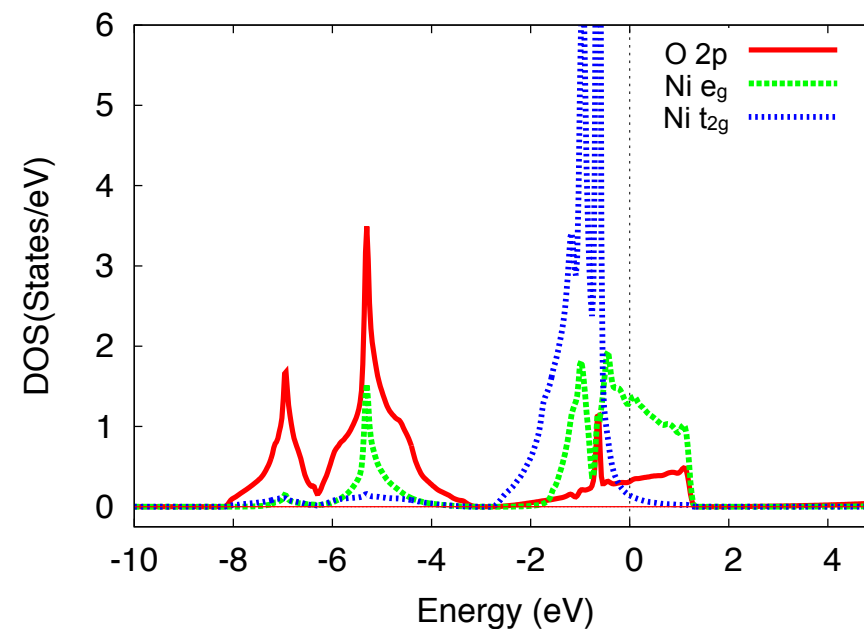
NiO (LDA, Wien2K)



Ni²⁺ (d⁸)

Partially filled

Density of states



VOLUME 53, NUMBER 24

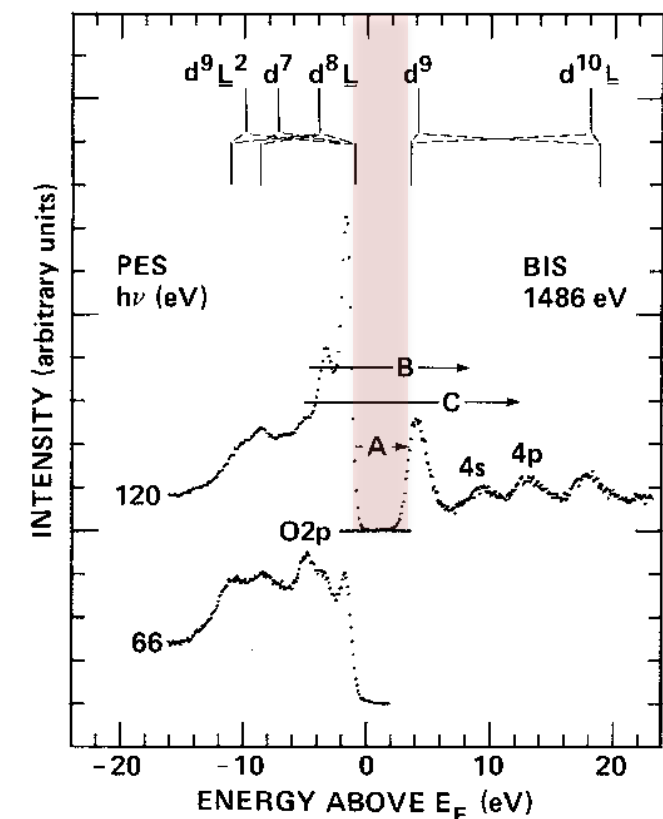
PHYSICAL REVIEW LETTERS

10 DECEMBER 1984

Magnitude and Origin of the Band Gap in NiO

G. A. Sawatzky^(a) and J. W. Allen
Xerox Palo Alto Research Center, Palo Alto, California 94304
(Received 5 July 1984)

Photoemission and bremsstrahlung-isochromat-spectroscopy data on a cleaved NiO single crystal are presented and compared to band- and cluster-theory predictions. In contrast to band-theory predictions the band gap is found to be large but not determined solely by the even larger *d-d* Coulomb interactions so that NiO is not a Mott-Hubbard insulator in the simplest sense. A large *d-d* interaction need not prevent NiS from being a metal.



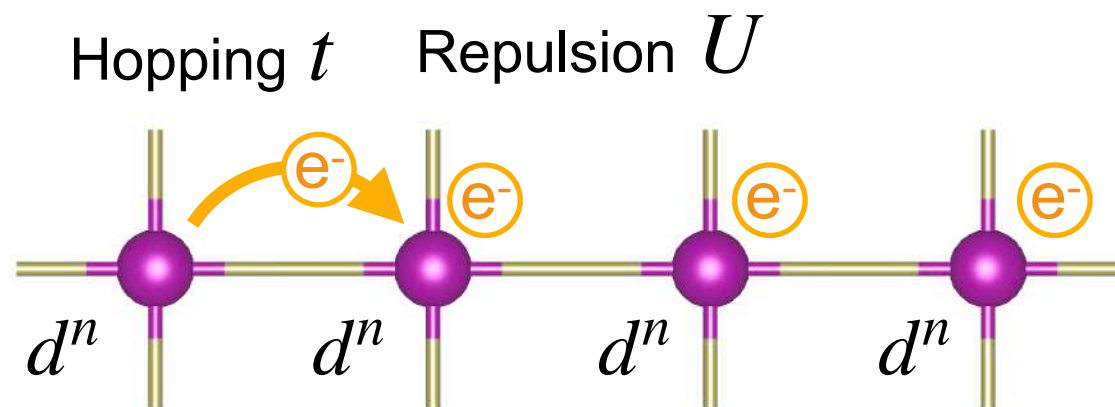
Simple DFT often fails to simulate the valence structure in d (and f) electron systems due to inaccurate treatment of electronic correlation

X-ray photoemission spectroscopies and DFT theory

Hubbard model (Kinetic energy + On-site Coulomb repulsion)

Hubbard term $H_{\text{Hubbard}} = \sum_i U n_{i\uparrow} n_{i\downarrow}$

G. Kotliar and D. Vollhardt, Physics Today 57 (2004)
: solved by dynamical mean-field theory (DMFT)

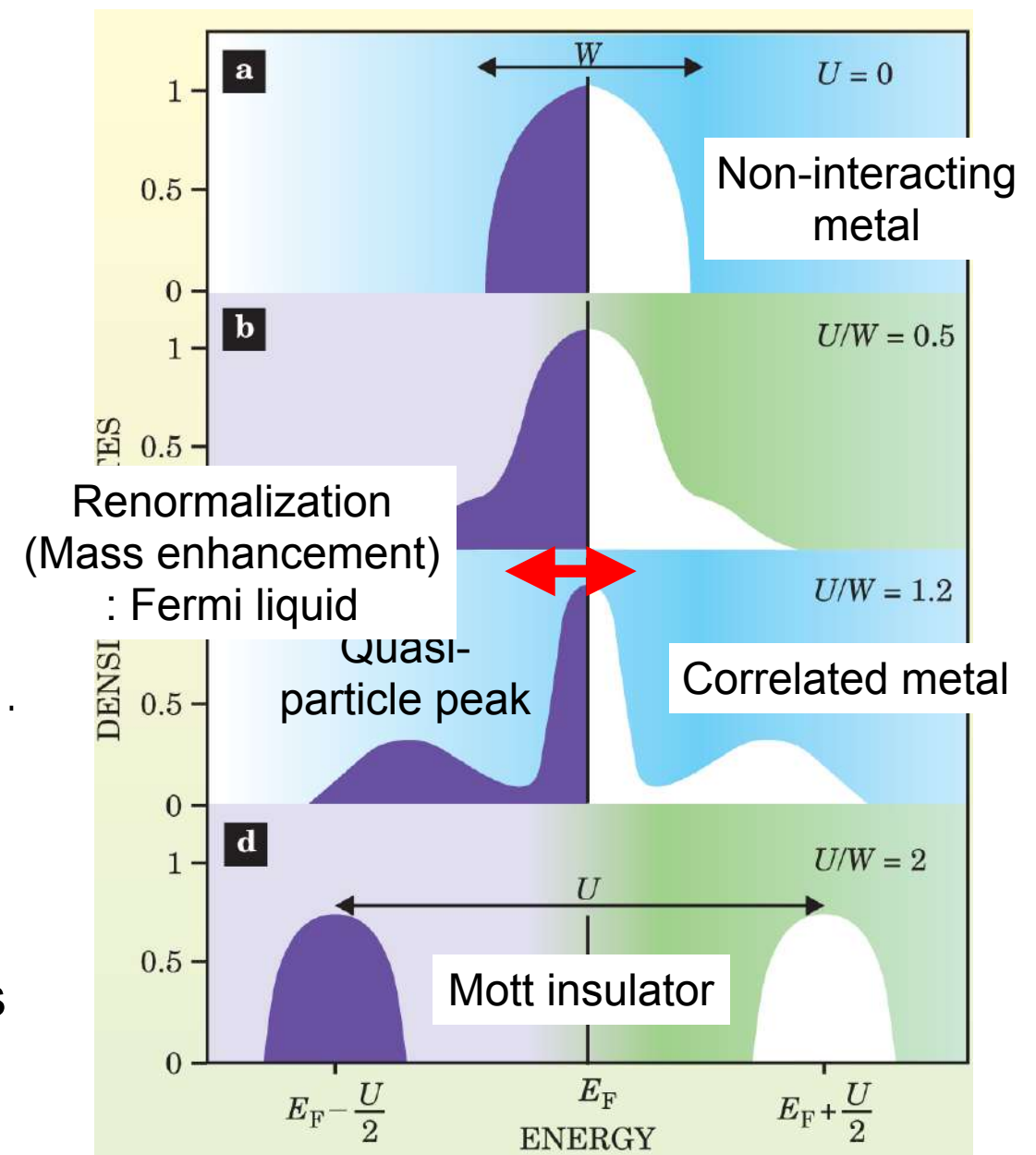


Before: d^n d^n ${}_nC_2 \times U + {}_nC_2 \times U$
 After : d^{n-1} d^{n+1} ${}_{n-1}C_2 \times U + {}_{n+1}C_2 \times U$

Energy cost U

When U is larger than the band width W ,
the system can be an insulator with localized electrons

: **Mott insulator**

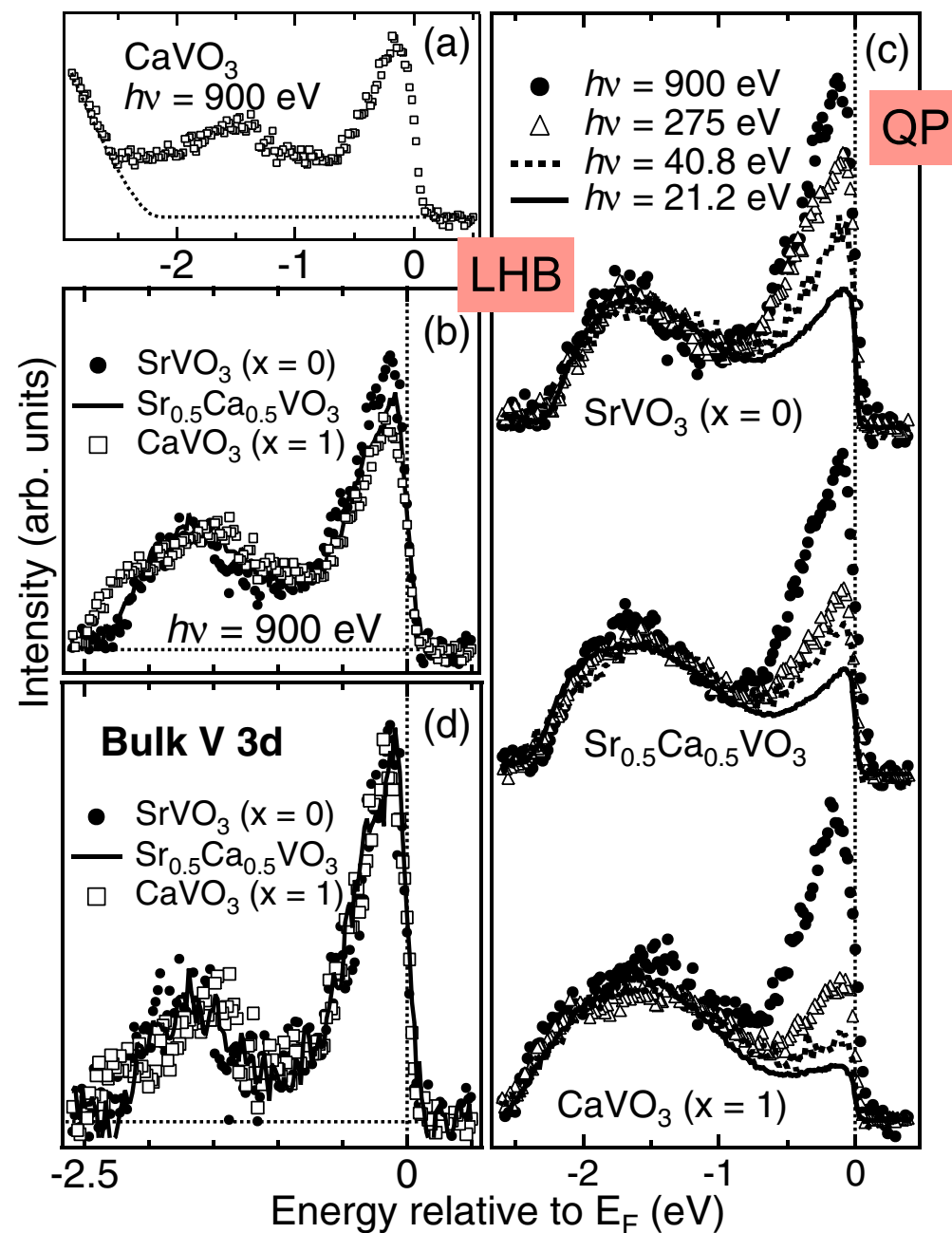


X-ray photoemission spectroscopies and DFT theory

Hubbard model (Kinetic energy + On-site Coulomb repulsion)

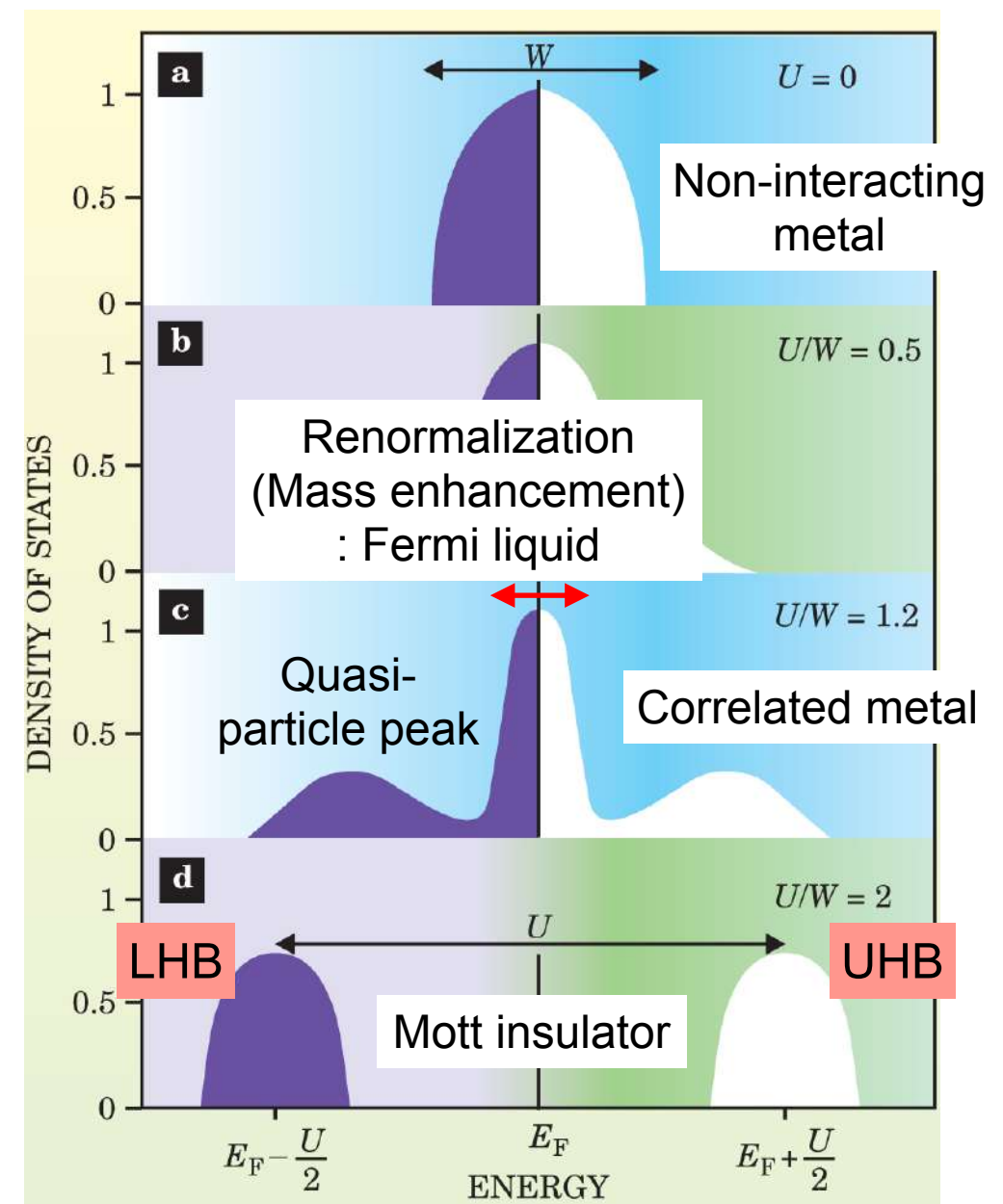
Valence-band photoemission spectroscopy in d¹ compounds

A. Sekiyama et al., Phys. Rev. Lett. **93**, 156402 (2004)



G. Kotliar and D. Vollhardt, Physics Today 57 (2004)

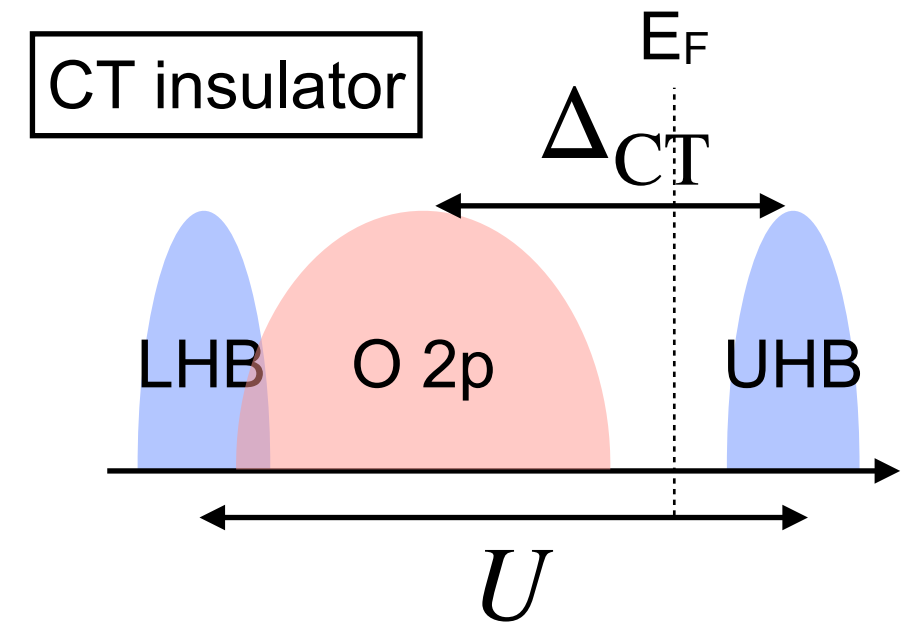
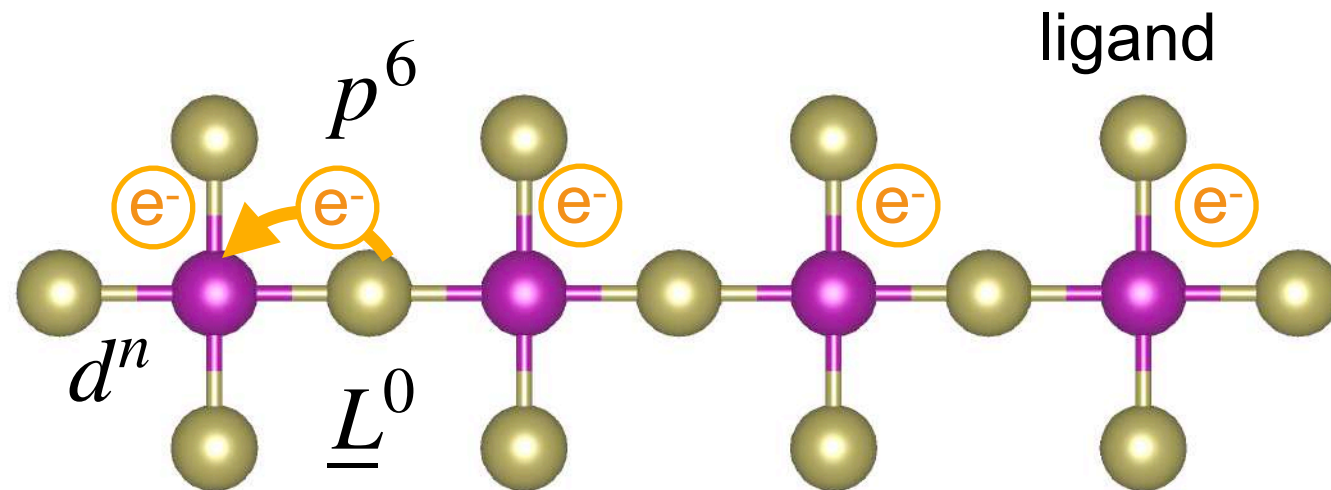
: solved by dynamical mean-field theory (DMFT)



X-ray photoemission spectroscopies and DFT theory

Hubbard model with ligand orbitals included (*dp* model)

Hubbard term $H_{\text{Hubbard}} = \sum_i U n_{i\uparrow} n_{i\downarrow}$

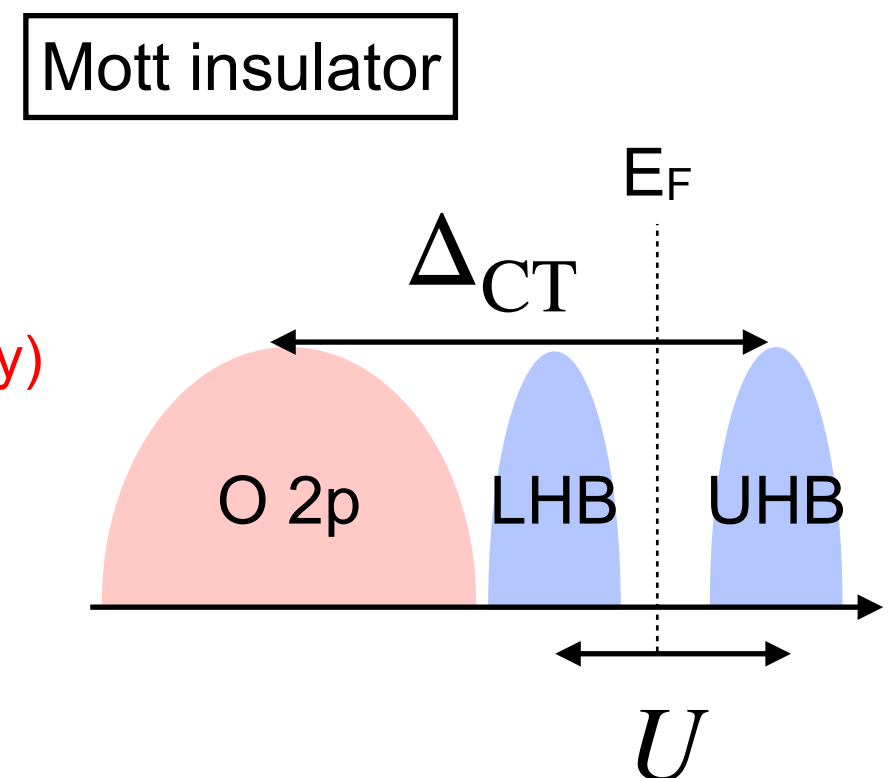


Before: $d^n \quad p^6 (\underline{L}^0) \quad n\varepsilon_d + n C_2 \times U + 6\varepsilon_p$
 After : $d^{n+1} \quad p^5 (\underline{L}^1) \quad (n+1)\varepsilon_d +_{n+1} C_2 \times U + 5\varepsilon_p$

Energy cost Δ_{CT} (Charge-transfer energy)

When $U > \Delta_{\text{CT}}$, the band gap is characterized by upper Hubbard band (above E_F) and O 2p bands (below E_F)

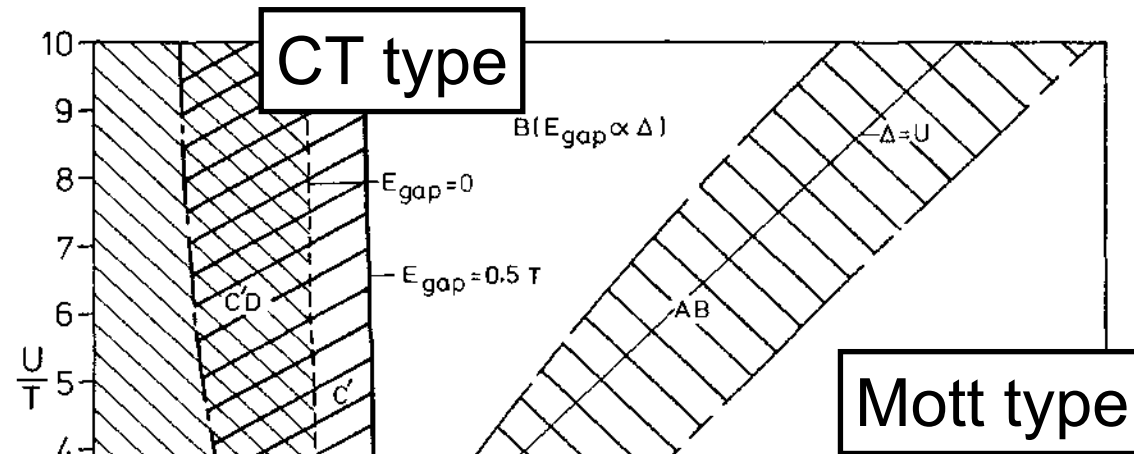
: **Charge-transfer insulator**



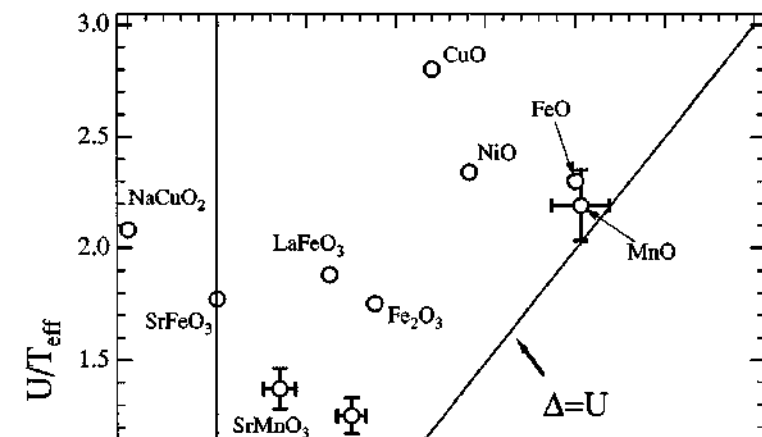
X-ray photoemission spectroscopies and DFT theory

Zaanen-Sawatzky-Allen diagram

J. Zaanen, G. A. Sawatzky, J. W. Allen, PRL **55**, 418 (1985)

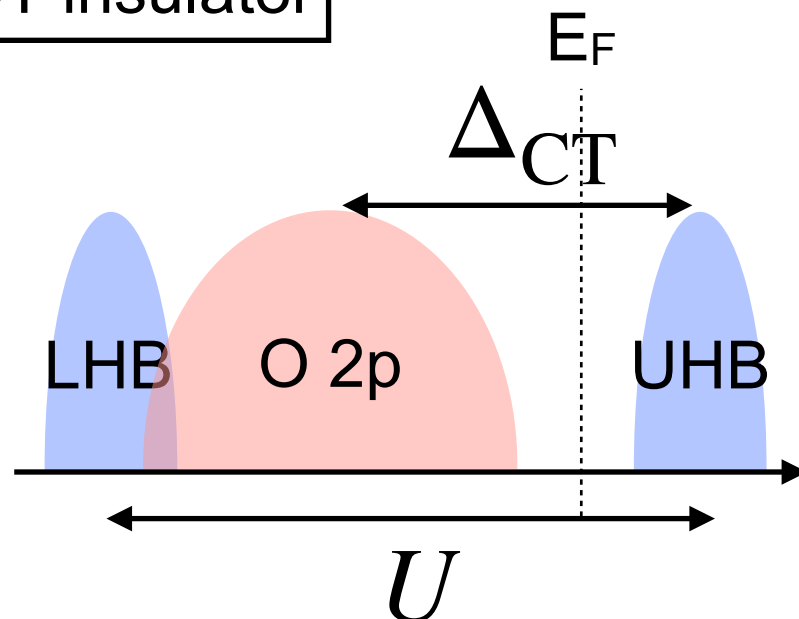


A. E. Bocquet et al., PRB **53**, 1161 (1996)

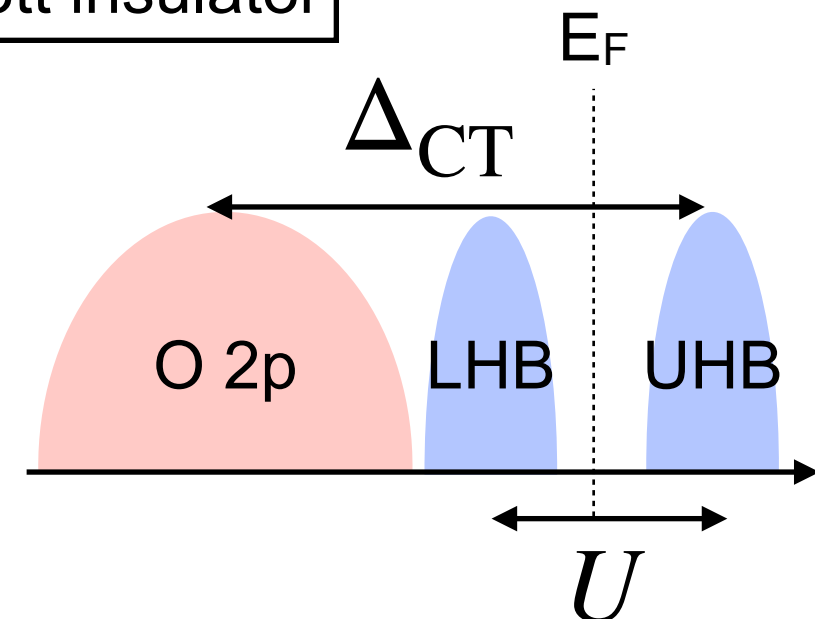


Both correlated *d* states and noninteracting (or weakly interacting) ligands are important in characterizing the low-energy excitations

CT insulator



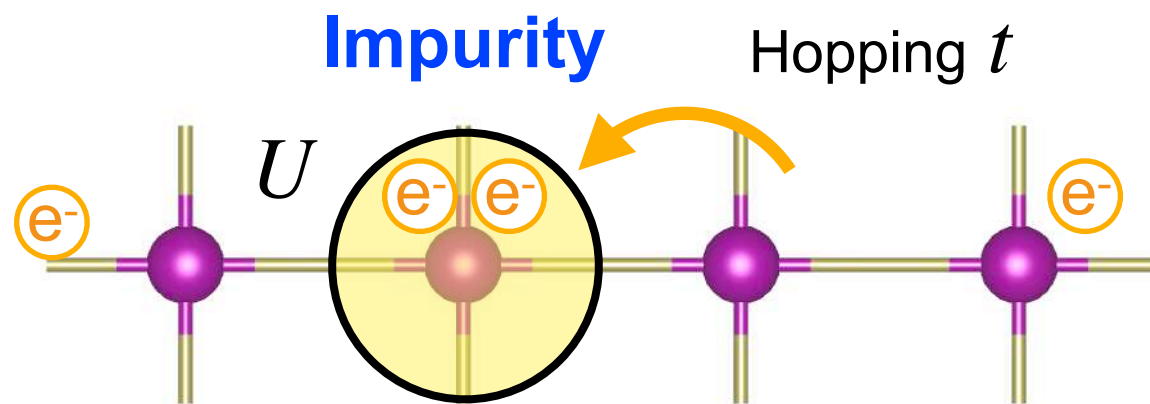
Mott insulator



Dynamical mean-field theory (DMFT)

Ref. A. Georges et al., RMP **68**, 13 (1996), G. Kotliar et al., RMP. **78**, 865 (2006)

Lattice model



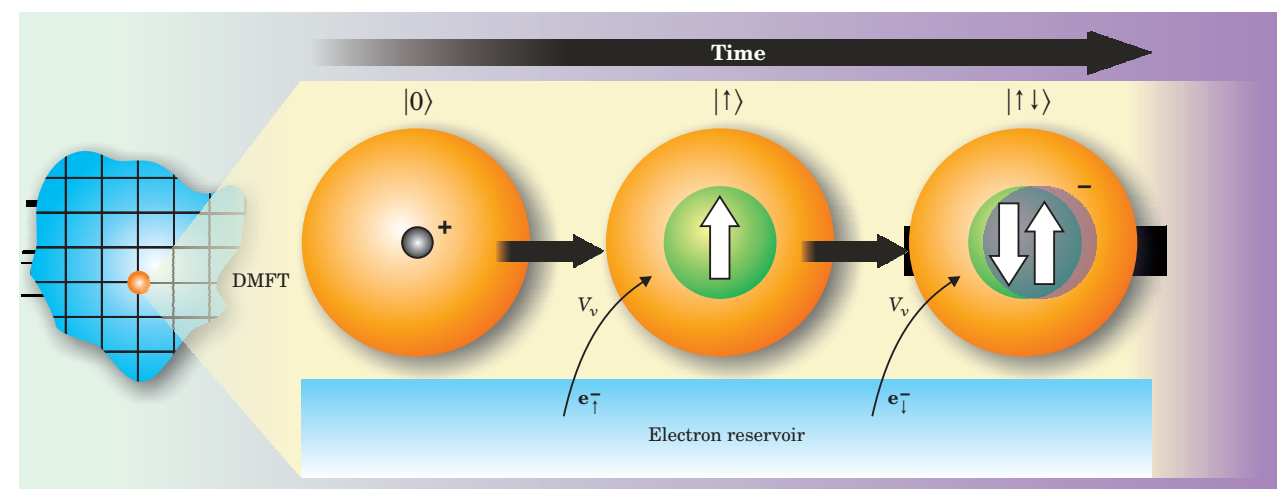
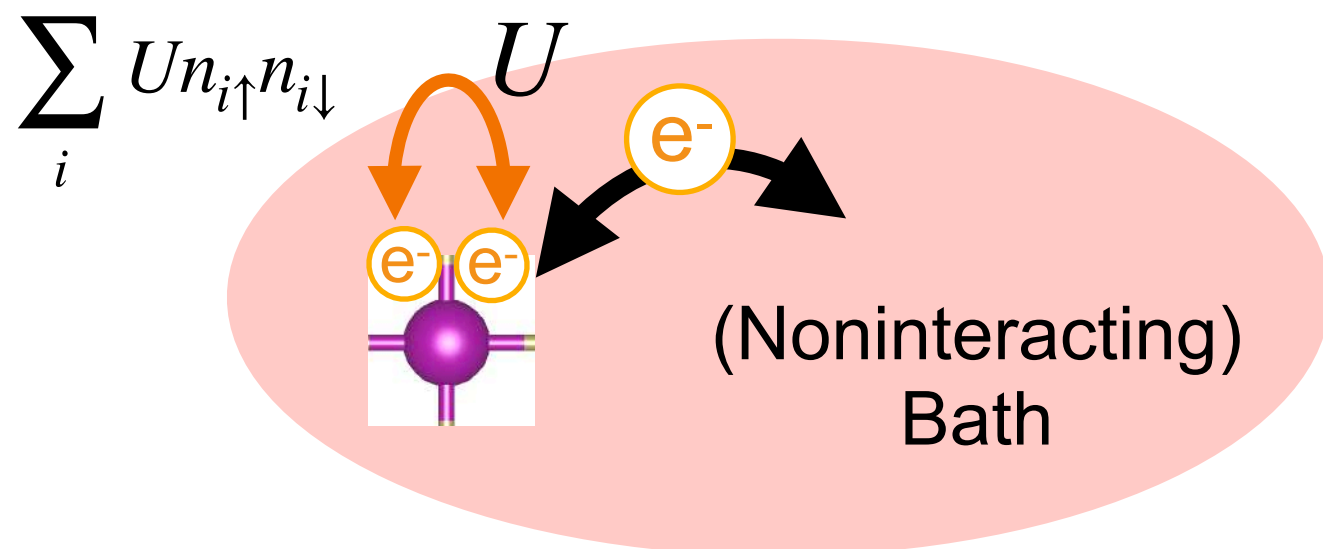
$$H_{\text{lattice}} = \sum_{i\sigma} \varepsilon_d n_{i,\sigma} + \sum_i U n_{i\uparrow} n_{i\downarrow} + t \sum_{i,\sigma} \left(d_{i+1,\sigma}^\dagger d_{i,\sigma} + d_{i,\sigma}^\dagger d_{i+1,\sigma} \right)$$

Embedding $\downarrow$

$$G_{\text{loc}}(\omega) = \frac{1}{\omega - \varepsilon_d - \Delta(\omega)} = \frac{1}{N_k} \sum_k \frac{1}{\omega - \varepsilon_k}$$

Anderson impurity model

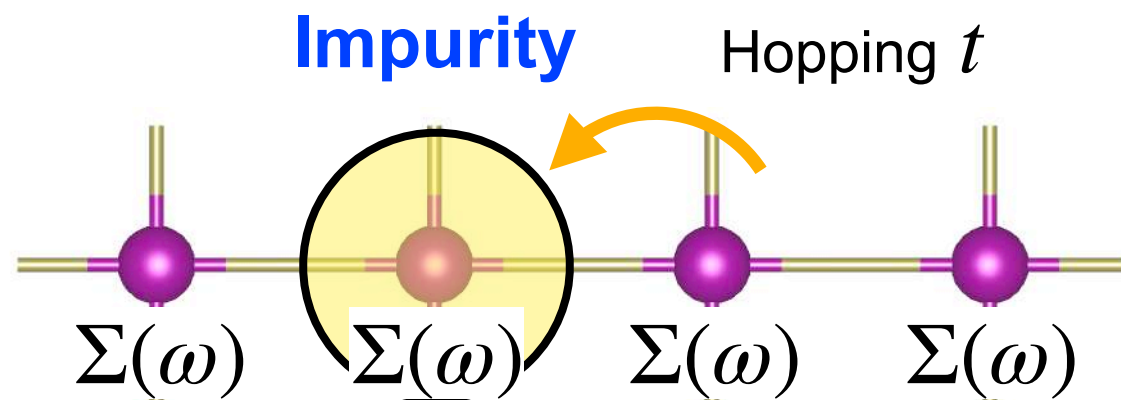
Hybridization density
(between impurity and the rest of the lattice)



Dynamical mean-field theory (DMFT)

Ref. A. Georges et al., RMP **68**, 13 (1996), G. Kotliar et al., RMP. **78**, 865 (2006)

Lattice model



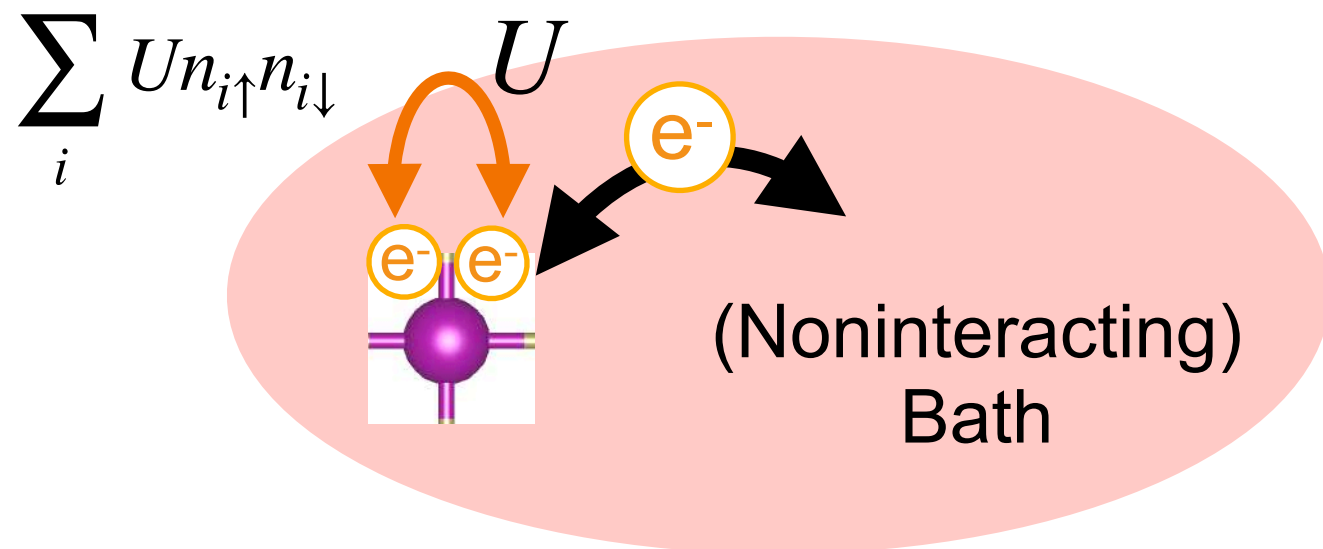
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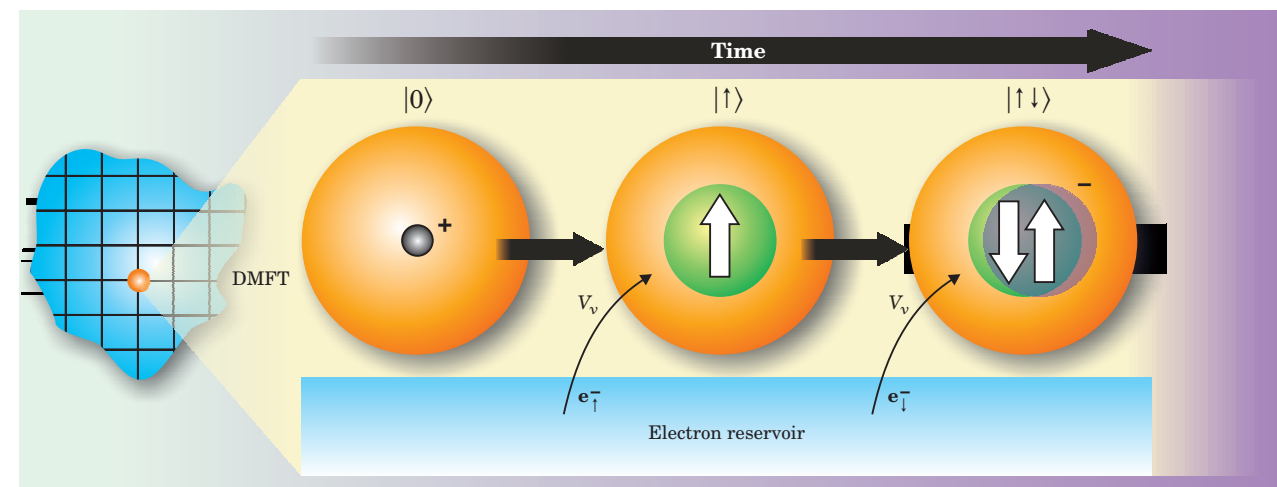
$$G_{\text{AIM}}(\omega) = \frac{1}{\omega - \varepsilon_d - \Delta(\omega) - \Sigma(\omega)}$$

$\Sigma(\omega, \mathbf{k})$
No $\mathbf{k}$ dep.

Anderson impurity model



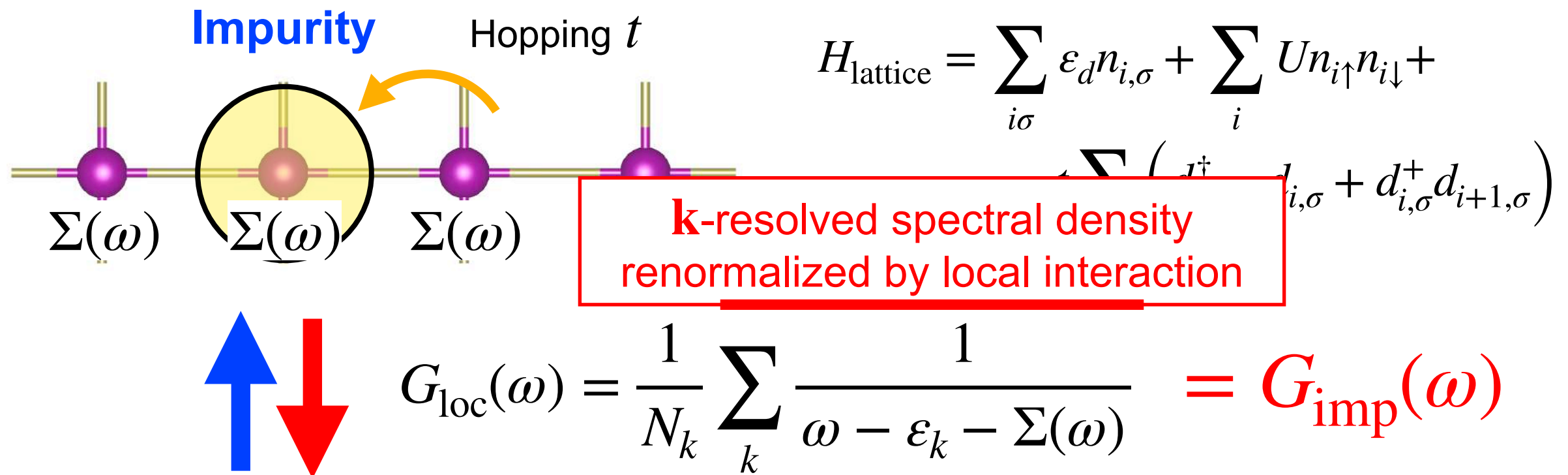
Local electron self-energy
(correlated dynamics at transition-metal site)



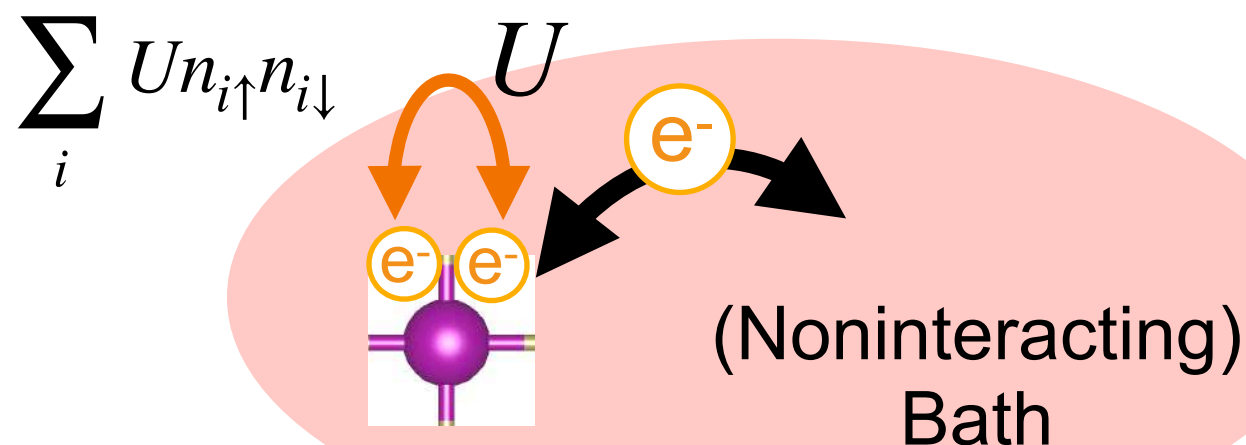
Dynamical mean-field theory (DMFT)

Ref. A. Georges et al., RMP **68**, 13 (1996), G. Kotliar et al., RMP. **78**, 865 (2006)

Lattice model



Anderson impurity model



: self-consistent condition

$\Sigma(\omega, \mathbf{k})$: exact in infinite lattice dimension
(incl. all local skeleton diagram contributions)
No $\mathbf{k}$ dep.

Extension of DMFT to recover $\mathbf{k}$ -dependence

- Cluster embedding
- Diagrammatic extension ...

Ref. G. Rohrenger et al., Rev. Mod. Phys. **90**, 025003 (2018)

T. Maier et al., Rev. Mod. Phys. **77**, 1027 (2005)

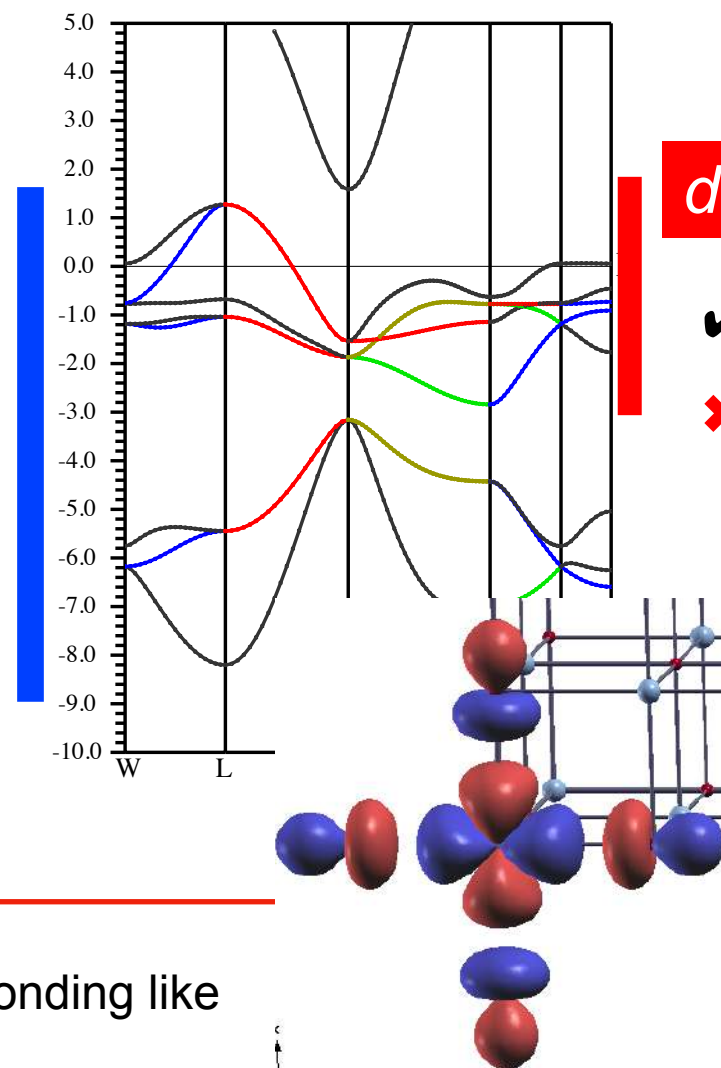
DFT + Dynamical mean-field theory (DMFT)

dp space (Ni 3d + O 2p)

✓ Both low- and high-energy physics can be captured, incl. cases where ligands (non-interacting bands) are directly involved

✗ The double-counting correction must be properly determined

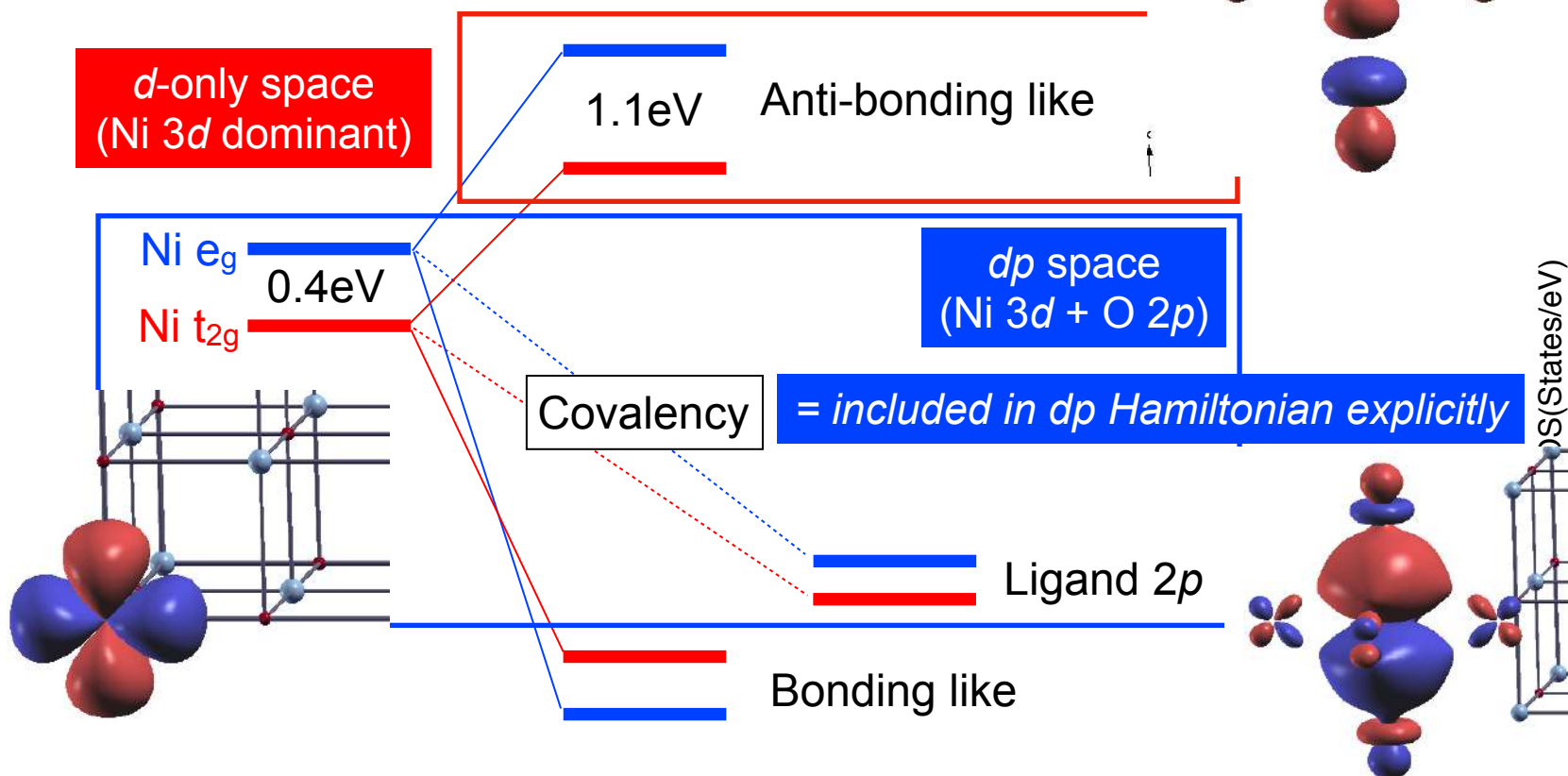
NiO (LDA, Wien2K)



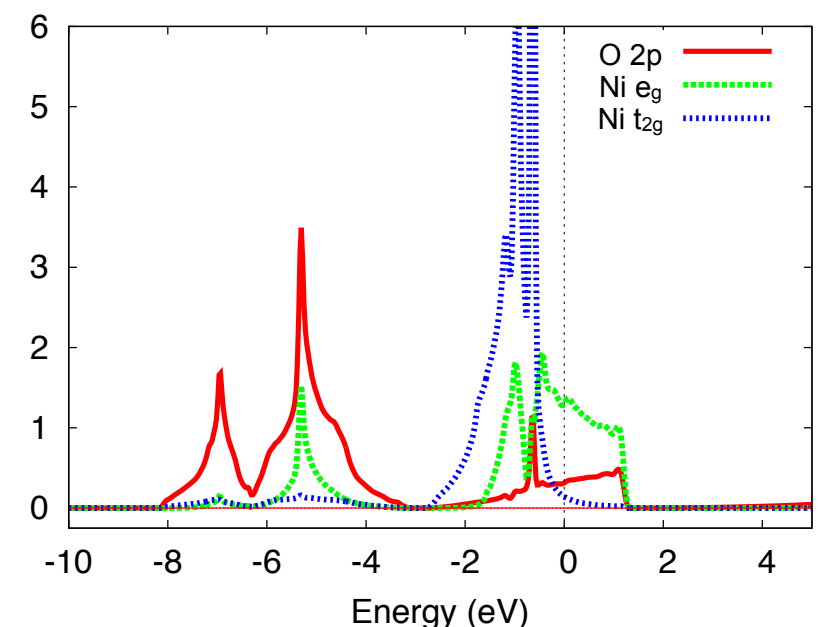
There are different implementations, see e.g.
K. Haule et al., Phys. Rev. Lett. **115**, 256402 (2015)

d -only space (Ni 3d dominant)

✓ Computationally cheap, simple
✗ Ligand p not included (explicitly)
(Covalent bonding information encoded in the low-energy band)



Density of states



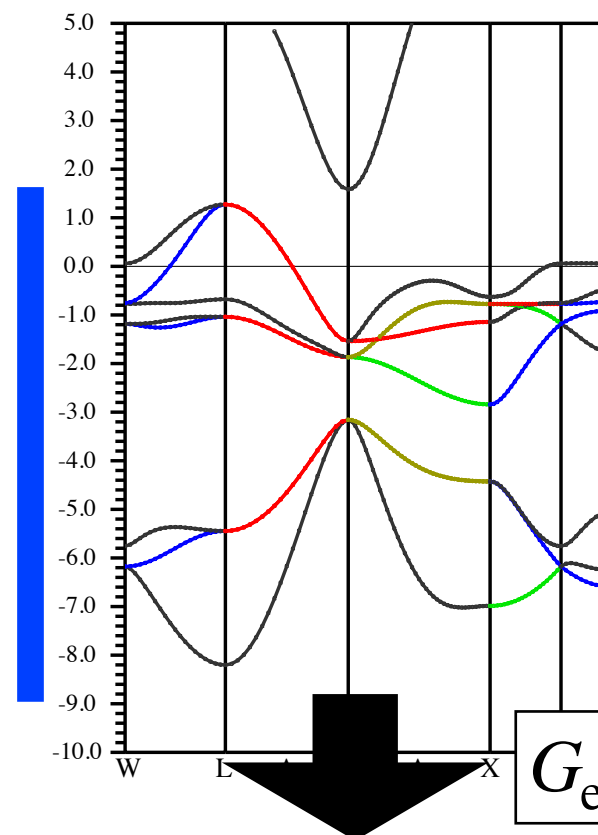
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NiO (LDA, Wien2K)



$$G_{\text{eff}} = P G_{\text{KS}} P^+$$

There are different implementations, see e.g.

K. Haule et al., Phys. Rev. Lett. **115**, 256402 (2015)

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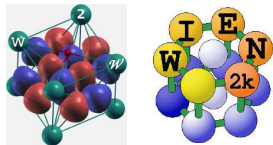
Tight-binding model from the target bands (d -only, dp) via wannier function

WANNIER90

wannier90: A tool for obtaining maximally-localised Wannier functions

A. A. Mostofi, et al., Comput. Phys. Commun. 178, 685 (2008)

with



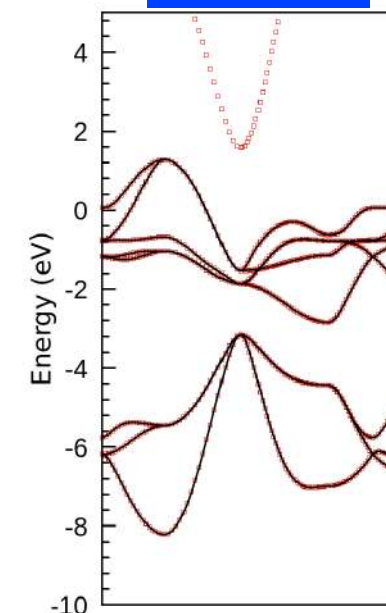
$$|\mathbf{R}, n\rangle = \frac{V}{(2\pi)^3} \int_{\text{BZ}} \sum_m U_{nm}^{(\mathbf{k})} |\psi_m(\mathbf{k})\rangle e^{-i\mathbf{k}\cdot\mathbf{R}} d^3\mathbf{k}$$

Bloch bands

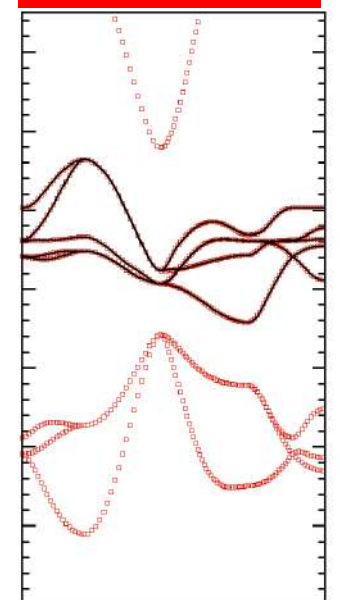
(Localized) Wannier functions
= basis for tight-binding model

The $\mathbf{k}$ -dependent phase (unitary matrix) is often chosen to minimize the spread of Wannier functions.

dp space



d -only space



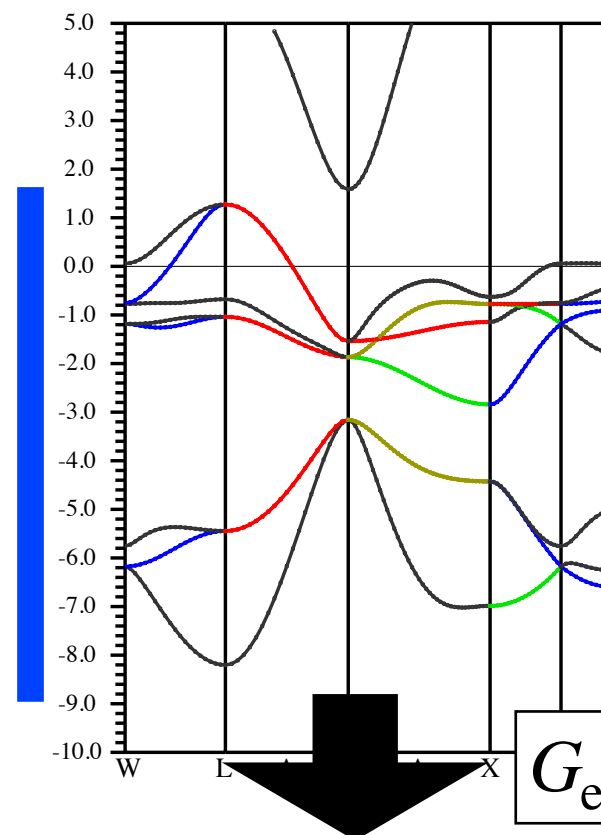
DFT + Dynamical mean-field theory (DMFT)

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There are different implementations, see e.g.

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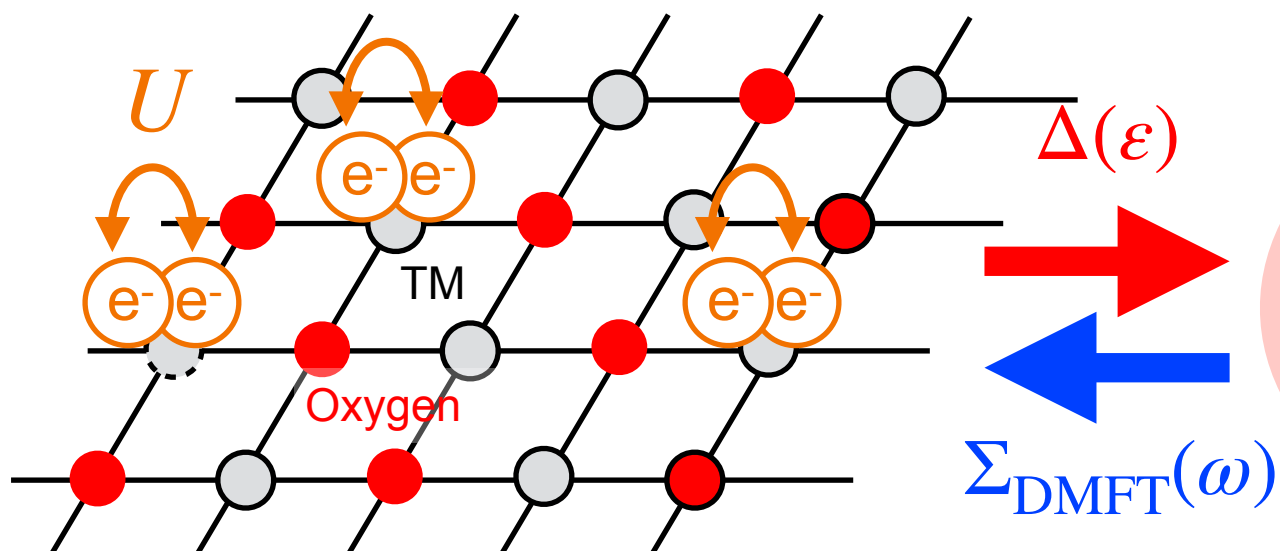
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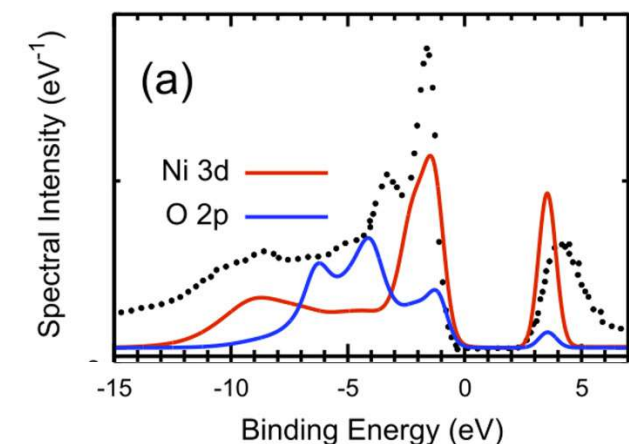
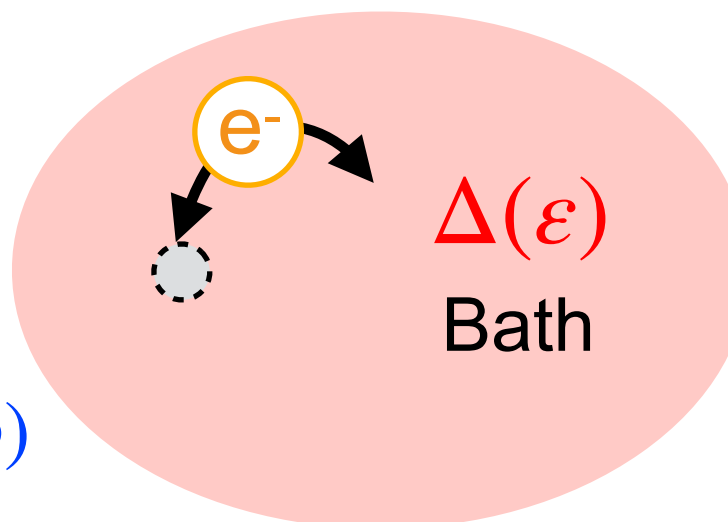
$$G_{\text{eff}} = P G_{\text{KS}} P^+$$

Tight-binding model from the target bands (d -only, dp) via wannier function

Non-interacting $\rightarrow$ Interacting



Embedding: lattice $\rightarrow$ Impurity coupled with noninteracting bath



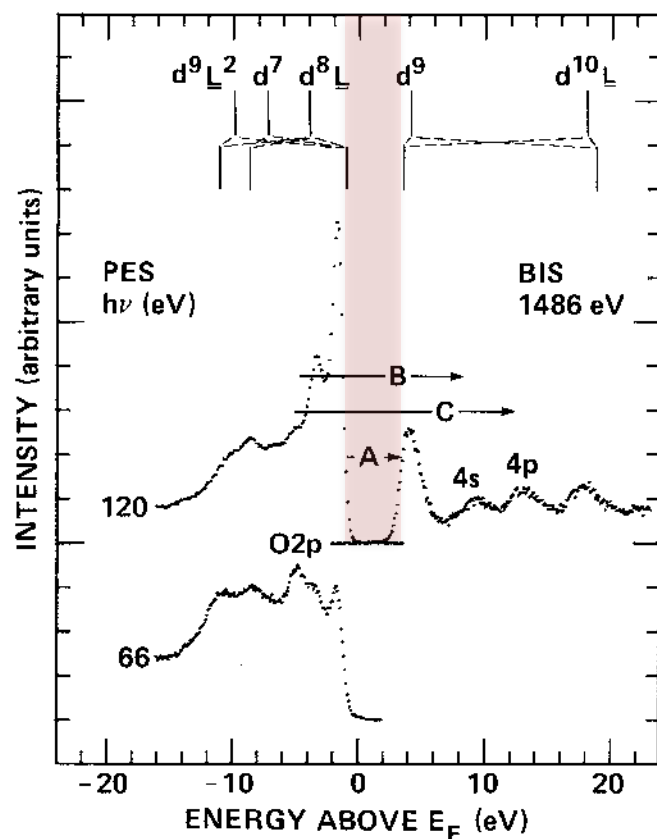
Magnitude and Origin of the Band Gap in NiO

G. A. Sawatzky^(a) and J. W. Allen

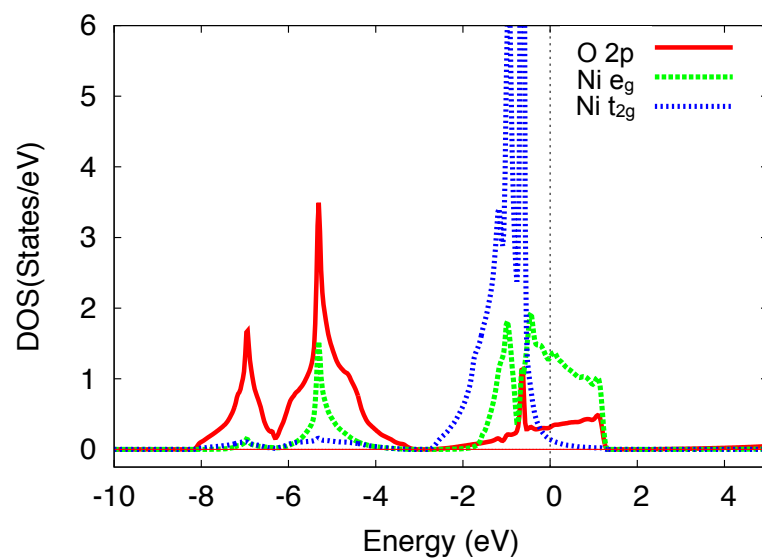
Xerox Palo Alto Research Center, Palo Alto, California 94304

(Received 5 July 1984)

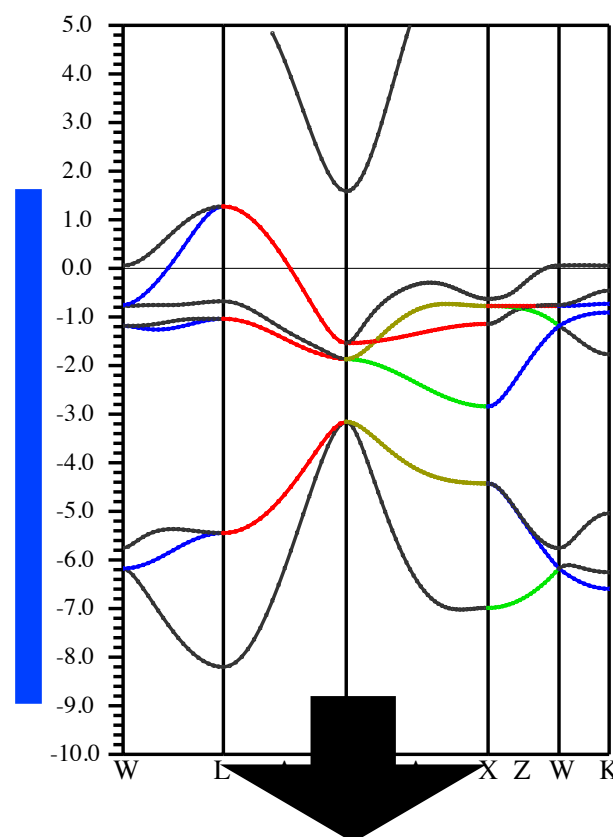
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LDA density of states



NiO (LDA, Wien2K)



There are different implementations, see e.g.

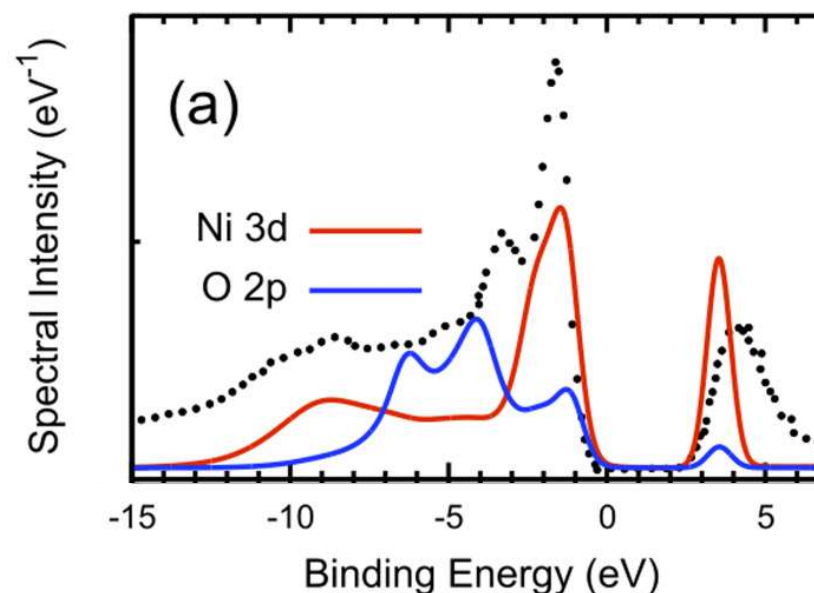
K. Haule et al., Phys. Rev. Lett. **115**, 256402 (2015)

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(Covalent bonding information encoded in the low-energy band)

DFT + DMFT

A. Hariki et al., Phys. Rev. B **101**, 115130 (2020)



- ✓ Large insulating gap in paramagnetic solution
- ✓ Complex spectral distribution due to many-body effect

DFT + Dynamical mean-field theory (DMFT)

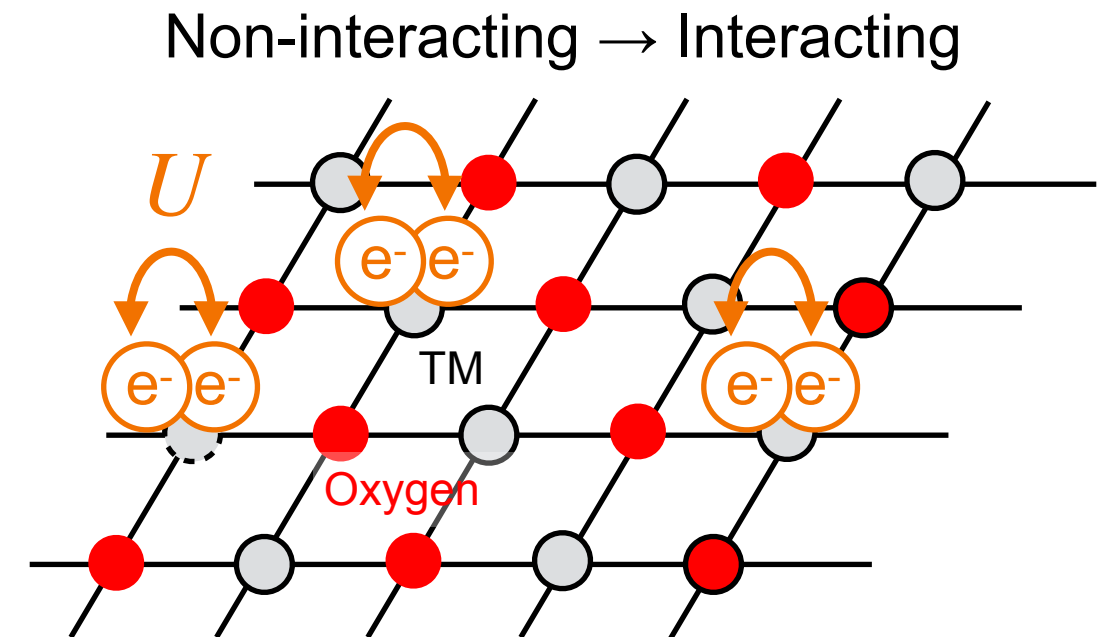
Q1. How to determine the interacting part of the Hamiltonian

DFT based routes

- ✓ Constrained LDA, **Constrained RPA**
F. Aryasetiawan et al., Phys. Rev. B **70**, 195104 (2004)

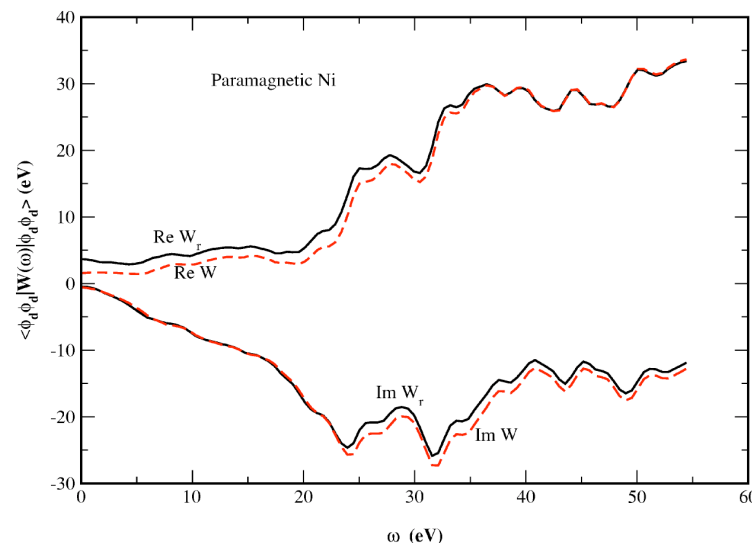
Experimental routes

- ✓ Fitting various spectroscopic experiment

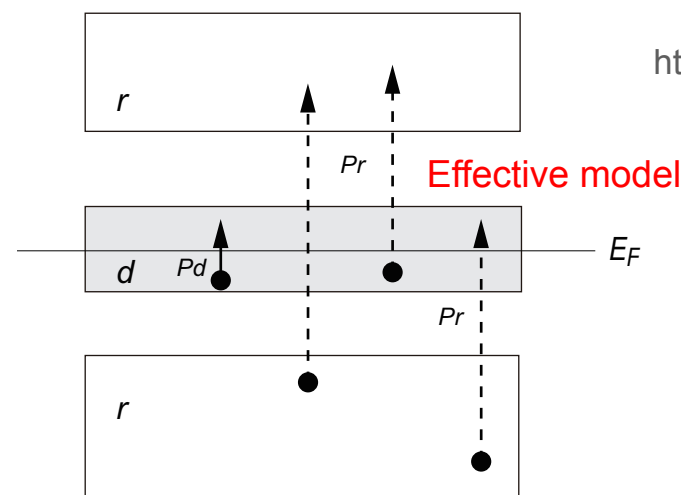


Screened interaction W

F. Aryasetiawan et al., Phys. Rev. B **70**, 195104 (2004)



Polarisation: $P = P_d + P_r$



Julich Autumn School on Correlated Electrons (2011)

<https://www.cond-mat.de/events/correl11/manuscripts/aryasetiawan.pdf>

7 The Constrained RPA Method for Calculating the Hubbard U from First-Principles

F. Aryasetiawan,¹ T. Miyake,^{2,3} and R. Sakuma¹

¹ Graduate School of Advanced Integration Science
Chiba University, Japan

² Nanosystem Research Institute, AIST, Japan

³ Japan Science and Technology Agency, CREST

Fully screened Coulomb interaction

$$W = [1 - W_d P_d]^{-1} W_d$$

**Screened Coulomb
interaction in effective model**

Quantifying the U 5*f* covalence and degree of localization in U intermetallics

Andrea Marino,^{1,2,*} Denise S. Christovam,¹ Daisuke Takegami,^{1,3} Johannes Falke,¹ Miguel M. F. Carvalho,^{1,4} Takaki Okauchi,⁵ Chun-Fu Chang,¹ Simone G. Altendorf,^{1,4,†} Andrea Amorese,^{1,4,‡} Martin Sundermann,^{1,6} Andrei Gloskovskii,⁶ Hlynur Gretarsson,^{6,7} Bernhard Keimer,⁷ Alexandr V. Andreev,⁸ Ladislav Havela,⁹ Andreas Leithe-Jasper,¹ Andrea Severing,^{4,1} Jan Kuneš,¹⁰ Liu Hao Tjeng,^{1,‡} and Atsushi Hariki^{5,§}

¹Max Planck Institute for Chemical Physics of Solids, Nöthnitzer Straße 40, 01187 Dresden, Germany

²Institute of Solid State and Materials Physics, TU Dresden, 01069 Dresden, Germany

³Department of Applied Physics, Waseda University, 3-4-1 Okubo, Shinjuku-ku, Tokyo 169-8555, Japan

⁴Institute of Physics II, University of Cologne, Zùlpicher Straße 77, 50937 Cologne, Germany

⁵Department of Physics and Electronics, Osaka Metropolitan University 1-1 Gakuen-cho, Nakaku, Sakai, Osaka 599-8531, Japan

⁶PETRA III, Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, 22607 Hamburg, Germany

⁷Max Planck Institute for Solid State Research, Heisenbergstraße 1, 70569 Stuttgart, Germany

⁸Institute of Physics, Academy of Sciences of the Czech Republic, Na Slovance 1999/2, 182 21 Prague 8, Czech Republic

⁹Department of Condensed Matter Physics, Faculty of Mathematics and Physics, Charles University, Ke Karlovu 5, 121 16 Prague 2, Czech Republic

¹⁰Department of Condensed Matter Physics, Faculty of Science, Masaryk University, Kotlářská 2, 611 37 Brno, Czechia

- ✓ UGa₂ (5*f* localized), UB₂ (5*f* delocalized)
- with mixed (or fluctuating) valence
- ✓ Different elements (orbital) have different photoionization cross-sections

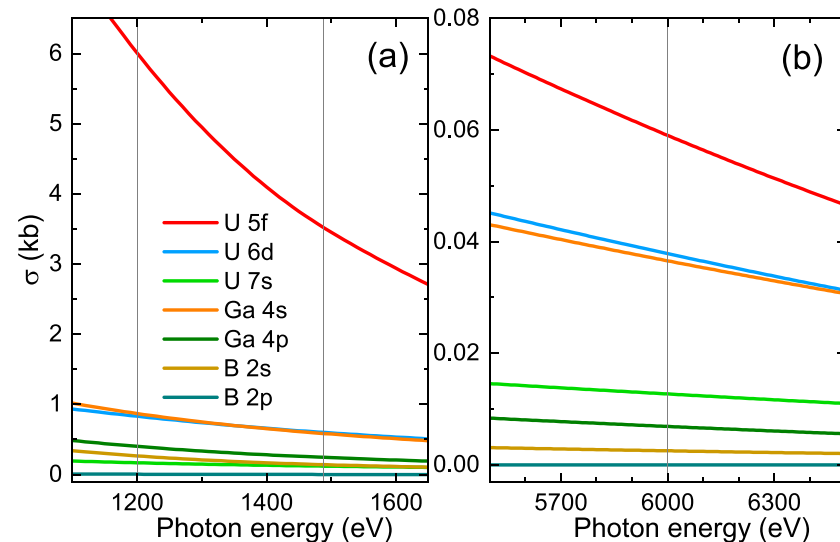
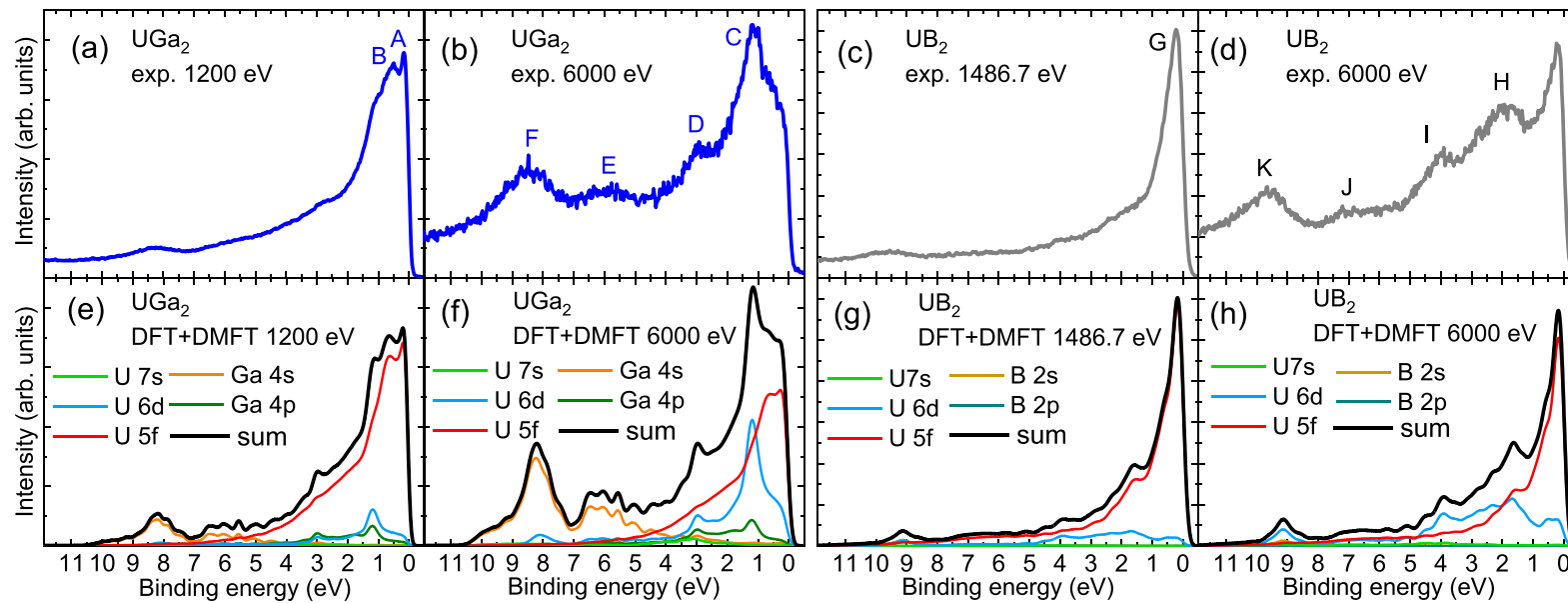
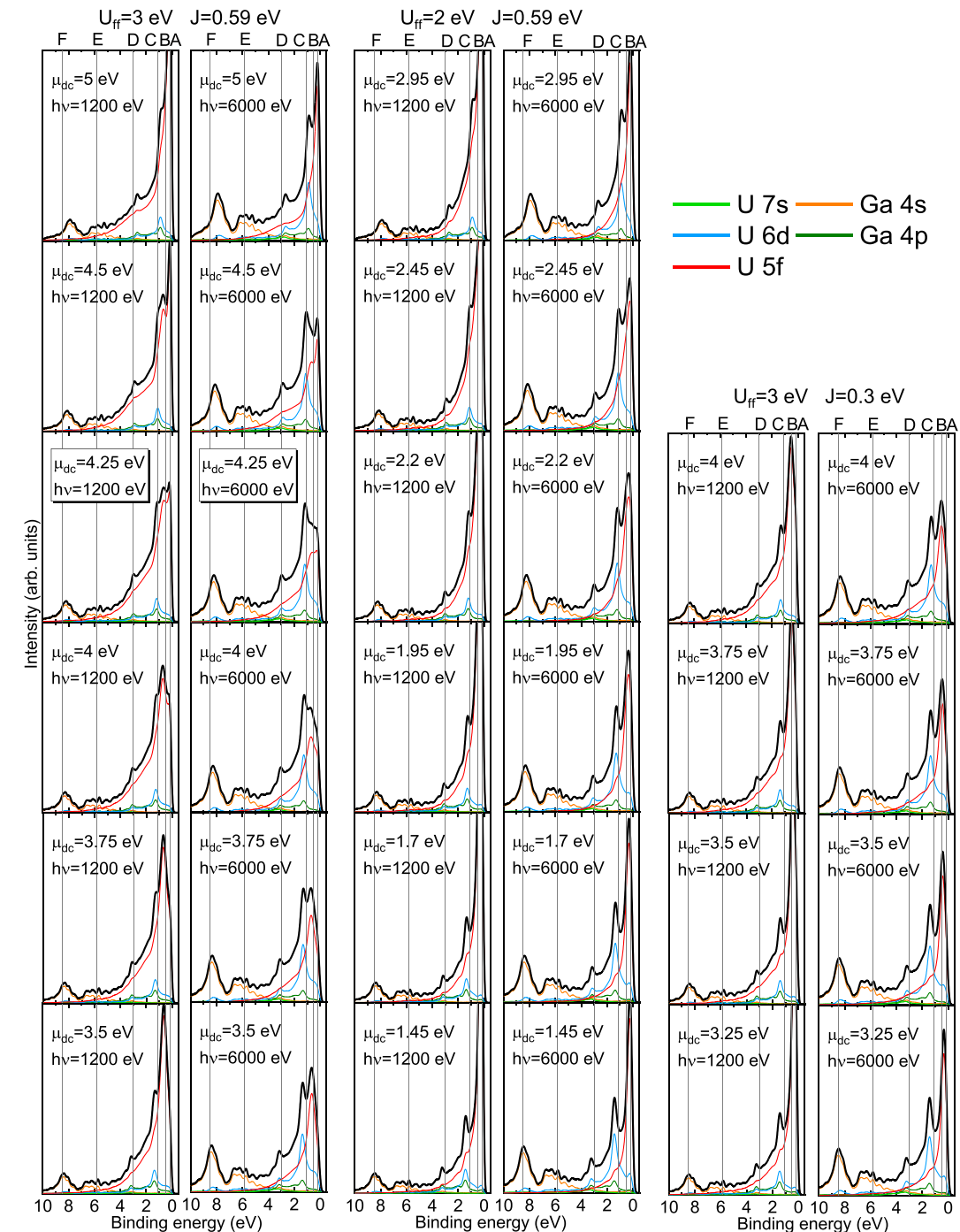


FIG. 3. Photoionization cross sections of U 5*f*, U 6*d*, U 7*s*, Ga 4*s*, Ga 4*p*, B 2*s*, B 2*p* as interpolated from Refs. [25–27]. The vertical lines indicate the photon energies where the experiments



CaCu₃Ru₄O₁₂: A High-Kondo-Temperature Transition-Metal Oxide

D. Takegami¹, C.-Y. Kuo,^{1,2} K. Kasebayashi,³ J.-G. Kim,⁴ C. F. Chang,¹ C. E. Liu,^{1,5} C. N. Wu,^{1,6} D. Kasinathan,¹ S. G. Altendorf,¹ K. Hofer,¹ F. Meneghin,¹ A. Marino,¹ Y. F. Liao,² K. D. Tsuei,² C. T. Chen,² K.-T. Ko,⁴ A. Günther,⁷ S. G. Ebbinghaus,⁸ J. W. Seo,¹ D. H. Lee,¹ G. Ryu,¹ A. C. Komarek,¹ S. Sugano,⁹ Y. Shimakawa,⁹ A. Tanaka,¹⁰ T. Mizokawa,¹¹ J. Kuneš,¹² L. H. Tjeng,^{1,*} and A. Hariki^{3,12,†}

¹Max Planck Institute for Chemical Physics of Solids, Nöthnitzer Straße 40, 01187 Dresden, Germany

²National Synchrotron Radiation Research Center, 101 Hsin-Ann Road, 30076 Hsinchu, Taiwan

³Department of Physics and Electronics, Osaka Prefecture University,

1-1 Gakuen-cho, Nakaku, Sakai, Osaka 599-8531, Japan

⁴Department of Physics, POSTECH, Pohang 37673, Korea

⁵Department of Electrophysics, National Yang Ming Chiao Tung University (NYCU), Hsinchu 30010, Taiwan

⁶Department of Physics, National Tsing Hua University, Hsinchu 30013, Taiwan

⁷Experimental Physics V, University of Augsburg, 86135 Augsburg, Germany

⁸Institute of Chemistry, Martin Luther University Halle-Wittenberg, 06120 Halle, Germany

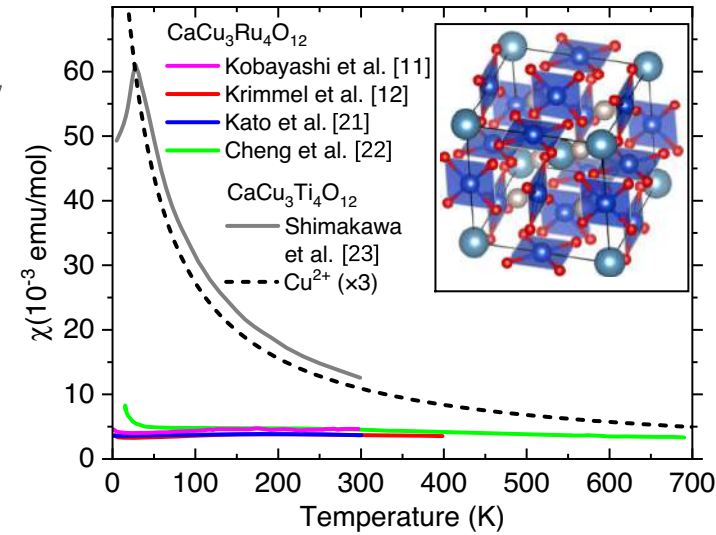
⁹Institute for Chemical Research, Kyoto University, Uji, Kyoto 611-0011, Japan

¹⁰Quantum Matter Program, Hiroshima University, Higashi-Hiroshima 739-8530, Japan

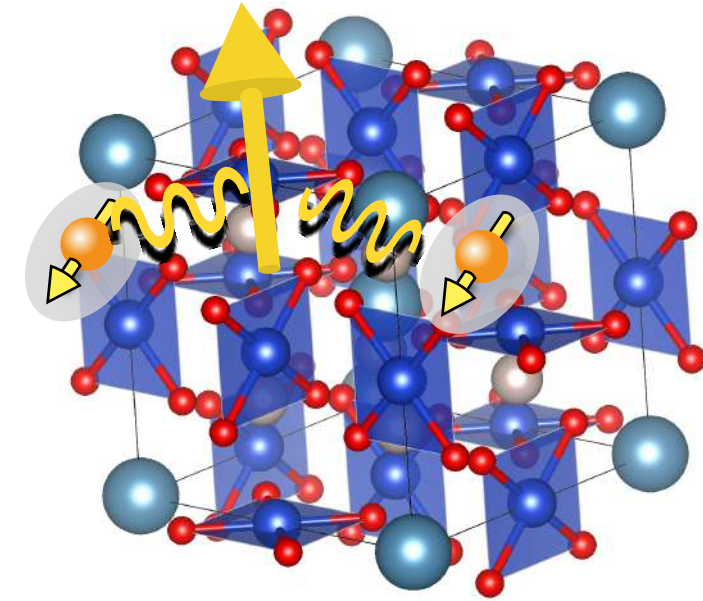
¹¹Department of Applied Physics, Waseda University, Shinjuku, Tokyo 169-8555, Japan

¹²Institute of Solid State Physics, TU Wien, 1040 Vienna, Austria

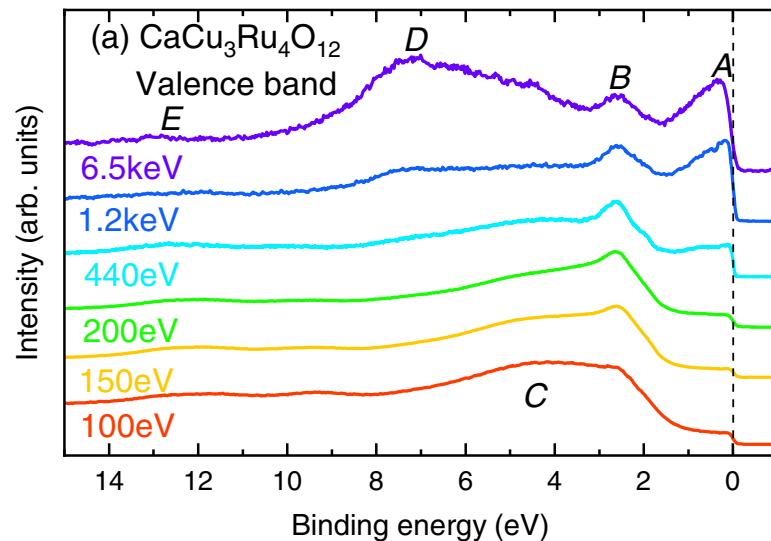
Experimental magnetic susceptibility



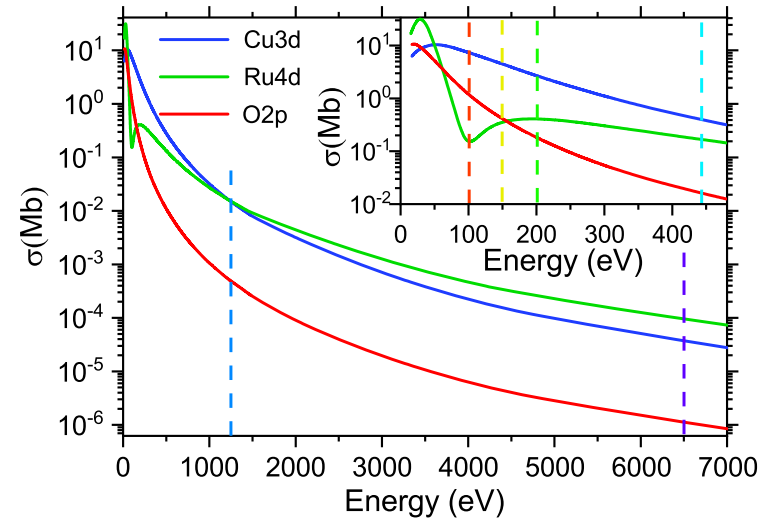
Cu²⁺: S=1/2



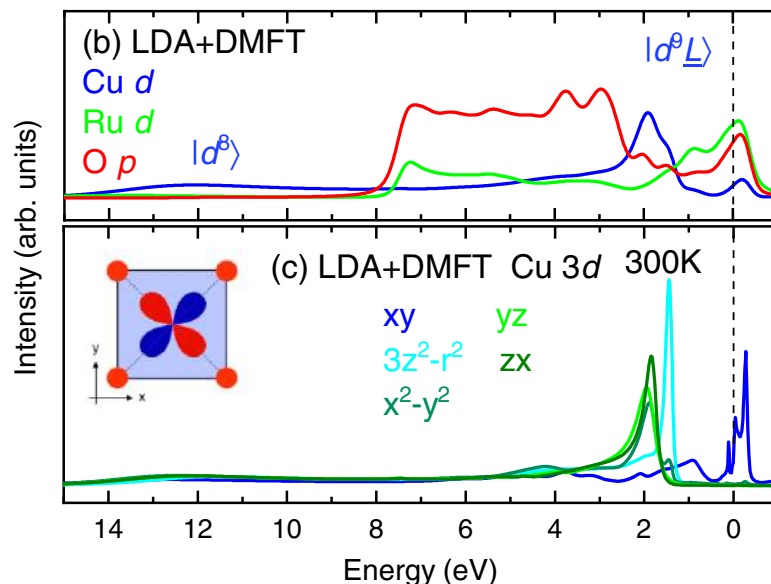
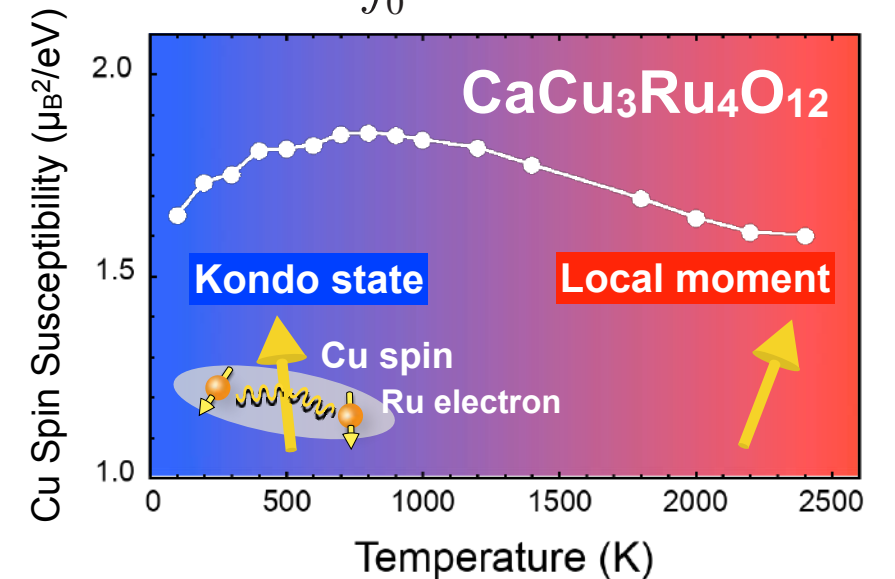
Photon-energy dependent PES



Photoionization cross-section



$$\chi_{\text{loc}}(T) = \int_0^{1/T} d\tau \langle m_z(\tau) m_z(0) \rangle.$$



- ✓ Different elements (orbital) have different photoionization cross-sections
- ✓ DMFT is capable of many-body physics (Kondo effect) in complex correlated materials

DFT + Dynamical mean-field theory (DMFT)

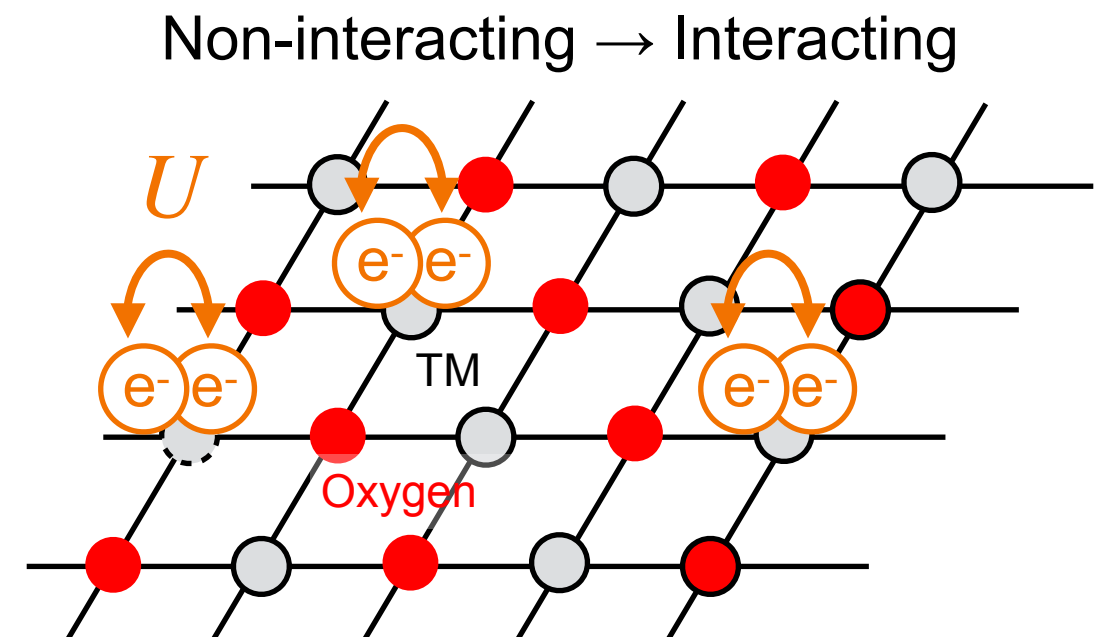
Q1. How to determine the interacting part of the Hamiltonian

DFT based routes

- ✓ Constrained LDA, **Constrained RPA**
F. Aryasetiawan et al., Phys. Rev. B **70**, 195104 (2004)

Experimental routes

- ✓ Fitting various spectroscopic experiment



Q2. How to determine double-counting correction?

$$\varepsilon_d - \mu_{\text{dc}} + \Sigma_{\text{DMFT}}(\omega)$$

DFT routes

- ✓ Ansatz for energy functional incl. U

Ref. Double counting in LDA + DMFT — The example of NiO
M. Karolak et al., J. Electron Spectrosc. Relat. Phenom. **181** (2010) 11–15

Exact double-counting

K. Haule, Phys. Rev. Lett. **115**, 196403 (2015)

Experimental routes

- ✓ Fitting valence-band photoemission spectra
measured with different photon energies (cross-section)

Refs.
A. Marino, A. Hariki et al., Phys. Rev. Research **6**, 033068 (2024)
K. Higashi, M. Winder, J. Kuneš, and A. Hariki, Phys. Rev. X **11**, 041009 (2021)
D. Takegami, A. Hariki et al., Phys. Rev. X **12**, 011017 (2022)

Q3. How to solve the impurity Anderson model?

- ✓ Development of various numerically-reliable impurity solver
(e.g. continuous time quantum Monte-Carlo solver)

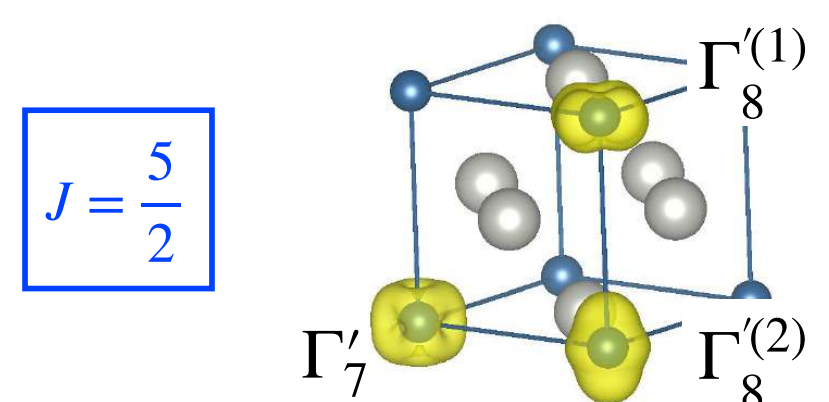
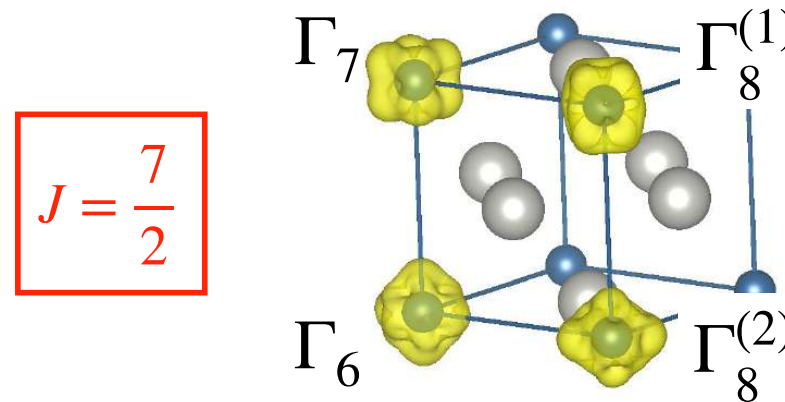
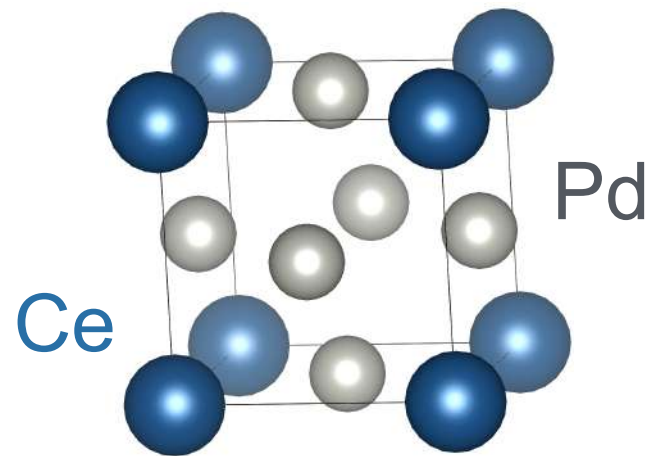
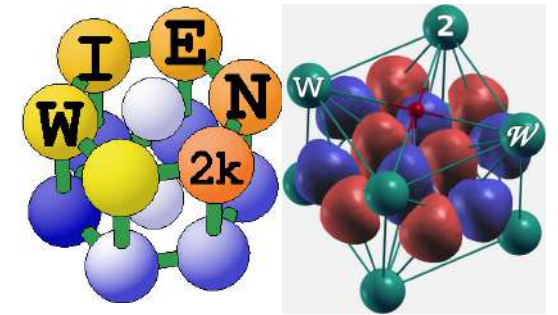
DCore **DCore**
integrated DMFT software for Correlated electrons

Kondo Dynamics by RIXS: CePd₃

M. C. Rahn, [AH](#) et al.,
Nat. Commun. **13**, 6129 (2022)

- Archetypal Kondo lattice
- $T_{\text{coh}} \sim 130\text{K}$, $T_K \sim 600\text{K}$
- $N_f \sim 0.75$ (from XAS)

4f wannier basis (from LDA with SOC)
with Wien2K and wannier90



$\Gamma_6(2)$	$\Gamma_7(2)$	$\Gamma_8(4)$	$\Gamma'_7(2)$	$\Gamma'_8(4)$
0.4881	0	0	0	0
0.4881	0	0	0	0
	0.5218	0	0.0994	0
	0.5218	0	0	-0.0994
		0.5846	0	-0.0714
		0.5846	0	0.0714
		0.5846	0	0
		0.5846	0	0.0714
			0.2102	0
			0.2102	0
				0.2033
				0.2033
				0.2033
				0.2033

$\Delta\xi_{\text{soc}} \sim 300 \text{ meV}$

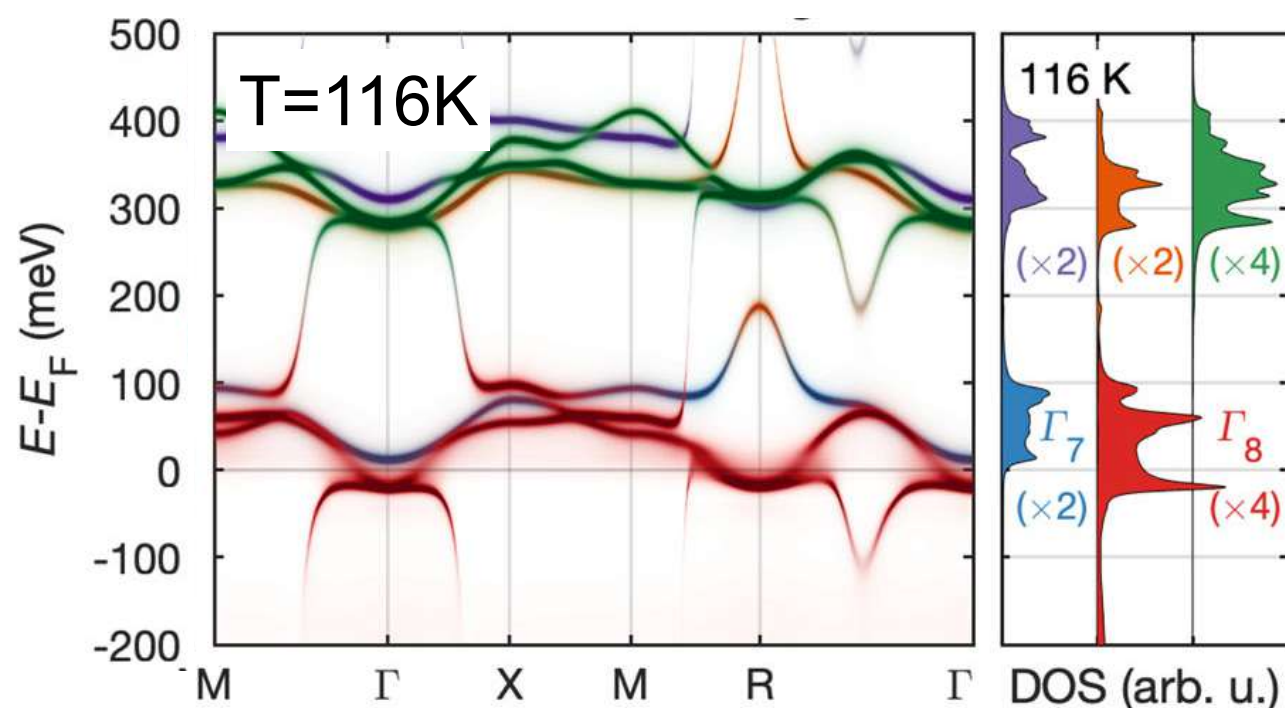
$H_{\text{loc}@ \text{Ce site}} =$

$J = \frac{7}{2}$

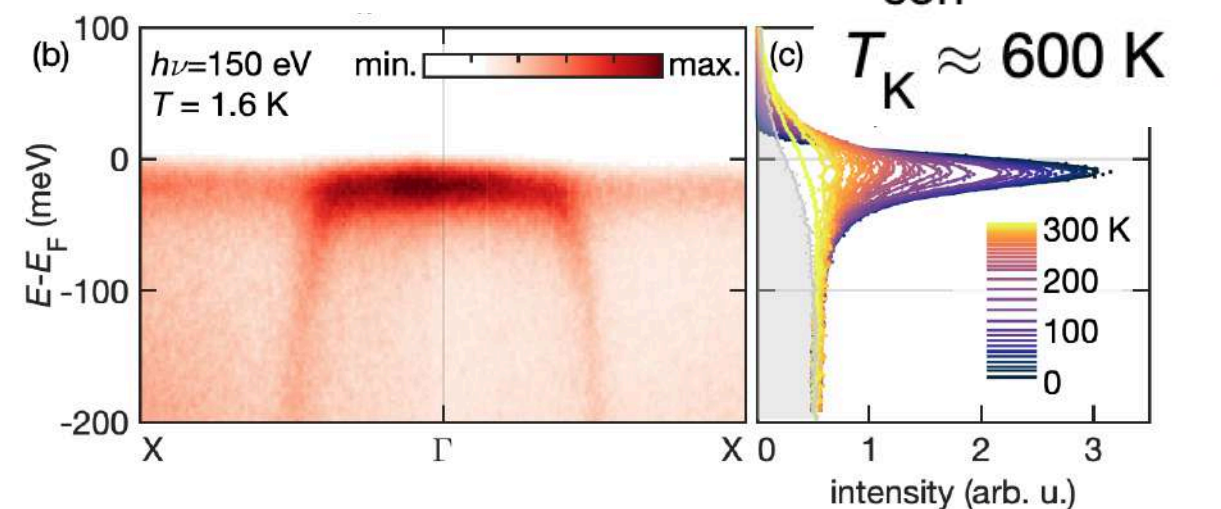
$J = \frac{5}{2}$

DFT+DMFT calc.

Below T_{coh}



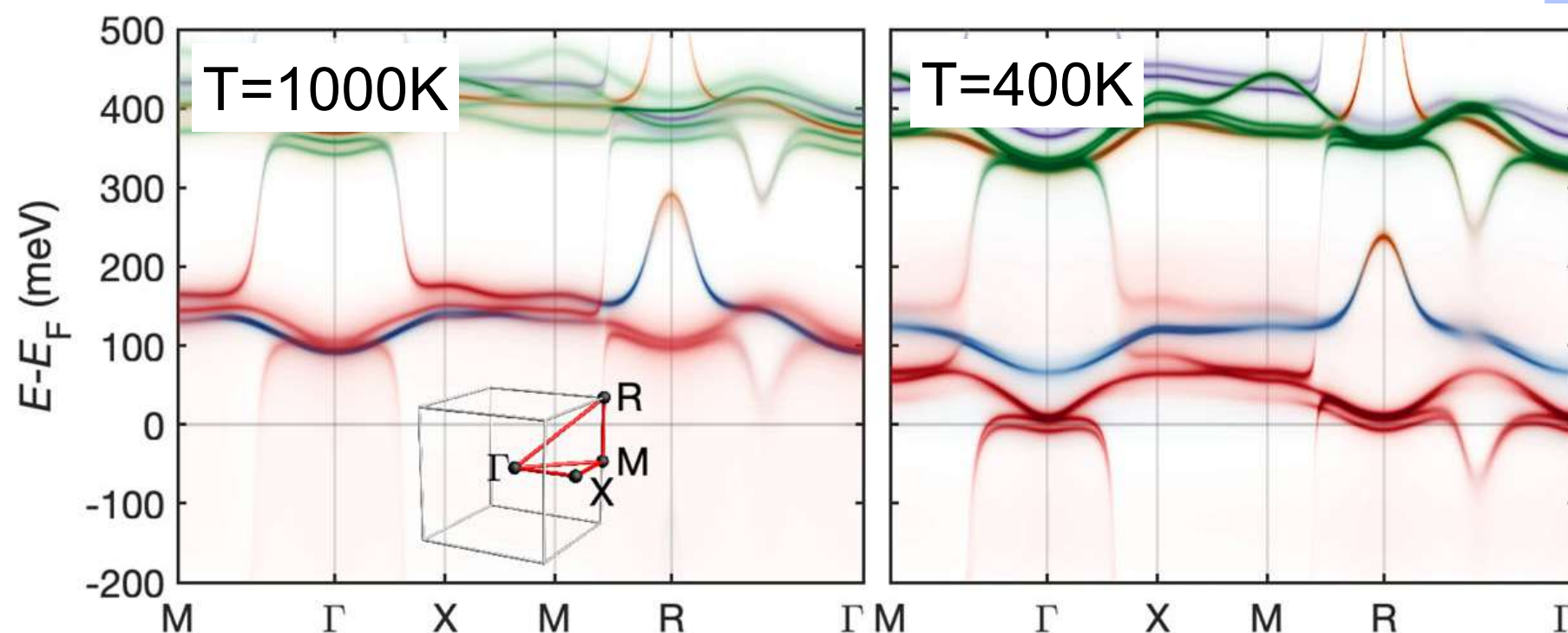
Exp. ARPES @ Γ point



- Sharp Kondo resonance near E_F
- Blind to spectral change above E_F with Kondo crossover

Above T_K

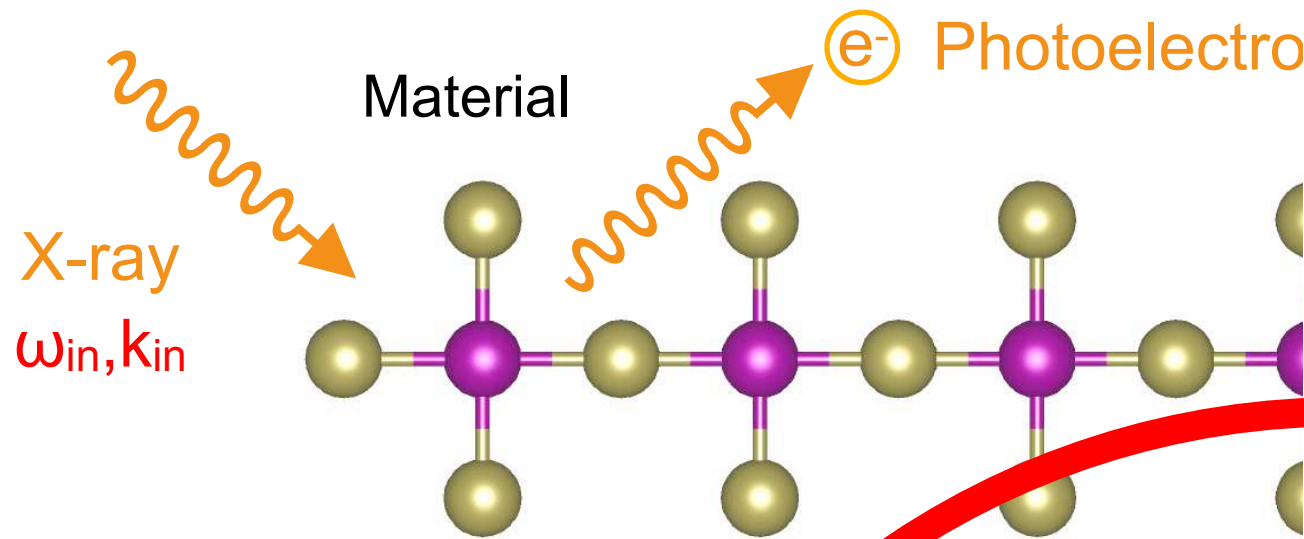
Above T_{coh}



Core-level x-ray spectroscopies

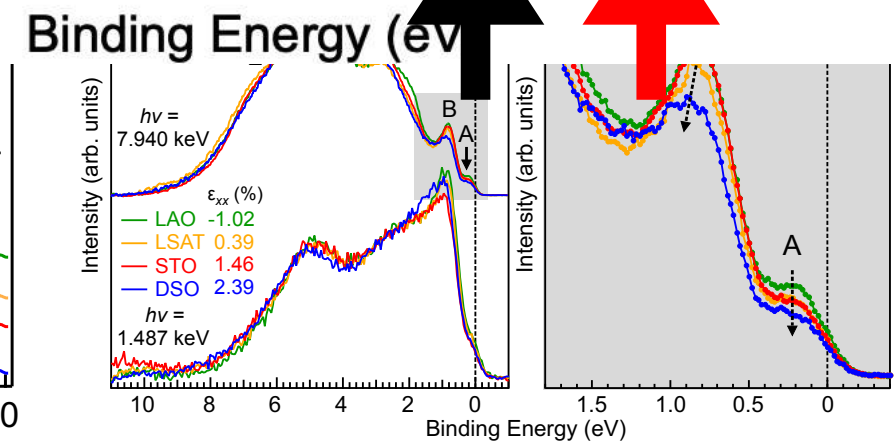
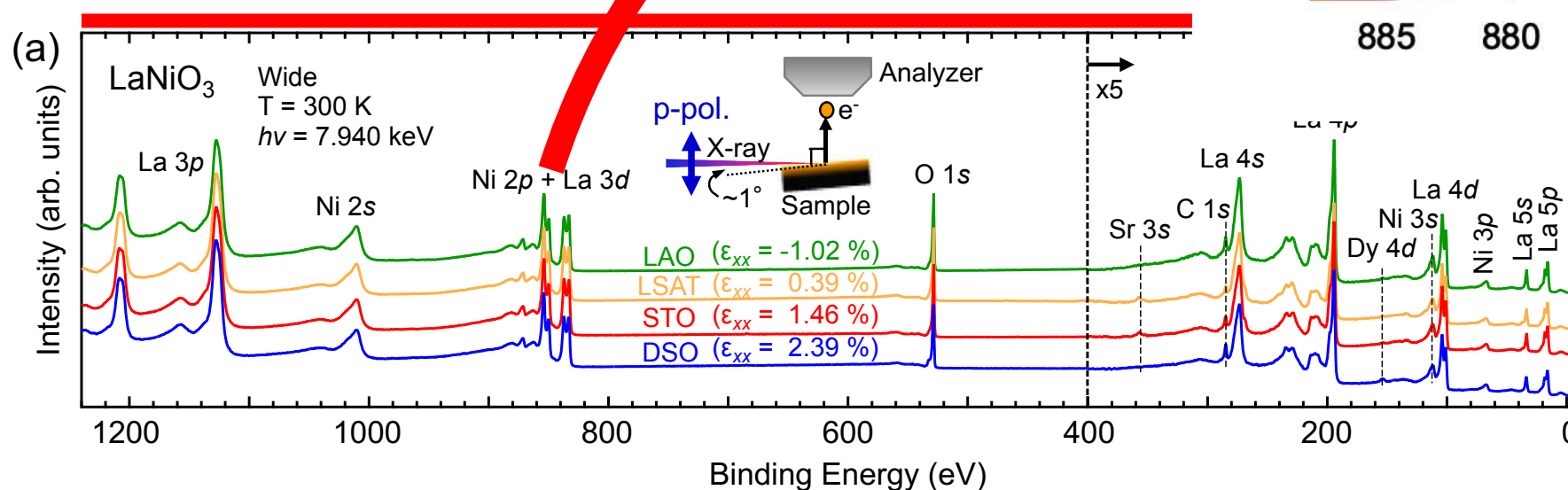
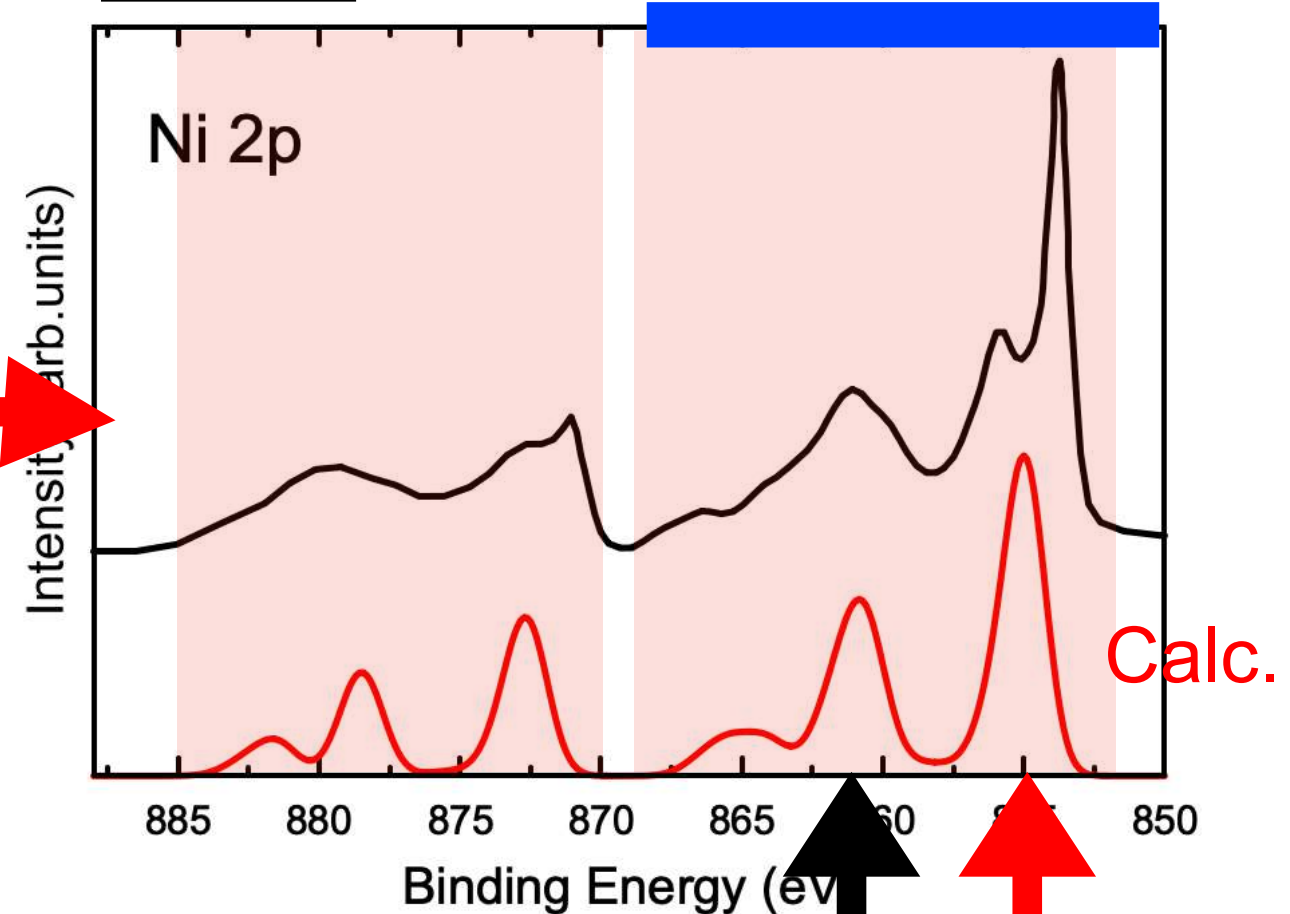
NiO

Many peaks ??



XPS spectrum in LaNiO₃ K. Yamamoto et al., Appl. Phys. Lett. 118, 1

Core levels



Core levels (no momentum dependence)

Core electrons (holes) completely localized at each ion

- Element specific information (valency)
- Local electronic structure (Hund's multiplet, crystal field, and more ...)

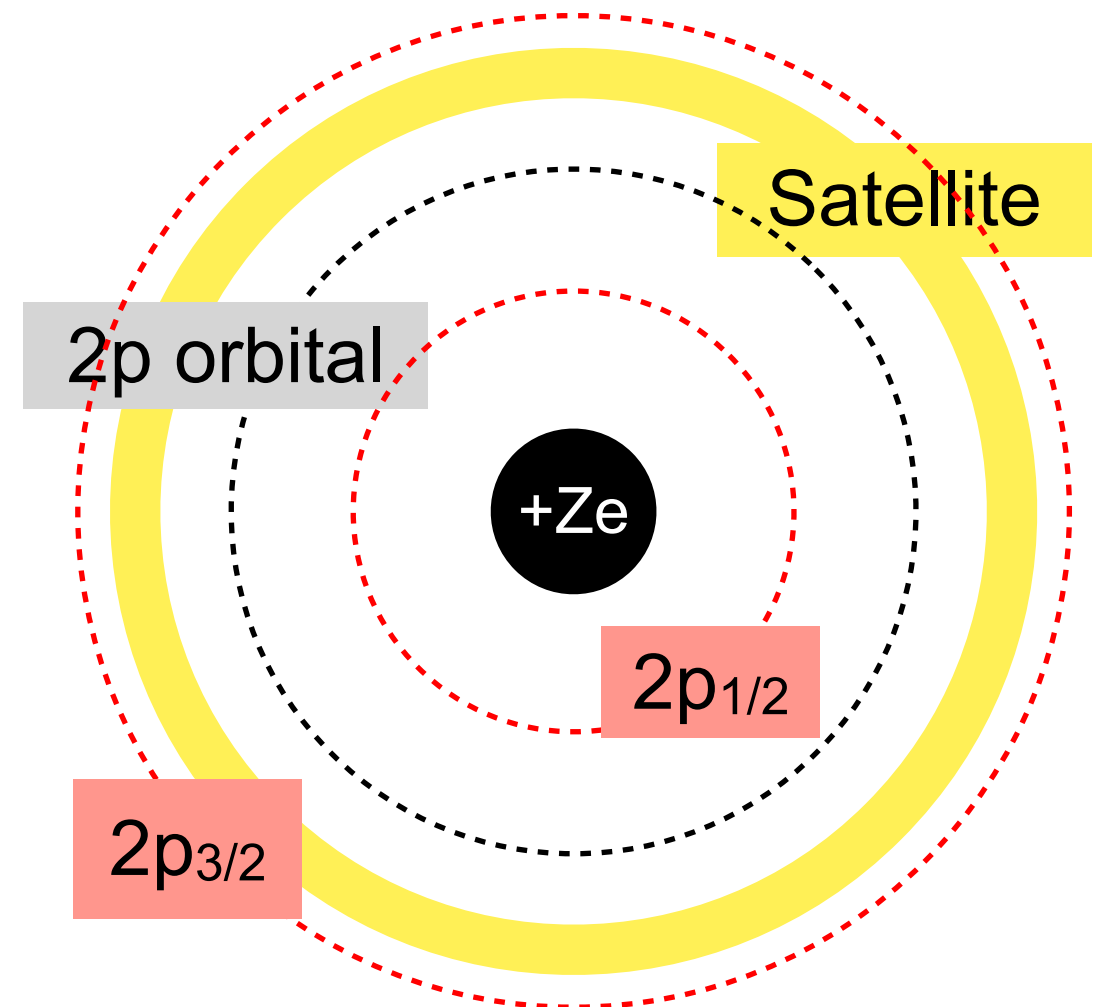
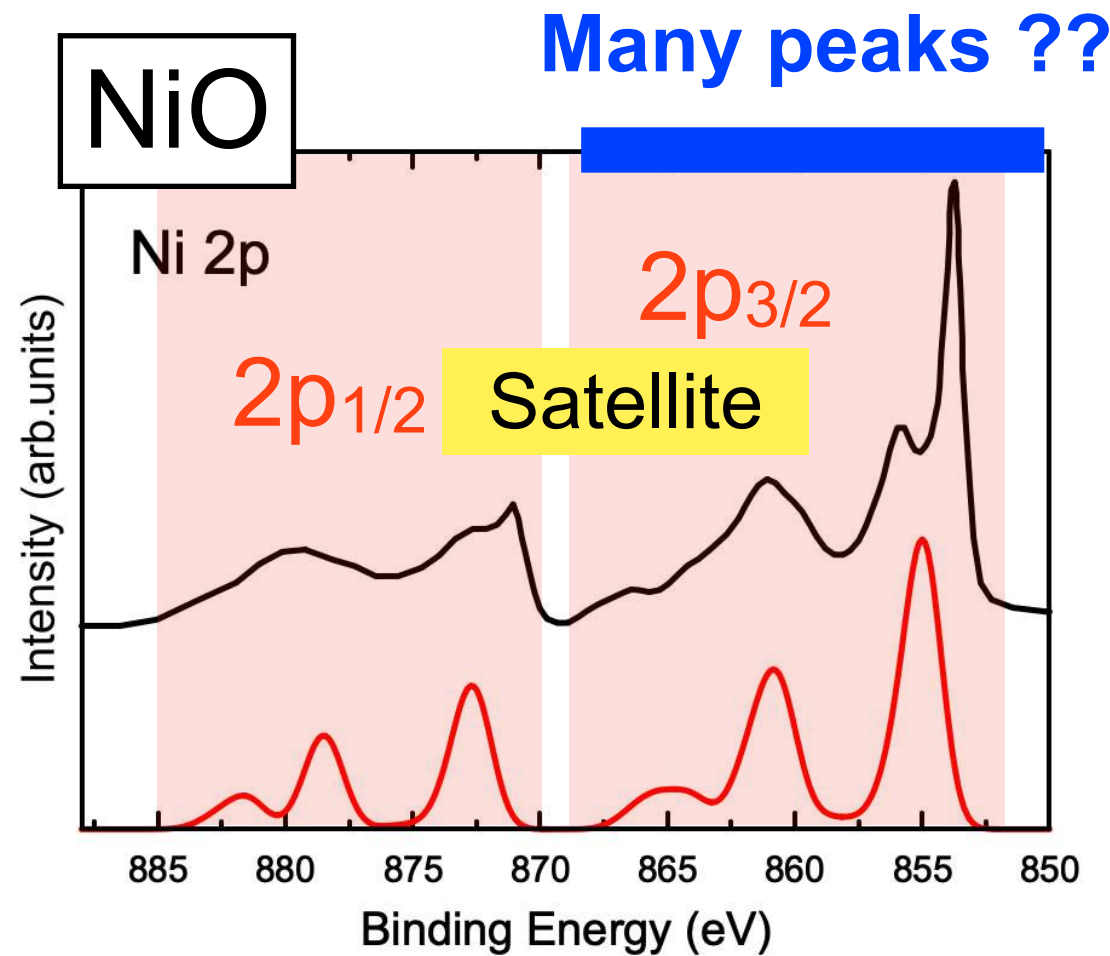
1-particle

Green's function $G_r(\epsilon) = \langle \Phi_0^{(N)} | c_r^\dagger \frac{1}{\epsilon - (E_0^{(N)} - \mathcal{H}) + i\delta} c_r | \Phi_0^{(N)} \rangle$

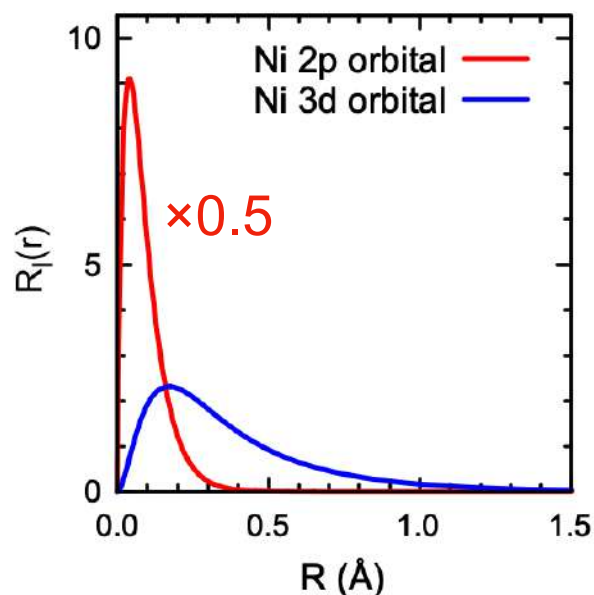
photoemission

$$= \sum_n \left[\frac{|\langle \Phi_n^{(N-1)} | c_r | \Phi_0^{(N)} \rangle|^2}{\epsilon - (E_0^{(N)} - E_n^{(N-1)}) + i\delta} \right]$$

Core-level x-ray spectroscopies



Atomic radial function
(from atomic Hartree-Fock calc.)



Spin orbit coupling

$$H_{\text{soc}}^{\text{atom}} = \xi \mathbf{L} \cdot \mathbf{S}$$

$$\xi_{\text{Ni } 2p} = 11.5 \text{ eV}$$

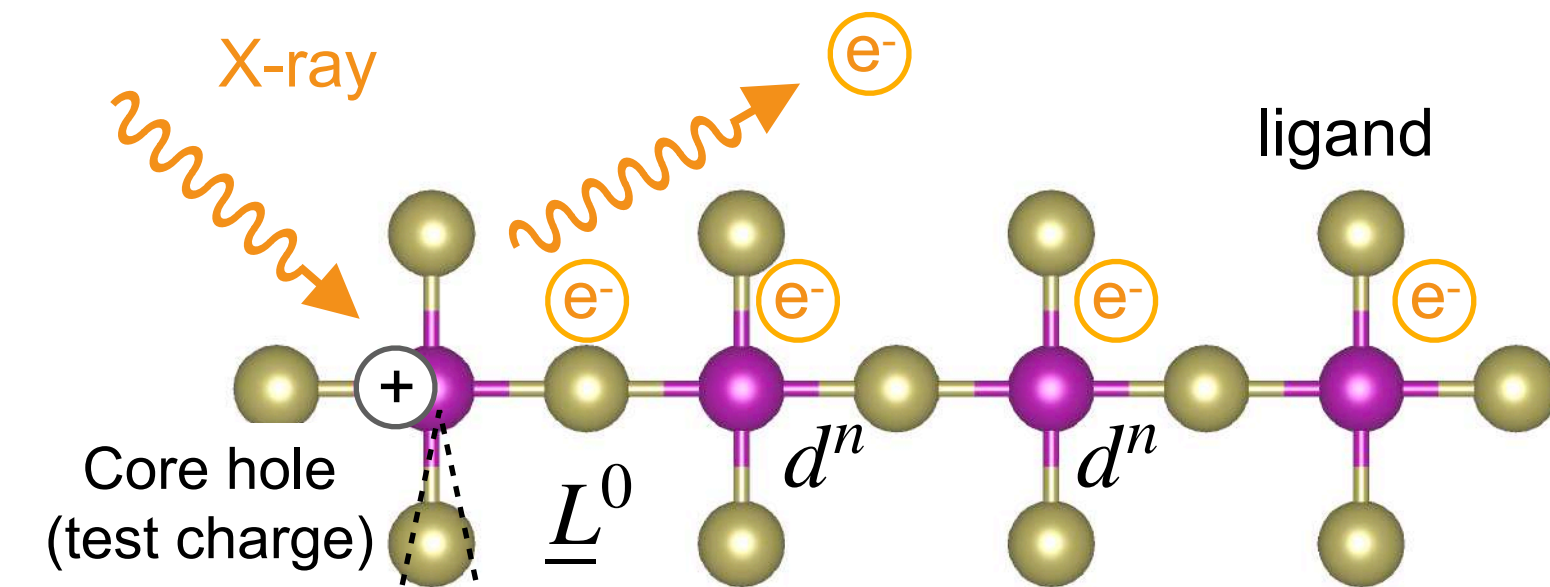
$$\xi_{\text{Ni } 3d} = 0.08 \text{ eV}$$

The origin of the satellite?

A. Many-body final-state effect
due to interaction between core-
hole and valence electrons

Core-level x-ray spectroscopies

Hubbard model with ligands included (dp model)

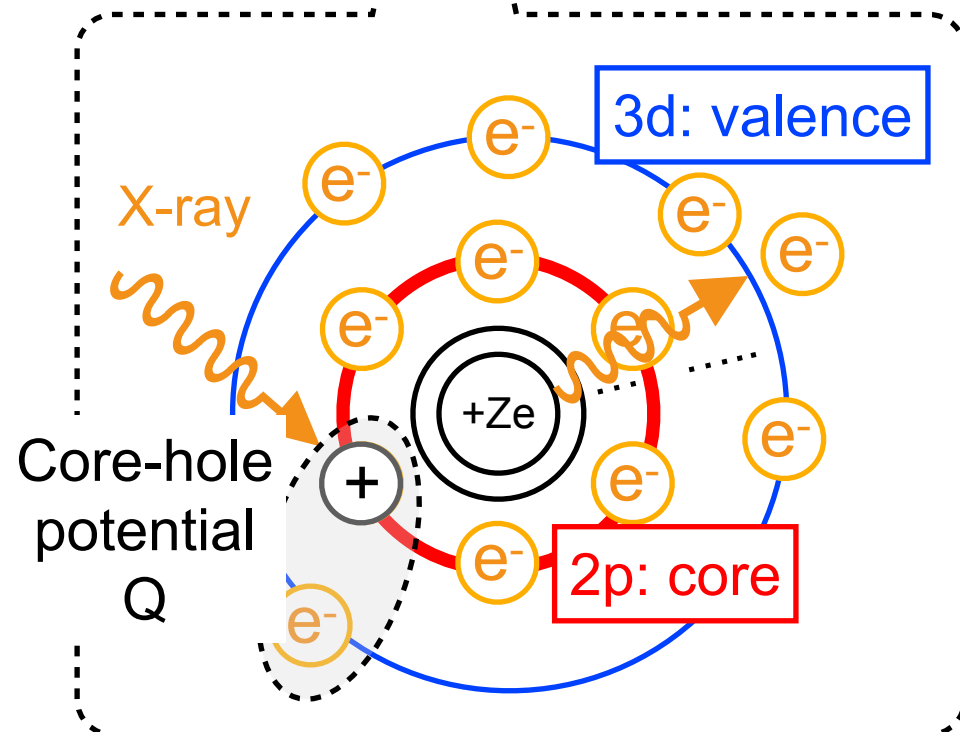


$$H_{\text{Hubbard}} = \sum_i U n_{i\uparrow} n_{i\downarrow}$$

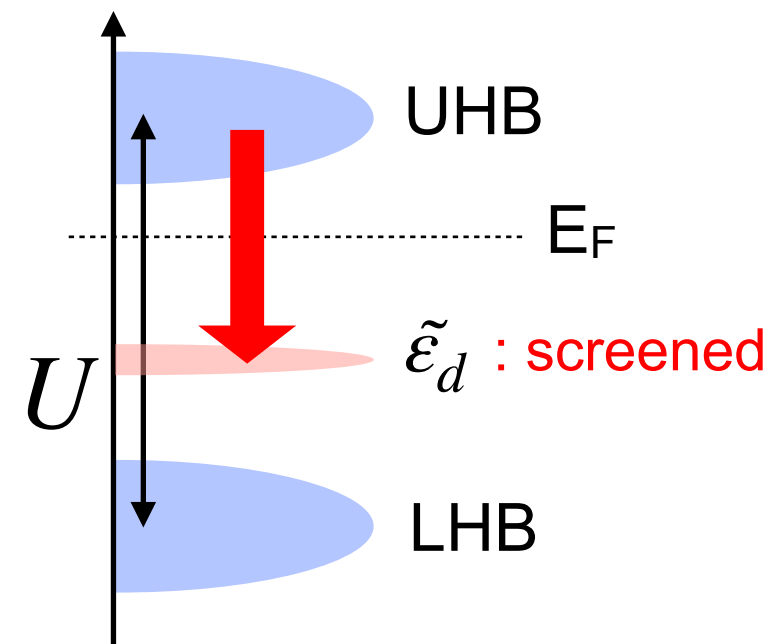
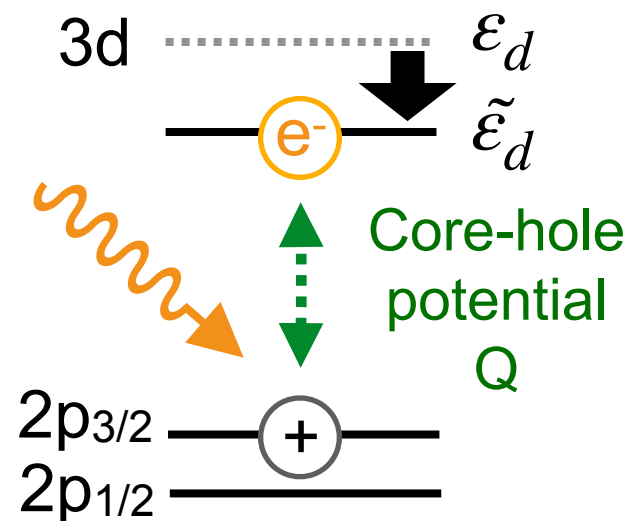
: Core-hole potential

$$+ Q \sum_i N_i (6 - N_c)$$

N_c : Number of electrons in 2p core levels



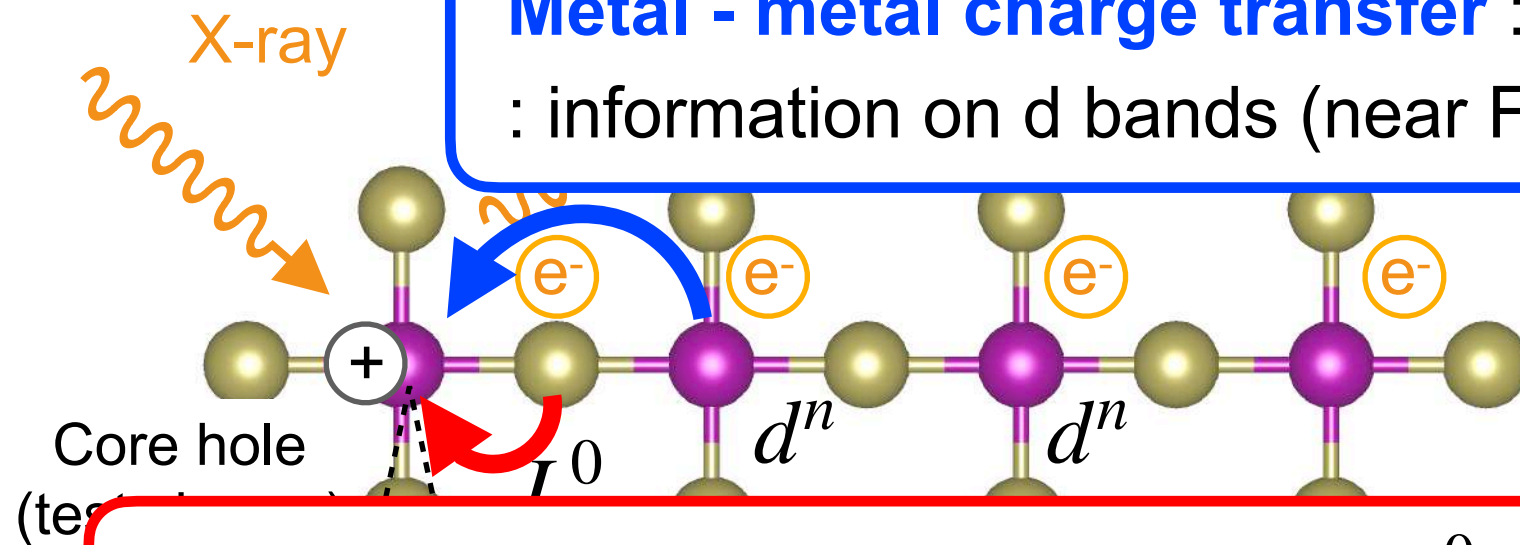
Energy



Core-level x-ray spectroscopies

Hubbard model with ligands included (dp model)

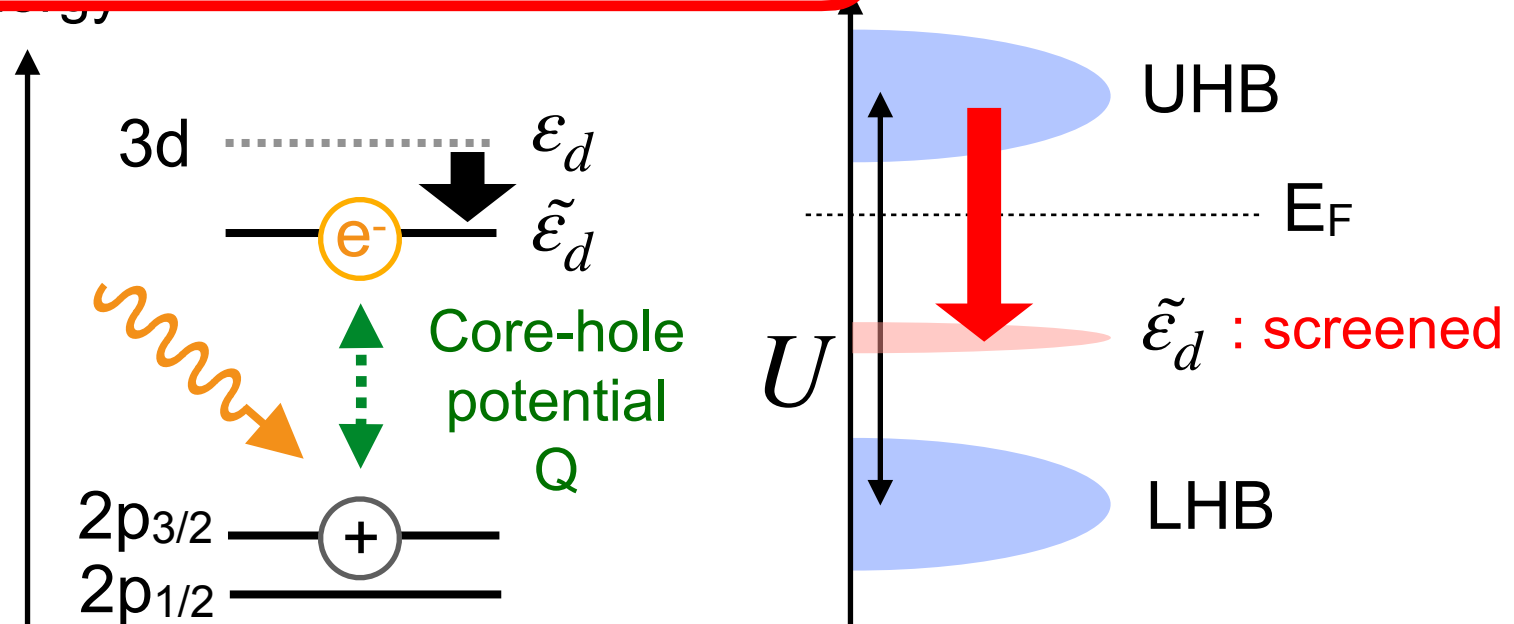
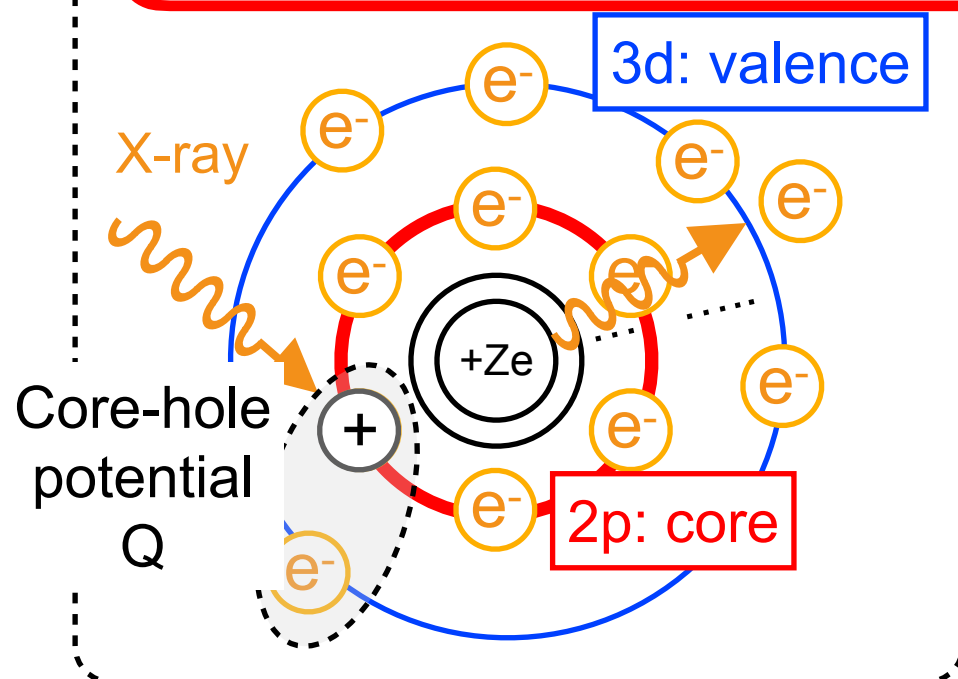
Metal - metal charge transfer : $d^n + d^n \rightarrow d^{n+1} + d^{n-1}$
: information on d bands (near Fermi energy)



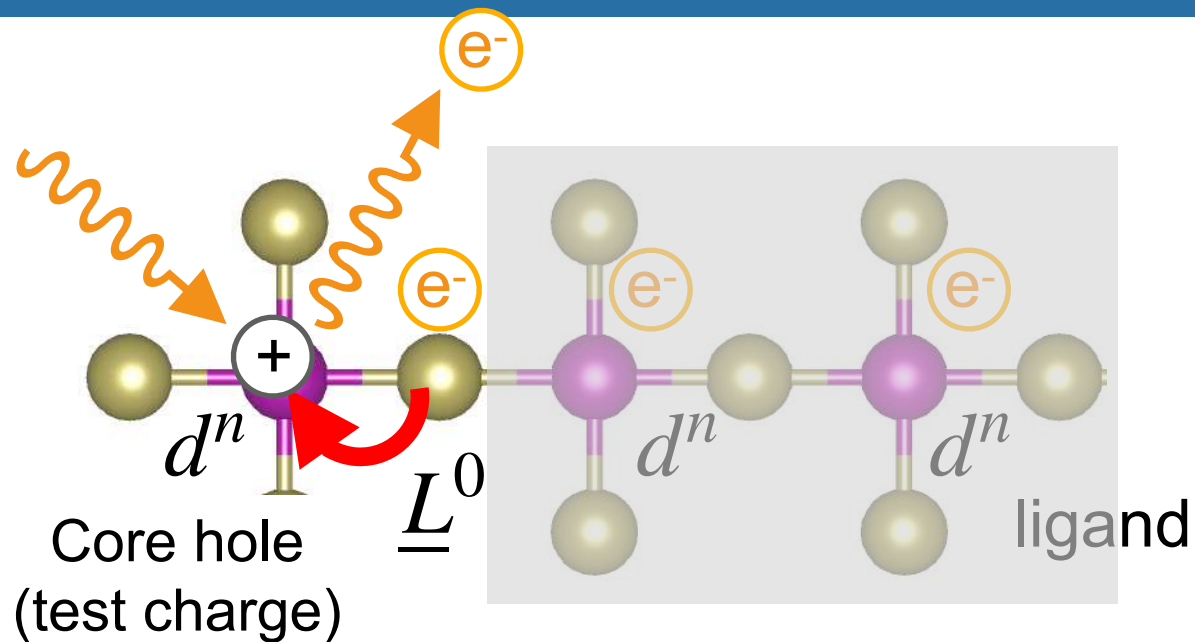
: Core-hole potential
 $+Q \sum_i N_i(6 - N_c)$

N_i : Number of electrons
 in 2p core levels

Metal - ligand charge transfer : $d^n + \underline{L}^0 \rightarrow d^{n+1} + \underline{L}^1$
: information on Δ_{CT} , hybridization with ligands



Core-level x-ray spectroscopies



Fermi golden rule

X-ray transition (dipole)

$$F(E_B) = \sum_f |\langle f | \bar{T} | g \rangle|^2 \delta(E_B - E_f - E_g)$$

$$E_B = \omega - \varepsilon - \phi,$$

ε : Kinetic energy of PE

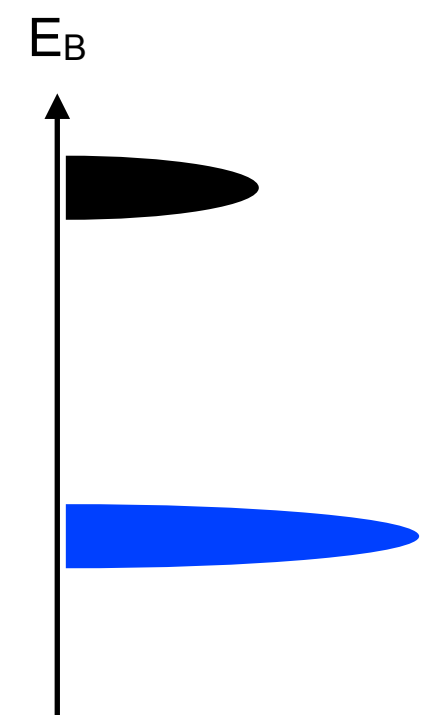
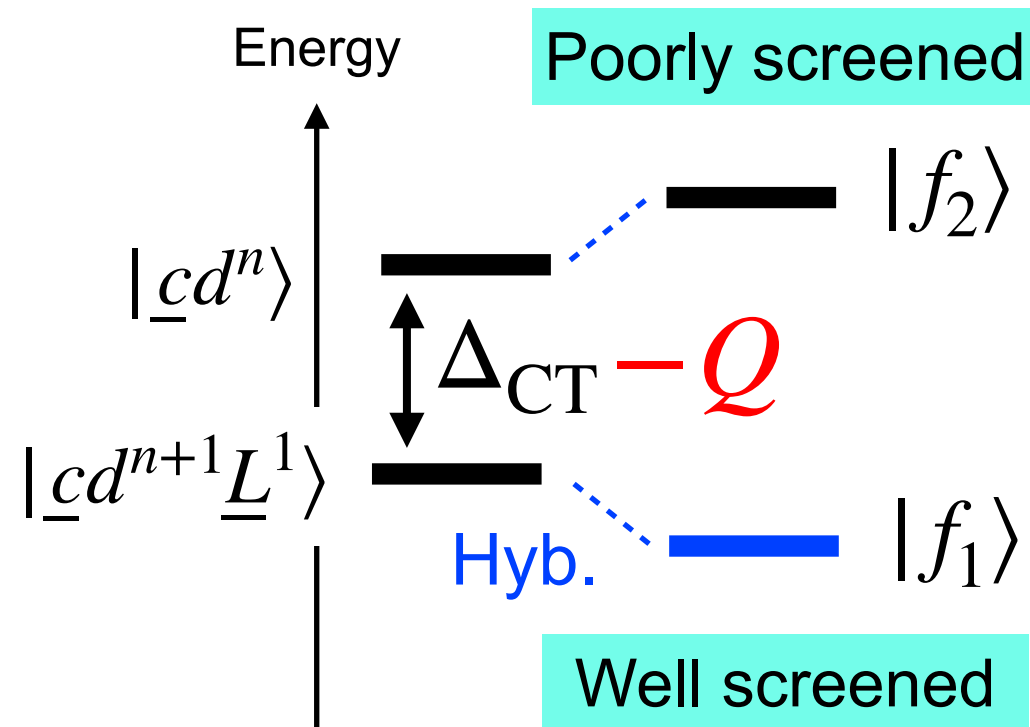
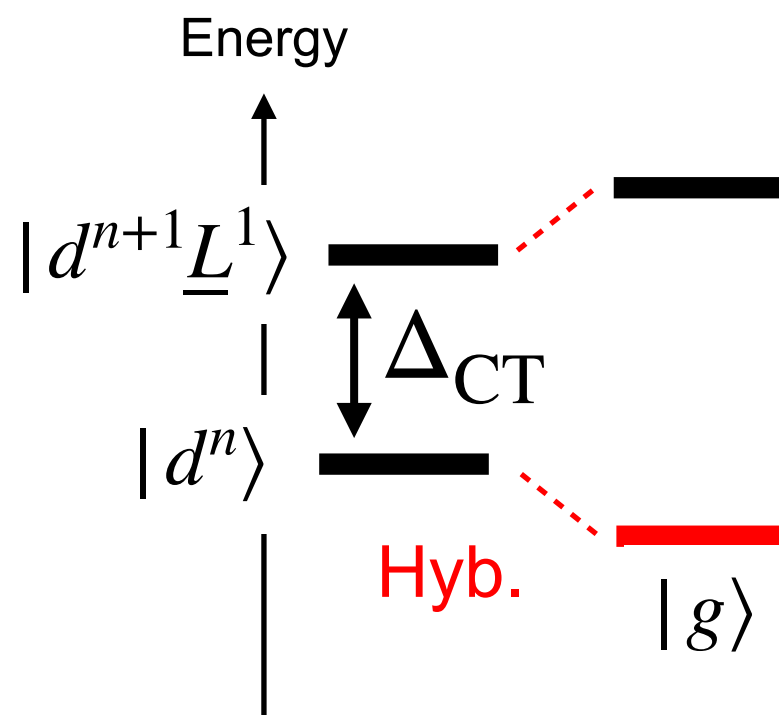
ω : Photon energy

Initial state:

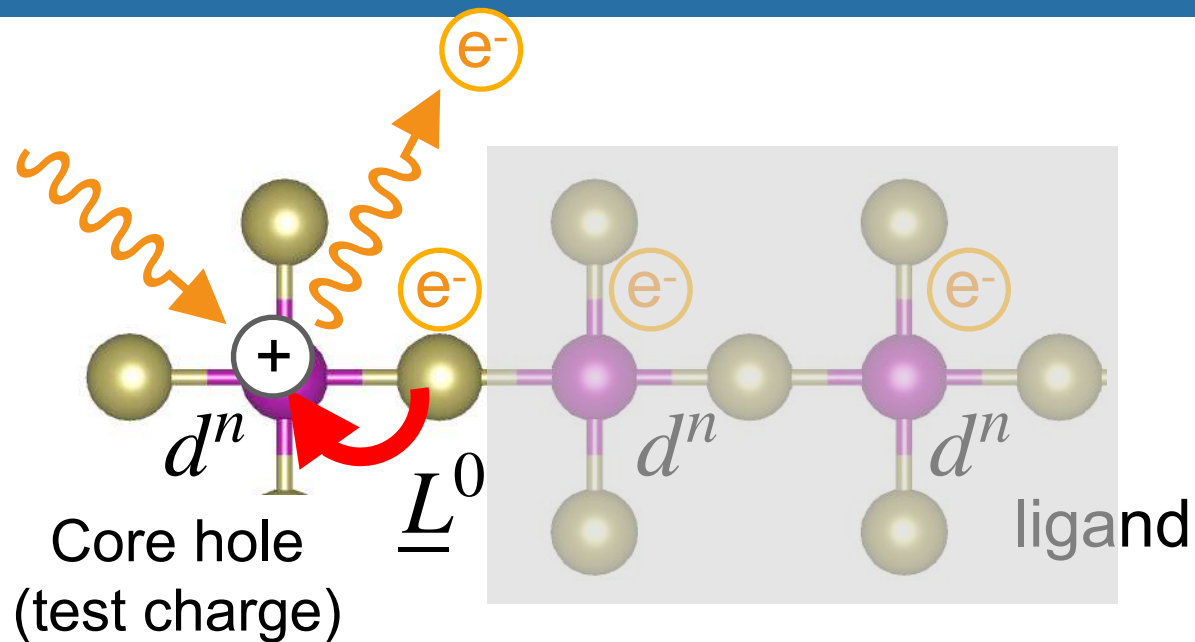
$$|g\rangle = |d^n\rangle + |d^{n+1}\underline{L}\rangle + \dots$$

Final state (with a core-hole):

$$|f\rangle = |\underline{c}d^n\rangle + |\underline{c}d^{n+1}\underline{L}\rangle + \dots$$

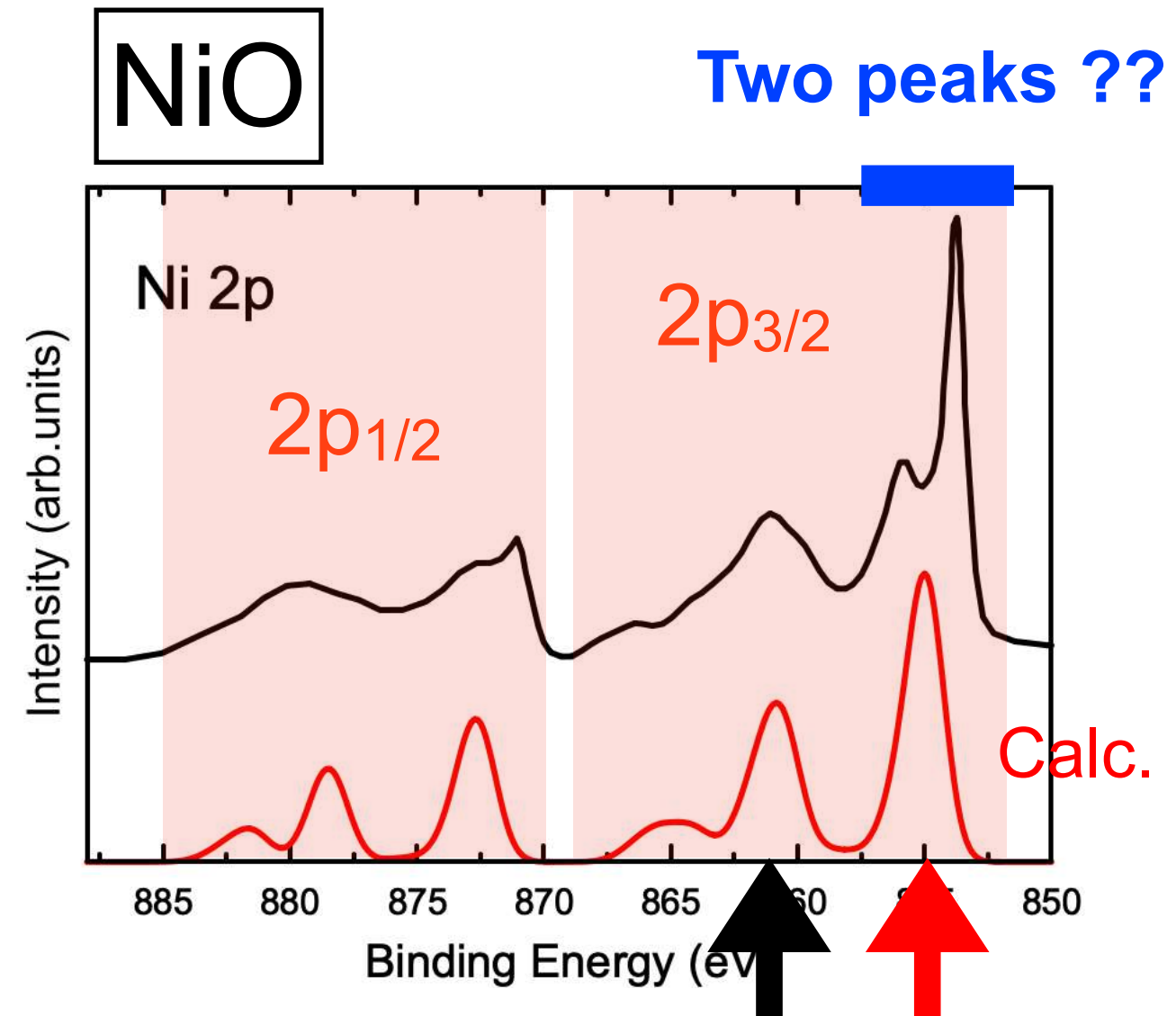
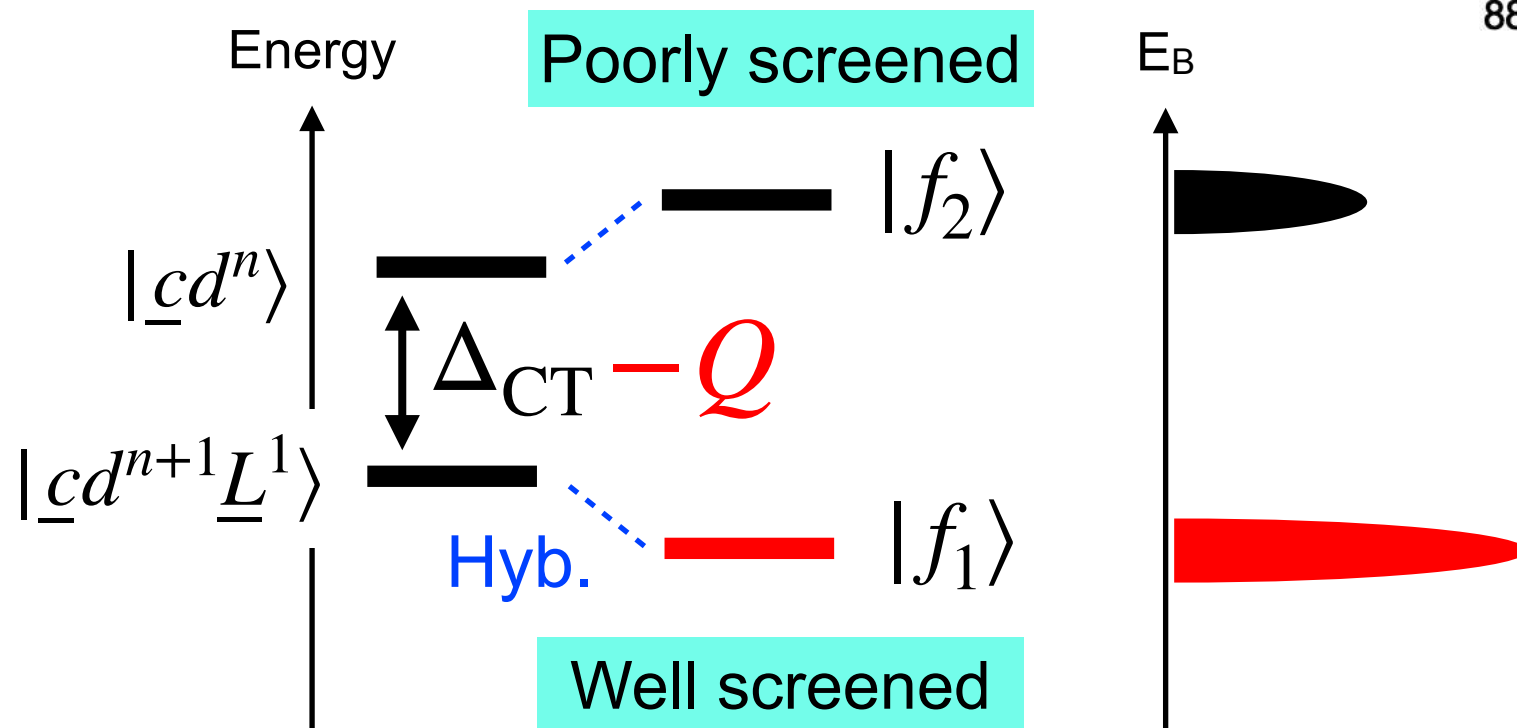


Core-level x-ray spectroscopies

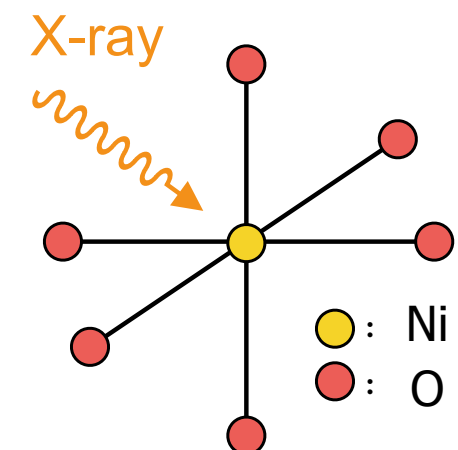


Final state (with a core-hole):

$$|f\rangle = |\underline{c}d^n\rangle + |\underline{c}d^{n+1}\underline{L}\rangle + \dots$$

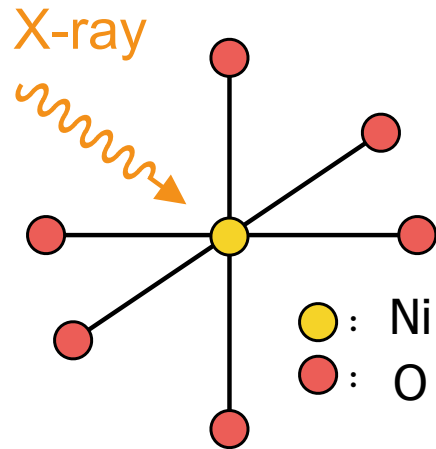


MO₆ cluster model (since 1980's)



Multiplet ligand-field calculation (Cluster model)

MO₆ cluster model (since 1980's)



- ✓ All local interactions explicitly (incl. core orbitals at the excited site)
- ✗ Only nearest-neighboring ligands (no translational symmetry)
- ✗ Many adjustable parameters (fitted to reproduce the experimental data)

Cluster model from DFT

PHYSICAL REVIEW B **85**, 165113 (2012)



Multiplet ligand-field theory using Wannier orbitals

M. W. Haverkort,¹ M. Zwierzycki,² and O. K. Andersen¹

¹Max Planck Institute for Solid State Research, Heisenbergstraße 1, 70569 Stuttgart, Germany

²Institute of Molecular Physics, Polish Academy of Sciences, M. Smoluchowskiego 17, 60-179 Poznań, Poland

(Received 21 November 2011; revised manuscript received 7 March 2012; published 9 April 2012)

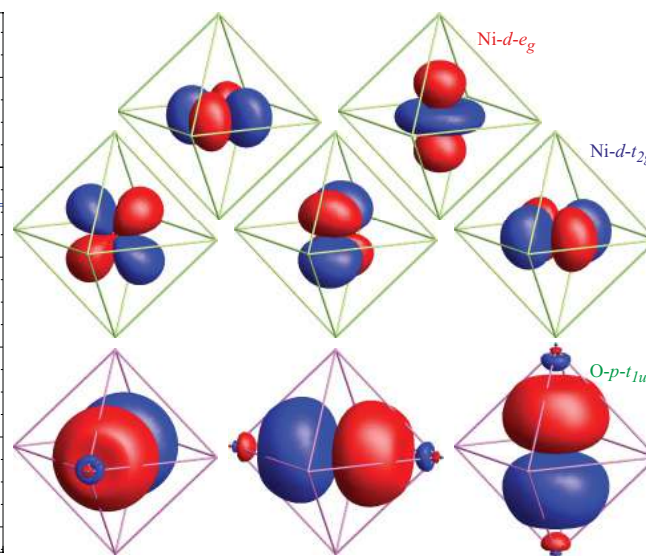
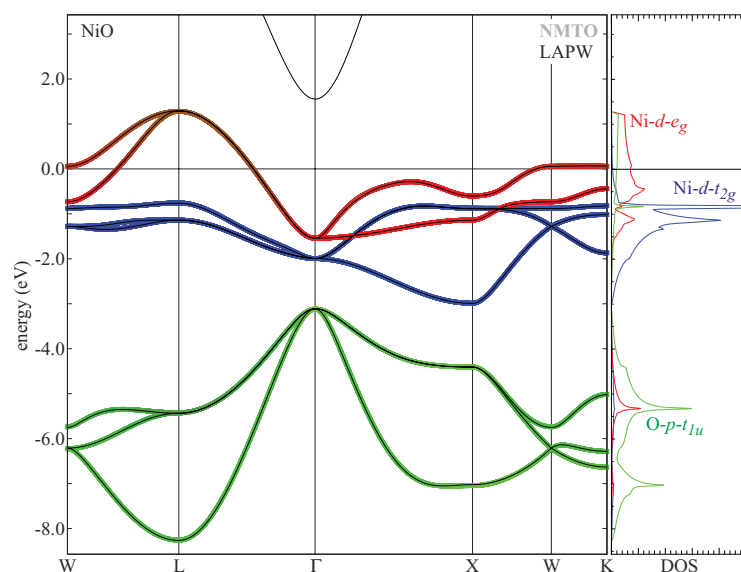
✓ Eliminate (most of) adjustable parameters

	V_{eg}	V_{t2g}	$10Dq$	T_{pp}	ζ_{3d}	$F_{dd}^{(2)}$	$F_{dd}^{(4)}$	ζ_{2p}	$F_{2p3d}^{(2)}$	$G_{2p3d}^{(1)}$	$G_{2p3d}^{(3)}$	ζ_{3p}	$F_{3p3d}^{(2)}$	$G_{3p3d}^{(1)}$	$G_{3p3d}^{(3)}$
NiO	2.06	1.21	0.56	0.72	0.08	11.14	6.87	11.51	6.67	4.92	2.80	1.40	12.87	15.89	9.58
MnO	1.92	1.15	0.67	0.53	0.04	9.35	5.78	6.85	5.29	3.77	2.14	0.77	10.93	13.56	8.15
SrTiO ₃	4.03	2.35	1.79	0.99	0.02	8.38	5.25	3.78	4.23	2.81	1.59	0.43	9.85	12.08	7.35

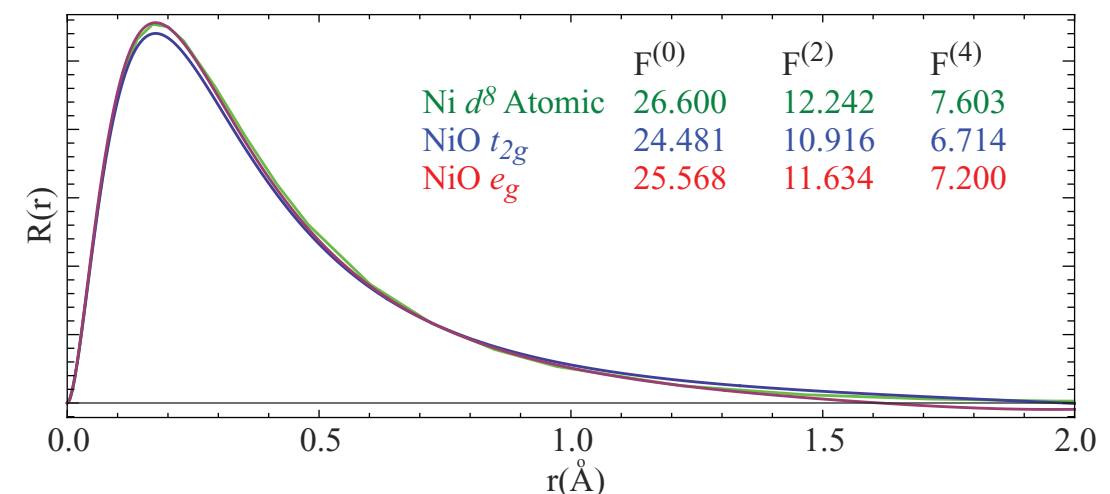
	[001]			
	$d_{z^2}p_z$	$d_{xz}p_x$		$d_{z^2}p_z$
NiO	1.19	-0.60		0.00
MnO	1.11	-0.57		0.02
SrTiO ₃	2.33	-1.18		—

Coulomb integrals
(valence-valence, core-valence)

	p_zp_z	p_xp_x	p_zp_x	p_xp_y	$p_y p_y$	$d_{z^2}d_{z^2}$	$d_{xz}d_{xz}$	$d_{xy}p_x$	$d_{yz}p_z$	$d_{z^2}p_y$	$d_{z^2}p_z$	$d_{xz}p_x$	$d_{xz}p_y$	$d_{xy}p_x$	ϵ_p	ϵ_d
NiO	0.02	-0.04	—	—	—	-0.01	-0.03	0.00	0.02	-0.03	0.00	0.00	0.00	0.00	-4.75	-1.35
MnO	0.05	-0.03	—	—	—	-0.06	-0.05	0.00	0.02	-0.03	-0.01	0.00	0.00	0.00	-5.22	-0.39
SrTiO ₃	-0.01	-0.11	0.06	-0.02	-0.02	0.05	-0.13	-0.02	0.05	-0.03	0.00	-0.02	-0.01	-0.02	-1.53	3.31



Localized wannier orbitals as basis functions



Local interaction: Coulomb interaction (valence-valence)

Coulomb interaction between 3d electrons

$$H_{3d-3d} = \sum_{k=2,4} F^k(3d,3d) \sum_{\omega_1 < \omega_2, \omega_3 < \omega_4} \left[\underbrace{f^k(d\omega_1 d\omega_2, d\omega_3 d\omega_4)}_{\text{direct}} - \underbrace{f^k(d\omega_1 d\omega_2, d\omega_4 d\omega_3)}_{\text{exchange}} \right] (d\omega_1)^\dagger (d\omega_2)^\dagger (d\omega_4) (d\omega_3)$$

F^0 omitted (monopole part)

here, $\omega = (m_l, m_s)$

F^k is Slater integral : $\underline{F^k(3d, 3d)} = e^2 \int_0^{+\infty} r_1^2 r_2^2 dr_1 dr_2 R_{3d}^2(r_1) R_{3d}^2(r_2) \frac{r_{<}^k}{r_{>}^{k+1}}$

(orbital, and spin magnetic quantum number)

: F^0, F^2, F^4 allowed for 3d-3d interactions

$$U = F_0 \quad : \text{Hubbard parameter}$$

$$J = \frac{F_2 + F_4}{14} \quad : \text{Hund's parameter}$$

Calculated from atomic Hartree Fock method,
constrained random phase approximation etc
: in reality, screening must be taken into account

Angular part of the integral:

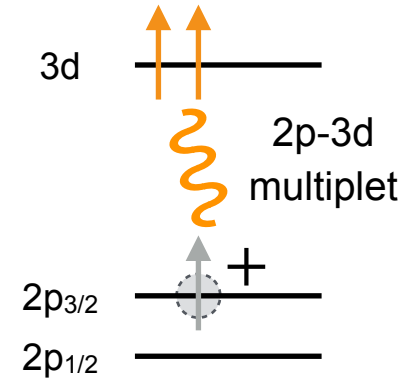
$$f^k(\omega_1 \omega_2, \omega_3 \omega_4) = \delta_{m_{s1}, m_{s3}} \delta_{m_{s2}, m_{s4}} \sum_q (-)^q \underbrace{\langle l_1 m_{l1} | C_q^k | l_3 m_{l3} \rangle \langle l_2 m_{l2} | C_{-q}^k | l_4 m_{l4} \rangle}_{\text{angular part}}$$

Calculated by CG coefficients (3j symbols) : $\langle lm | C_q^k | l'm' \rangle = (-)^m \sqrt{(2l+1)(2l'+1)} \begin{pmatrix} l & k & l' \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} l & k & l' \\ -m & q & m' \end{pmatrix}$

Local interaction: Coulomb interaction (core-valence)

Coulomb interaction between 2p (core) and 3d (valence) electrons

$$H_{2p-3d} = \sum_{\omega_1, \omega_2, \omega_3, \omega_4} \left[\underbrace{\left(p\omega_1 d\omega_2 \left| \frac{1}{r_{12}} \right| p\omega_3 d\omega_4 \right)}_{\text{direct}} - \underbrace{\left(p\omega_1 d\omega_2 \left| \frac{1}{r_{12}} \right| d\omega_4 p\omega_3 \right)}_{\text{exchange}} \right] (p\omega_1)^\dagger (p\omega_3) (d\omega_2)^\dagger (d\omega_4)$$



$$= F^2(2p, 3d) \sum_{\omega_1, \omega_2, \omega_3, \omega_4} f^2(p\omega_1 d\omega_2, p\omega_3 d\omega_4) (p\omega_1)^\dagger (p\omega_3) (d\omega_2)^\dagger (d\omega_4)$$

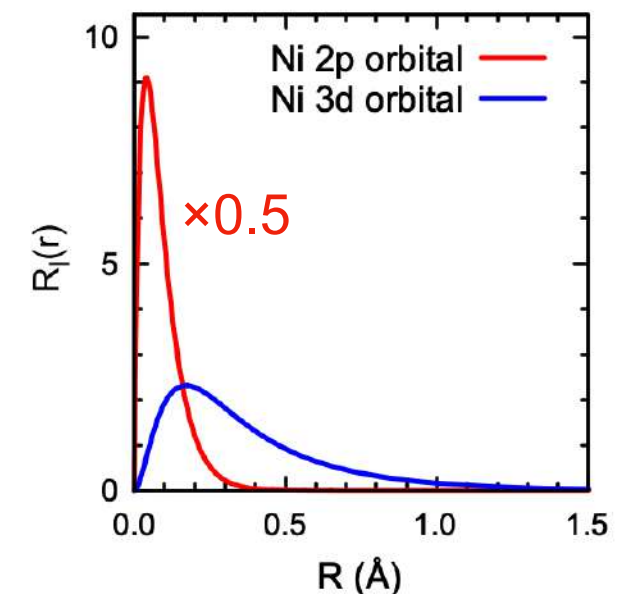
F^0 omitted
(monopole part)

: direct term

$$- \sum_{k=1,3} G^k(2p, 3d) \sum_{\omega_1, \omega_2, \omega_3, \omega_4} f^k(p\omega_1 d\omega_2, d\omega_4 p\omega_3) (p\omega_1)^\dagger (p\omega_3) (d\omega_2)^\dagger (d\omega_4)$$

: exchange term

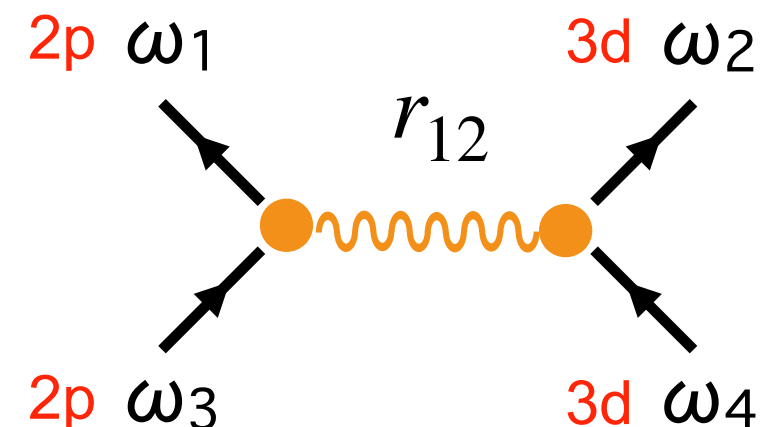
Atomic radial function
(from atomic Hartree-Fock calc.)



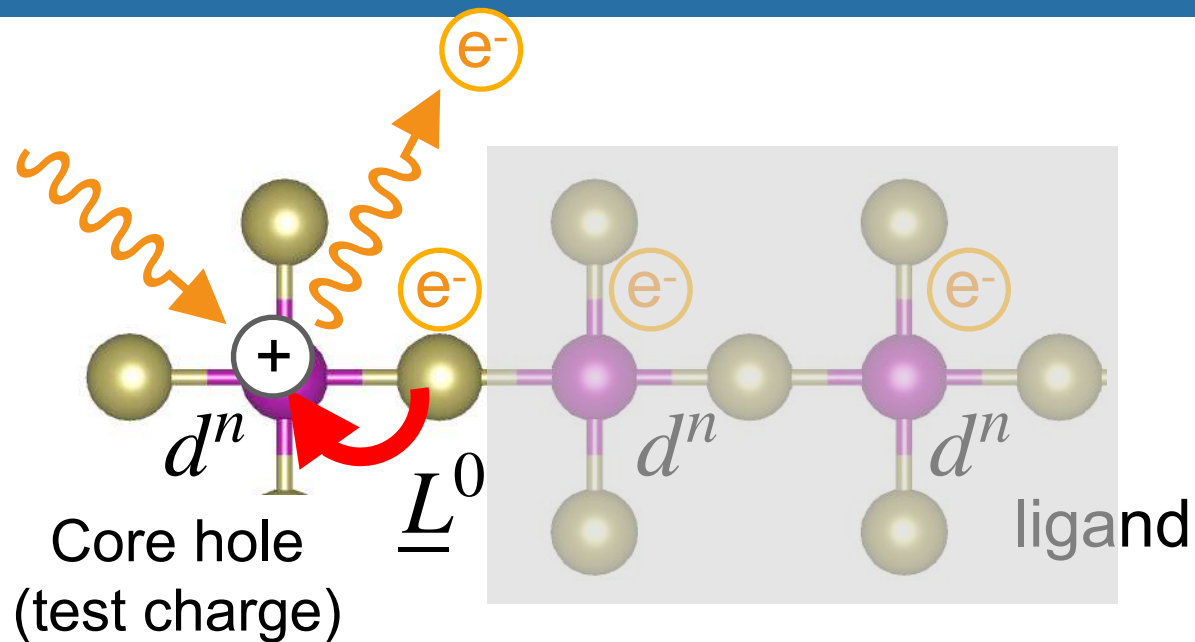
Slater
integral

$$F^k(2p, 3d) = \int_0^\infty \int_0^\infty R_{2p}^2(r_1) R_{3d}^2(r_2) \frac{r_{<}^k}{r_{>}^{k+1}} r_1^2 r_2^2 dr_1 dr_2$$

$$G^k(2p, 3d) = \int_0^\infty \int_0^\infty R_{2p}(r_1) R_{3d}(r_1) R_{2p}(r_2) R_{3d}(r_2) \frac{r_{<}^k}{r_{>}^{k+1}} r_1^2 r_2^2 dr_1 dr_2$$

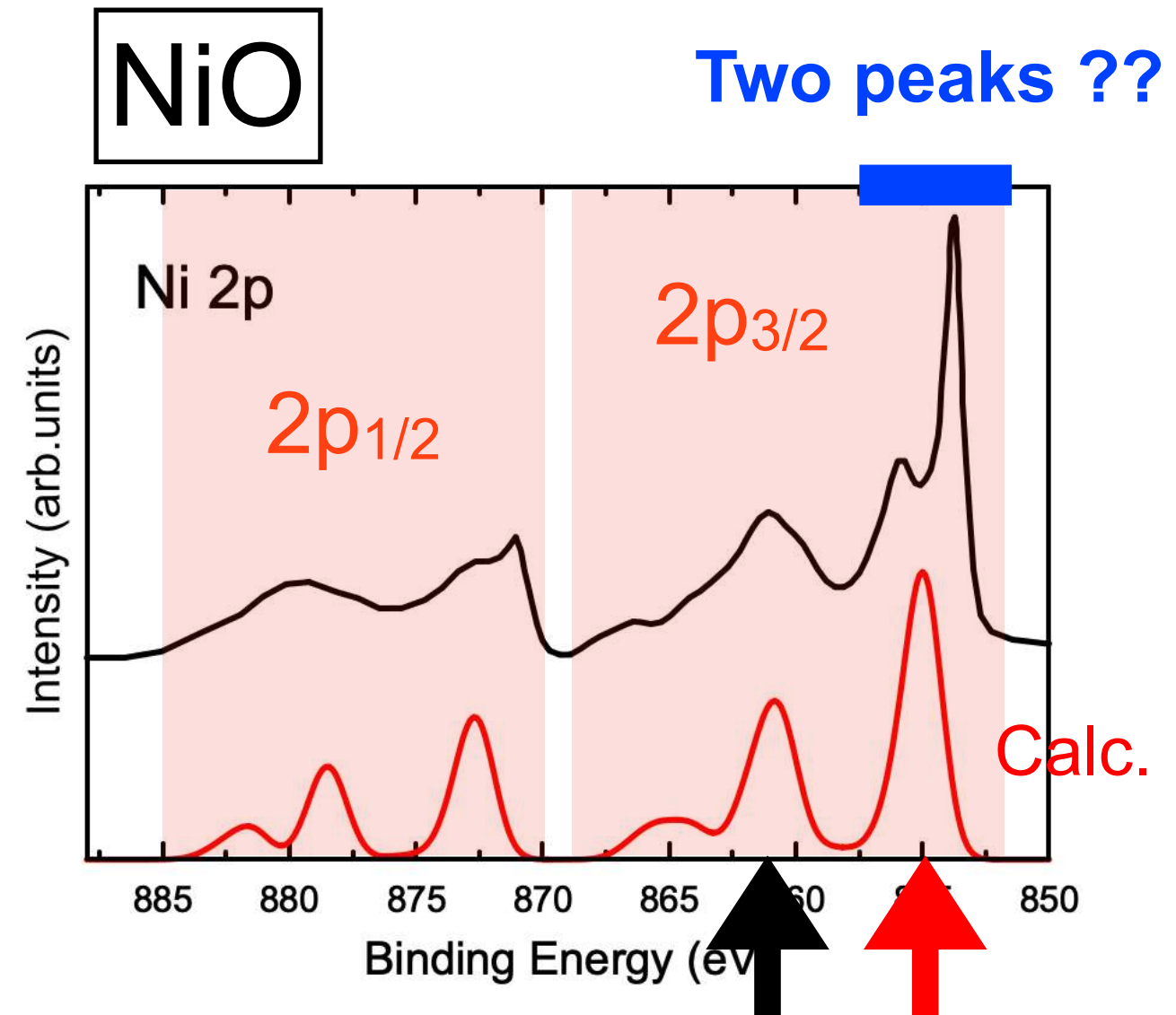
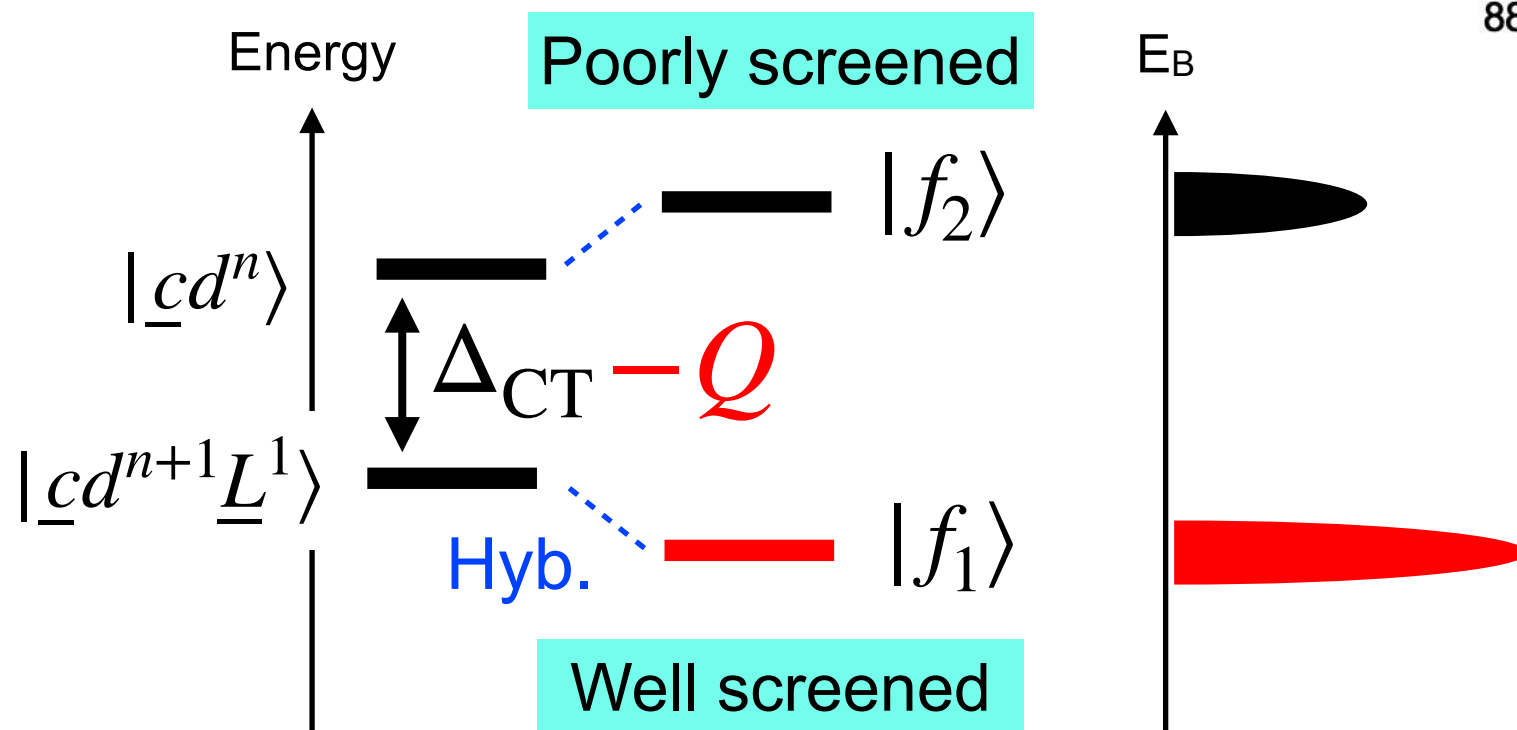


Core-level x-ray spectroscopies

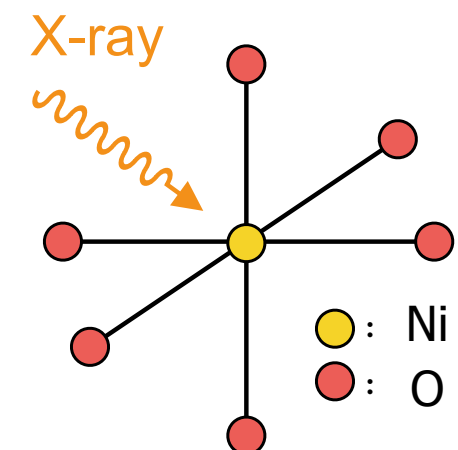


Final state (with a core-hole):

$$|f\rangle = |\underline{c}d^n\rangle + |\underline{c}d^{n+1}\underline{L}\rangle + \dots$$

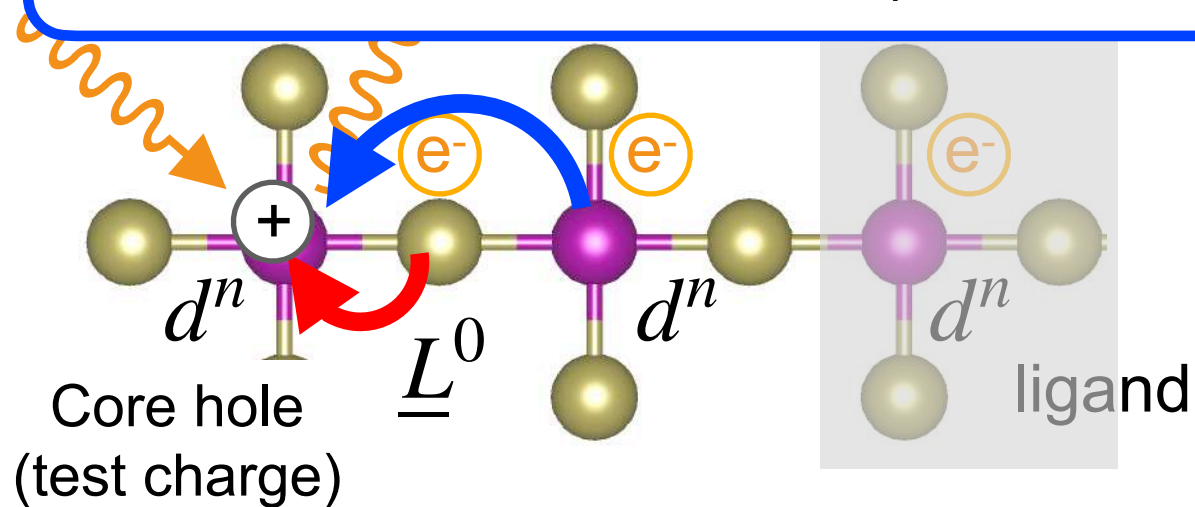


MO₆ cluster model (since 1980's)



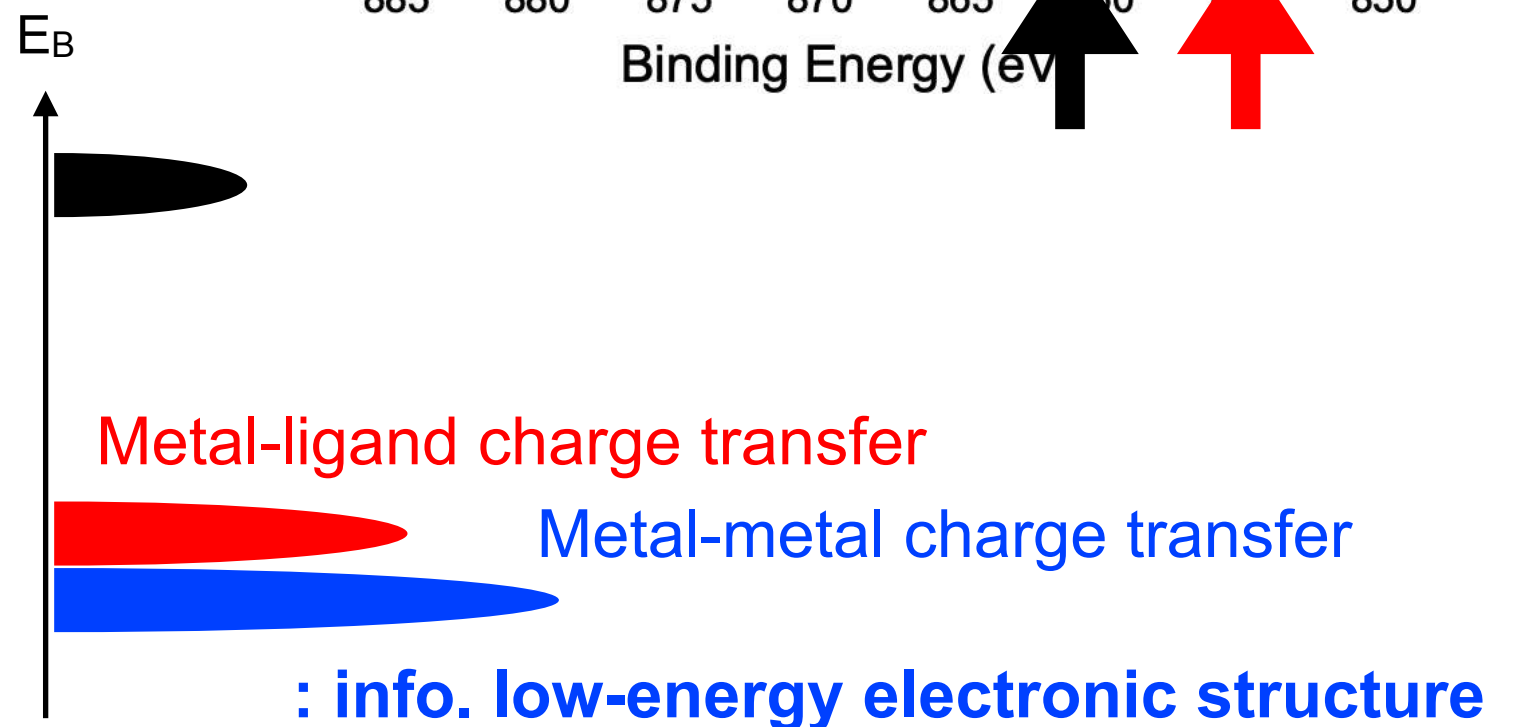
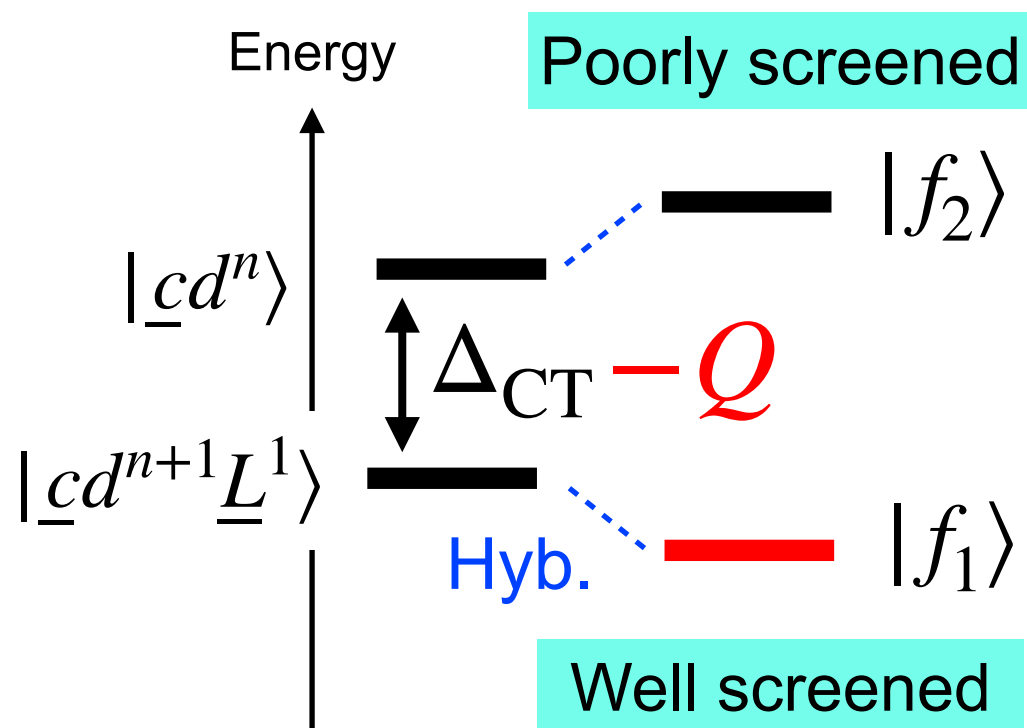
Metal - metal charge transfer : $d^n + d^n \rightarrow d^{n+1} + d^{n-1}$

: information on d bands (near Fermi energy)



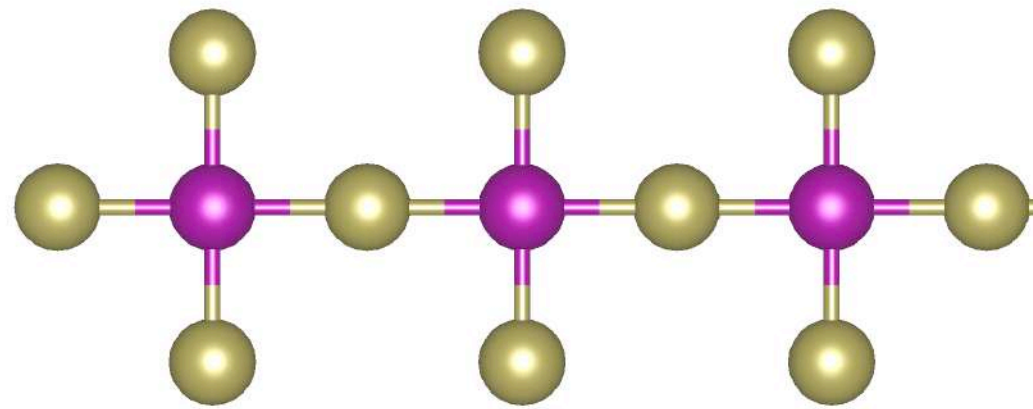
Final state (with a core-hole):

$$|f\rangle = |\underline{c}d^n\rangle + |\underline{c}d^{n+1}\underline{L}\rangle + \dots$$

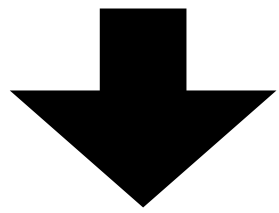


Quantum embedding approach to core-level spectroscopies

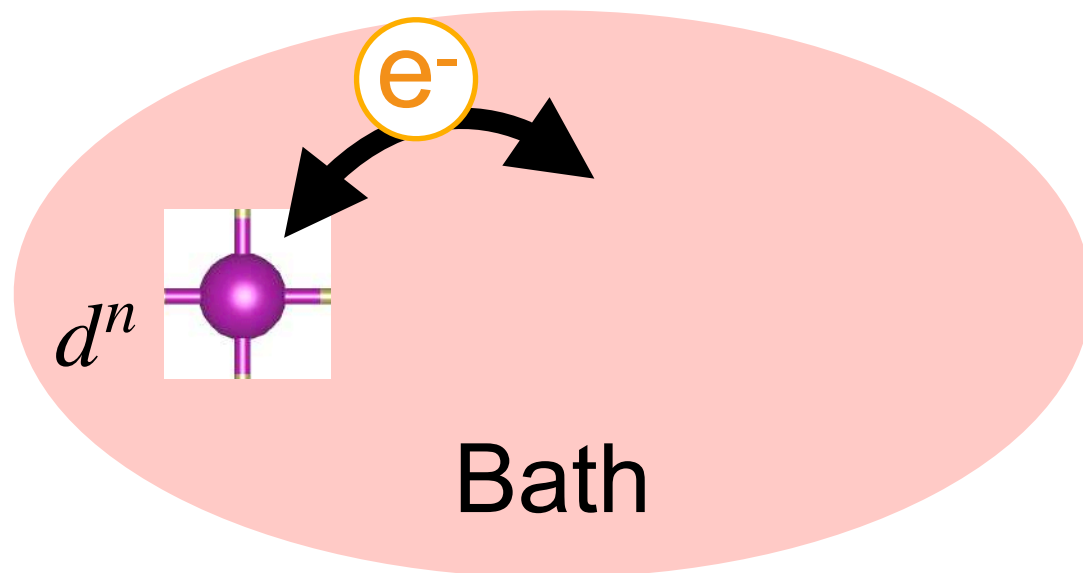
Fermi golden rule



Quantum embedding



: **DFT + DMFT**
Anderson model



Incl. both **ligand** and
metal 3d bands

X-ray transition (dipole)

$$F(E_B) = \sum_f |\langle f | \overline{T} | g \rangle|^2 \delta(E_B - E_f - E_g)$$

$$E_B = \omega - \varepsilon - \phi,$$

ε : Kinetic energy of PE

ω : Photon energy

Core orbitals and their interaction included
.....

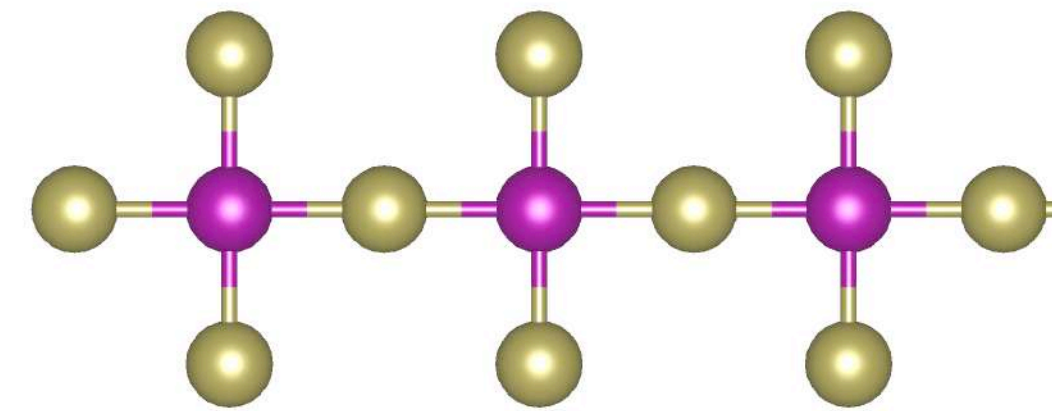
$$H_{\text{DMFT-AIM}} + H_{\text{core}} + H_{\text{core-valence}}$$

: spin-orbit coupling

: core-valence Coulomb multiplet

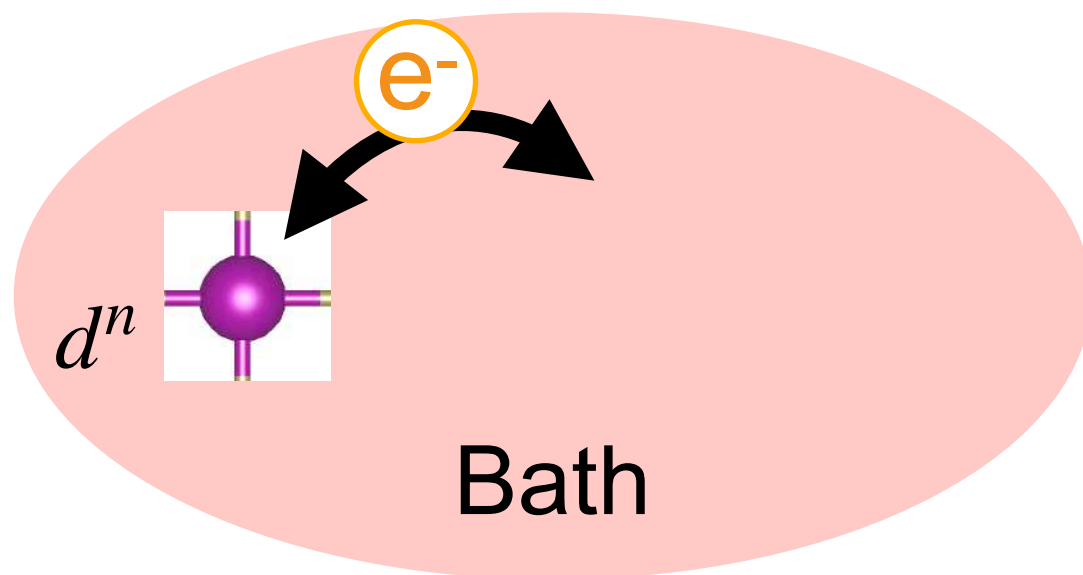
(Monopole part is adjusted to fit
the experimental spectrum)

Quantum embedding approach to core-level spectroscopies



Quantum embedding

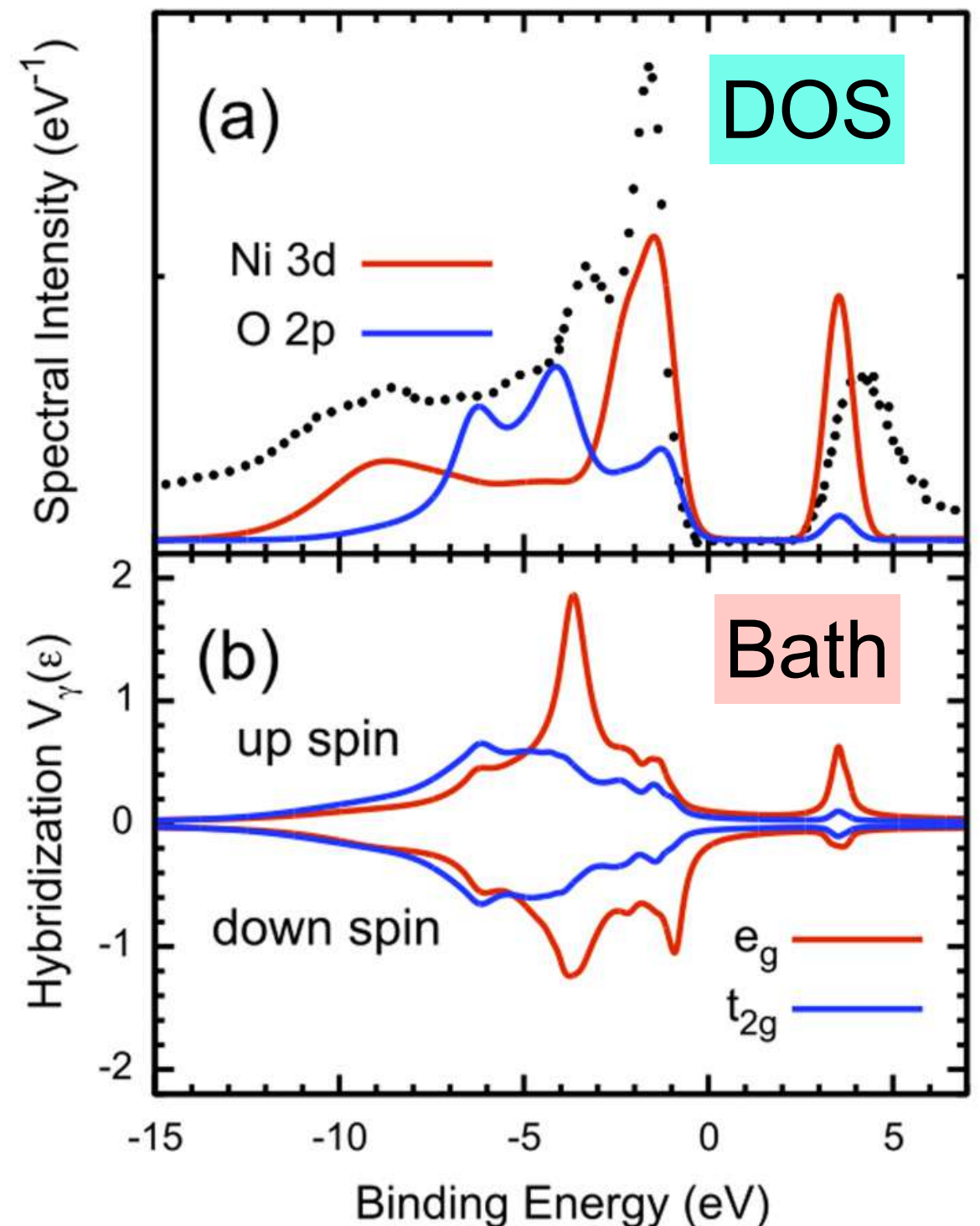
: DFT + DMFT
Anderson model



Incl. both **ligand** and
metal 3d bands

NiO

A. Hariki et al., PRB **96**, 045111 (2017)



Quantum embedding approach to core-level spectroscopies

Hybridization density $V^2(\varepsilon)$

: Key quantity in embedding approach

: hybridization property of 3d orbitals
in the metal site (impurity) with the crystal

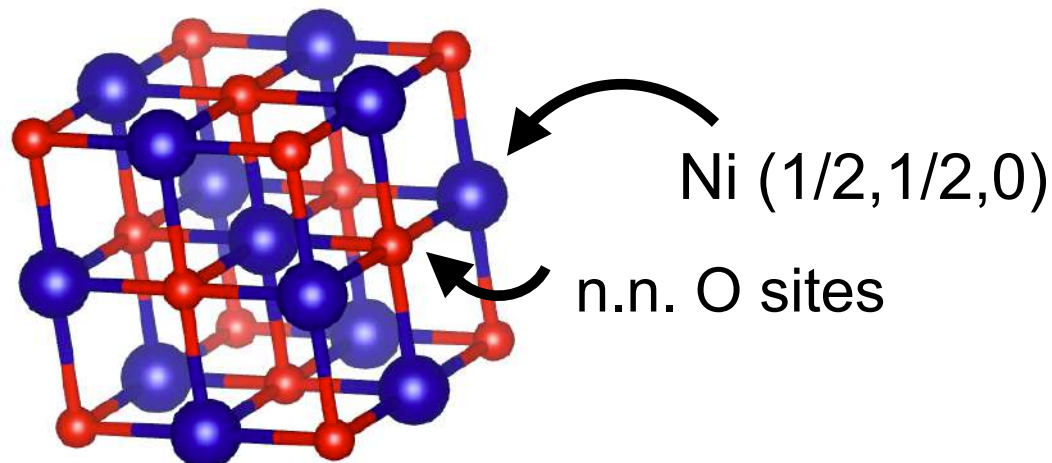
Local Hamiltonian
(at embedded site)

Local GF

$$\Delta(\varepsilon) = \varepsilon - \underbrace{H_{\text{imp}}}_{\text{Local Hamiltonian}} - \underbrace{\Sigma(\varepsilon)}_{\text{DMFT self-energy}} - \underbrace{G^{-1}(\varepsilon)}_{\text{Local GF}}$$

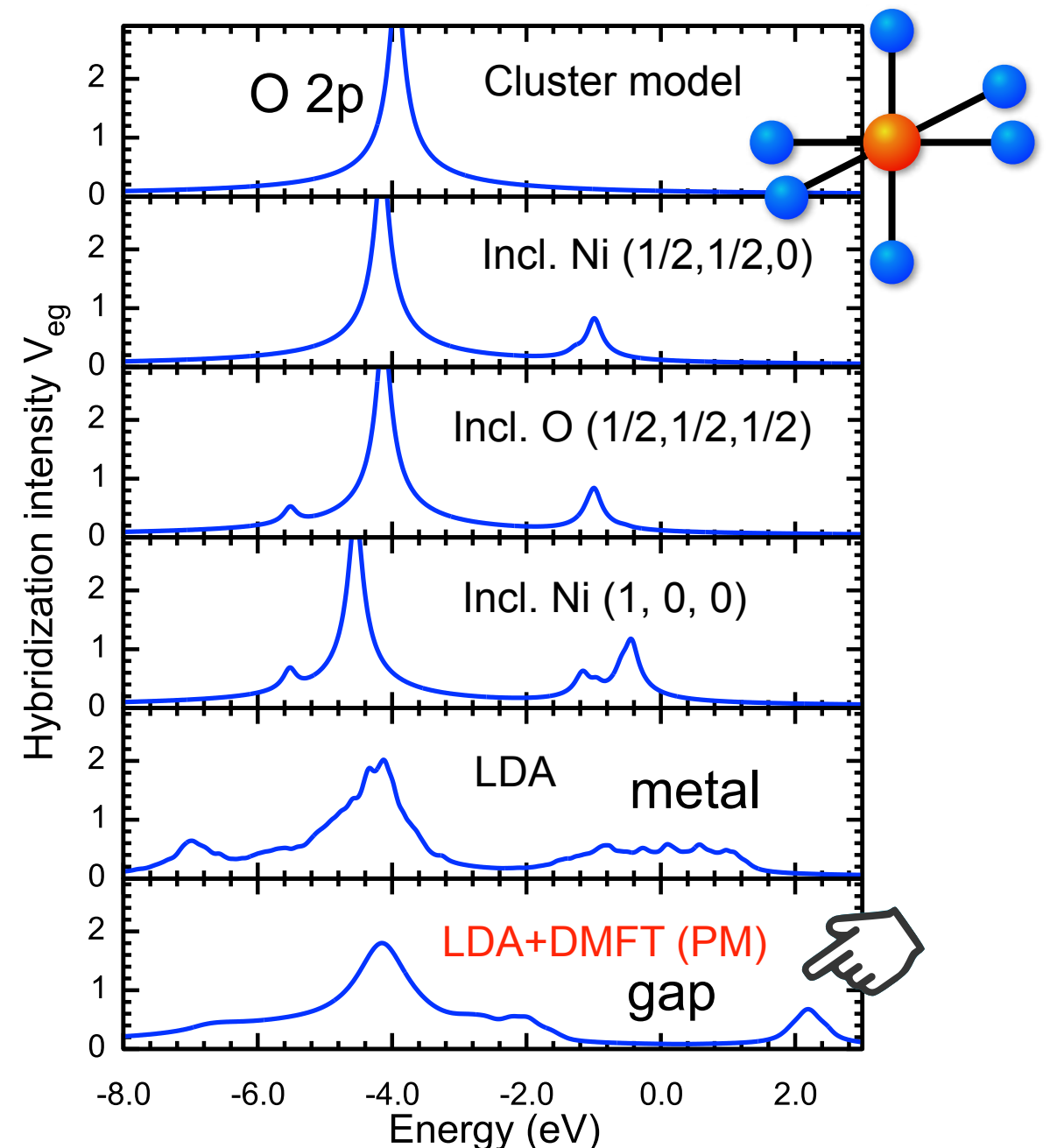
DMFT self-energy

$$\begin{aligned} \underline{V_\gamma^2(\varepsilon)} &= \sum_i |\langle \psi_{\gamma,i} | \hat{V}_{\text{imp-host}} | d_\gamma \rangle|^2 \delta(\varepsilon - \varepsilon_{\gamma,i}) \\ &= -\frac{1}{\pi} \text{Im} \langle d_\gamma | \hat{V}_{\text{imp-host}} \underbrace{\frac{1}{\varepsilon - H_{\text{host}}(\varepsilon)}}_{\Delta(\varepsilon)} \hat{V}_{\text{host-imp}} | d_\gamma \rangle \end{aligned}$$



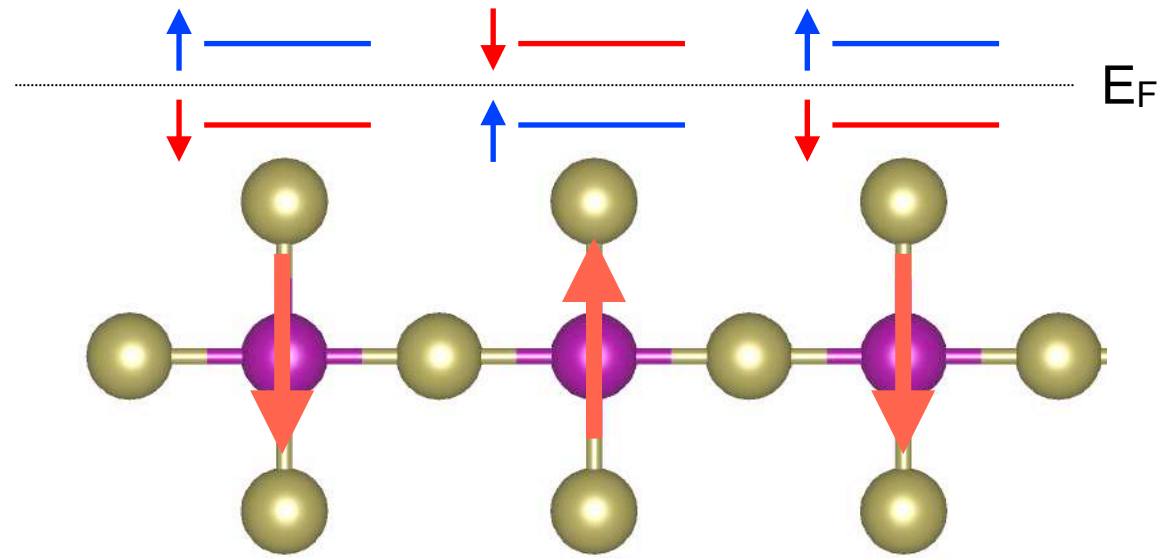
Hybridization density of Ni e_g orbital

M. Ghiasi, **AH** et al., Phys. Rev. B **100**, 075146 (2019)



Note : Coulomb interaction is not included in $V(\varepsilon)$ of the finite-size clusters in figures

Quantum embedding approach to core-level spectroscopies



NiO

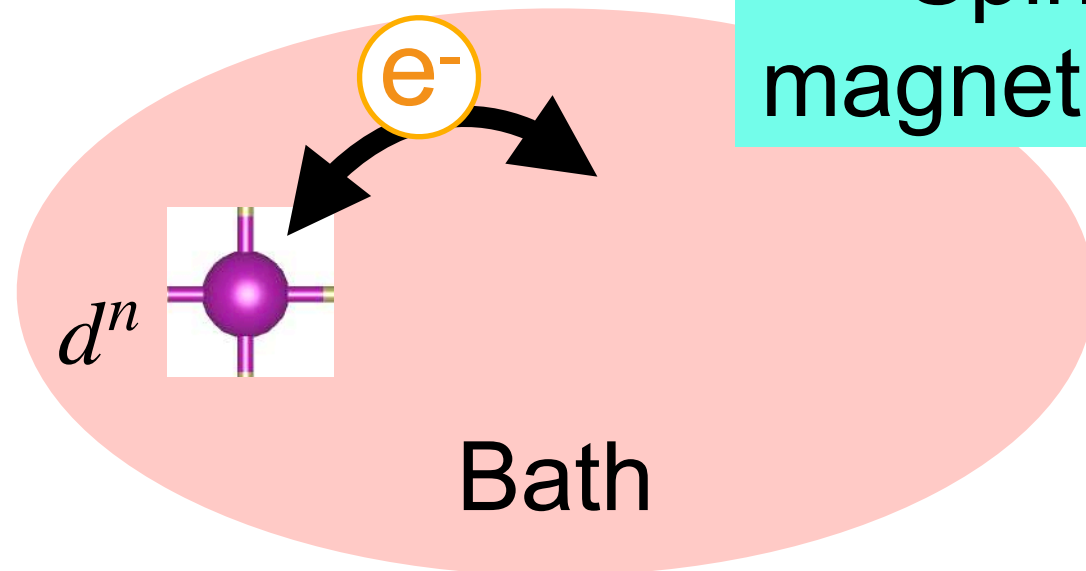
A. Hariki et al., PRB **96**, 045111 (2017)

Quantum embedding

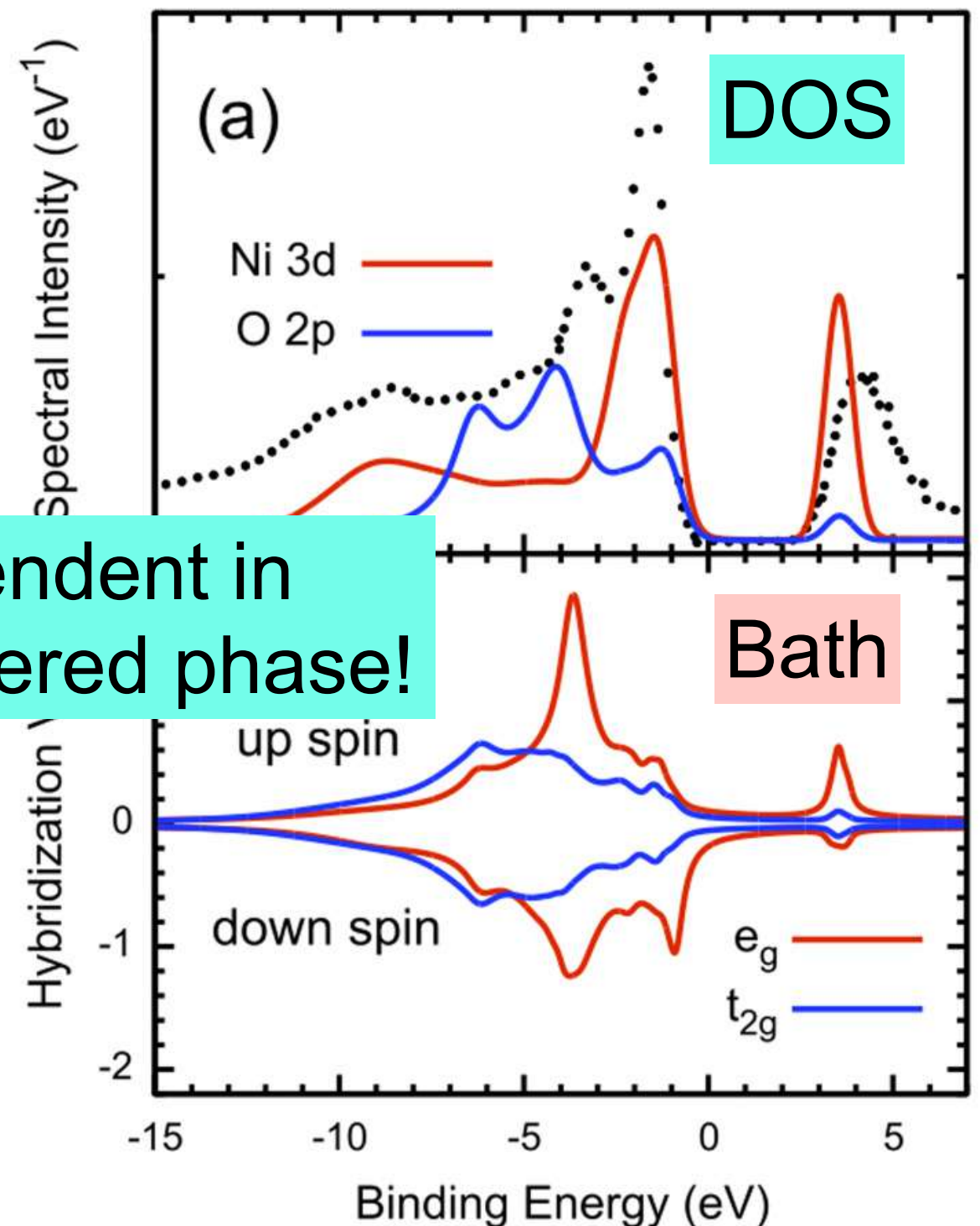
: **DFT + DMFT**

Anderson model

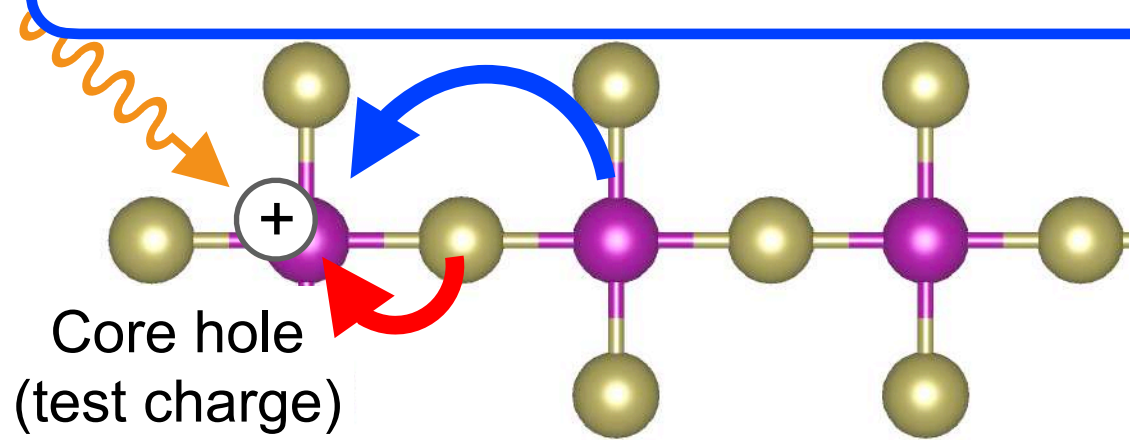
Spin dependent in
magnetic ordered phase!



Incl. both **ligand** and
metal 3d bands

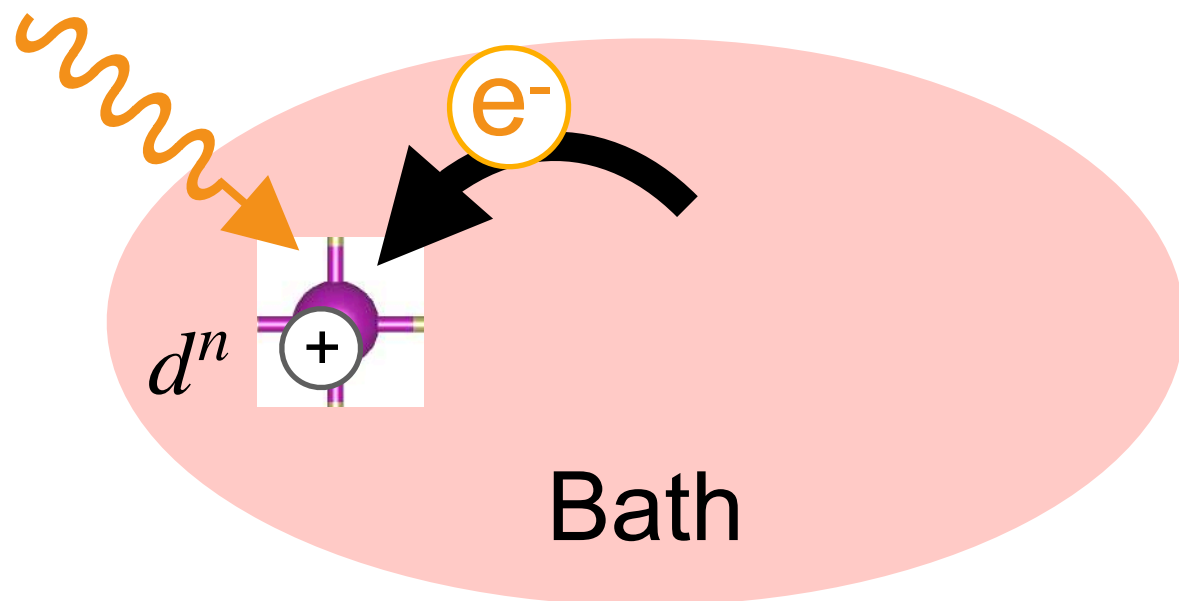


Metal - metal charge transfer : $d^n + d^n \rightarrow d^{n+1} + d^{n-1}$
 : information on d bands (near Fermi energy)



Quantum embedding

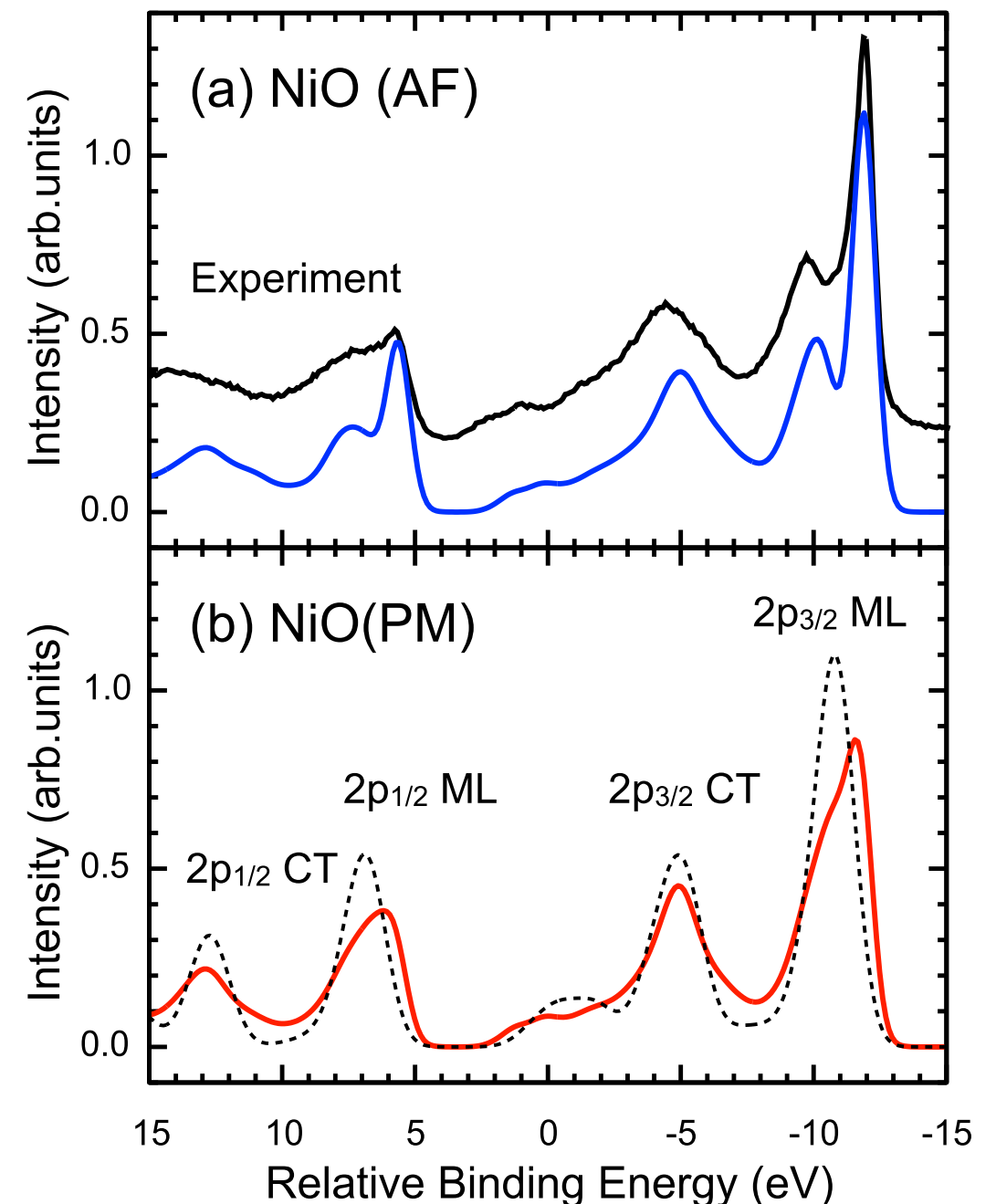
: **DFT + DMFT**
Anderson model



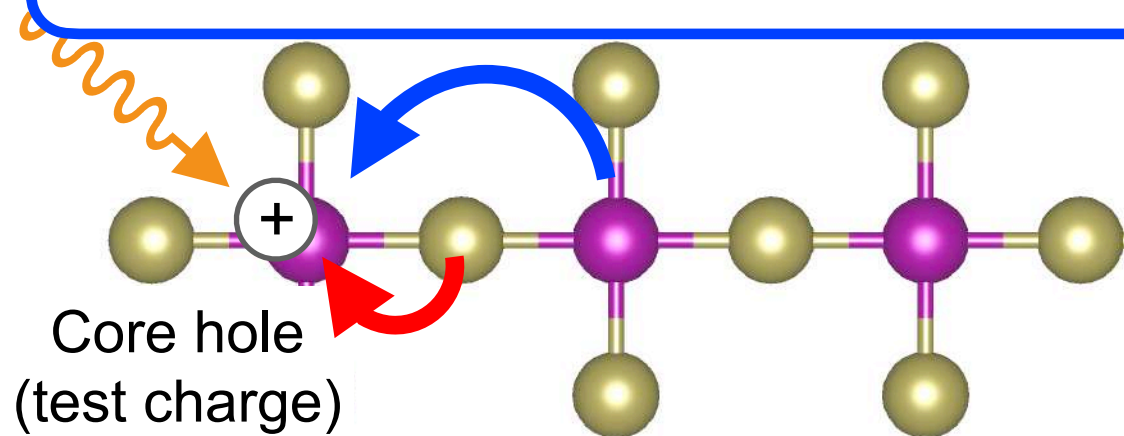
Incl. both **ligand** and
metal 3d bands

Calc. LDA+DMFT Anderson model

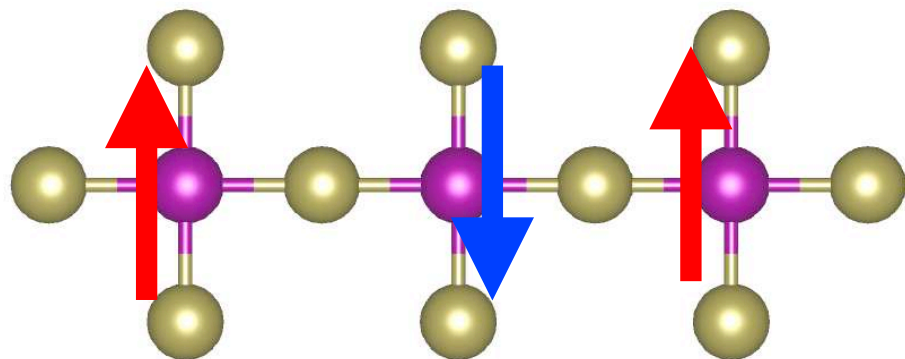
A. Hariki et al., PRB **96**, 045111 (2017)



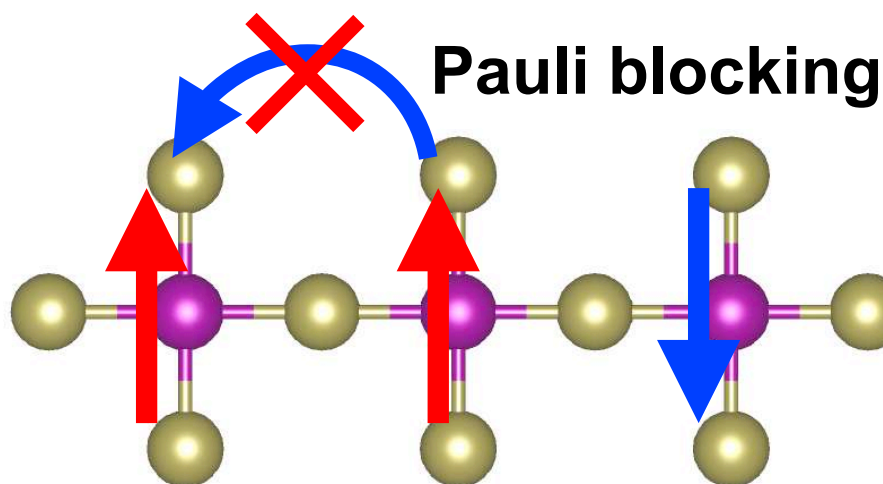
Metal - metal charge transfer : $d^n + d^n \rightarrow d^{n+1} + d^{n-1}$
 : information on d bands (near Fermi energy)



Antiferromagnetic phase:

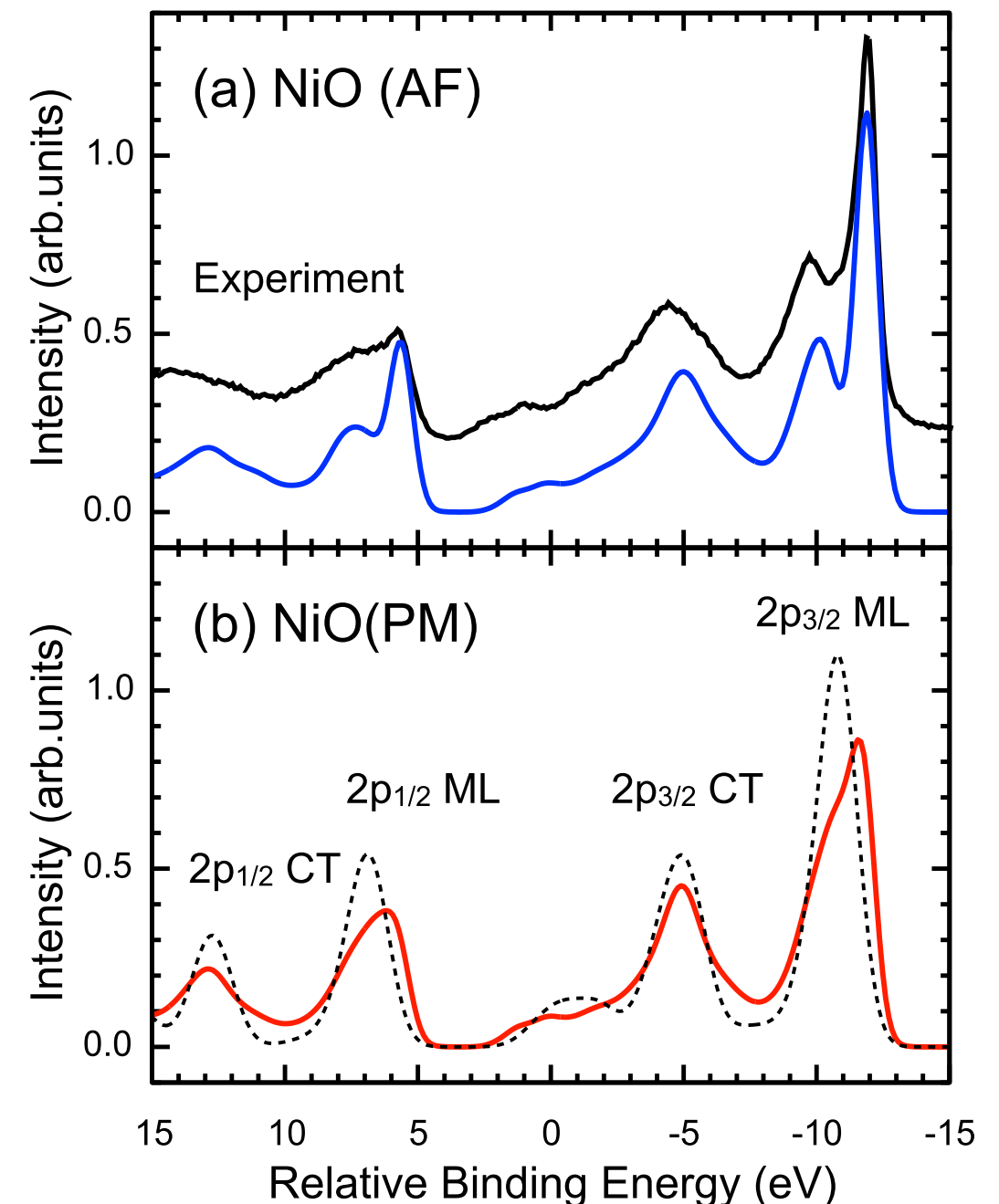


Paramagnetic phase (moment fluctuating):

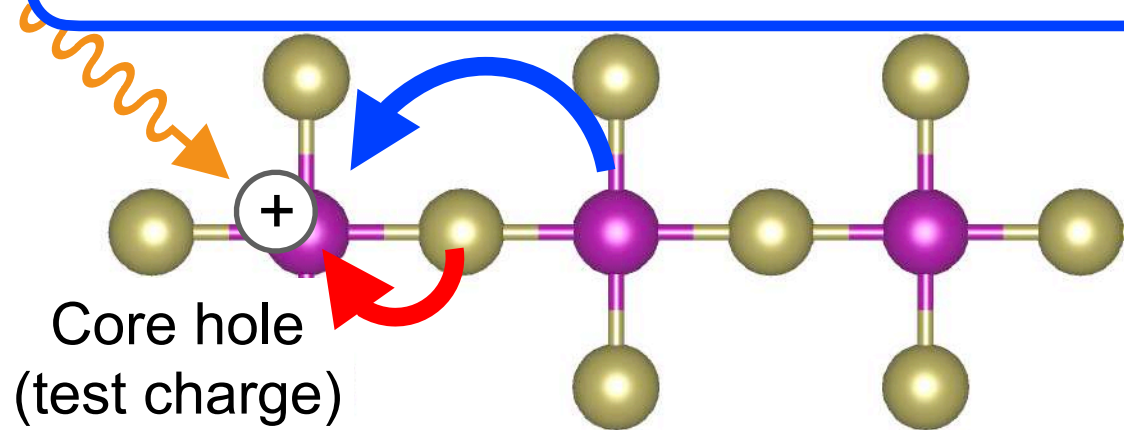


Calc. LDA+DMFT Anderson model

A. Hariki et al., PRB **96**, 045111 (2017)



Metal - metal charge transfer : $d^n + d^n \rightarrow d^{n+1} + d^{n-1}$
: information on d bands (near Fermi energy)



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Spin-selective evolution of the Zhang-Rice state in binary transition metal oxide MnO(001) film

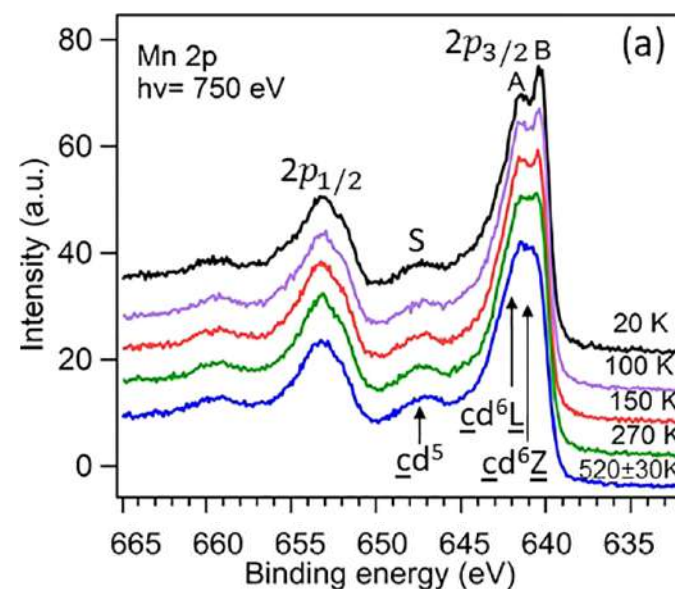
Asish K. Kundu^{1,2,3,4,*}, Polina M. Sheverdyayeva², Paolo Moras², Krishnakumar S. R. Menon⁵, Subhasish Mandal^{6,†}, and Carlo Carbone²

Show more

Phys. Rev. B **109**, 195111 – Published 3 May, 2024

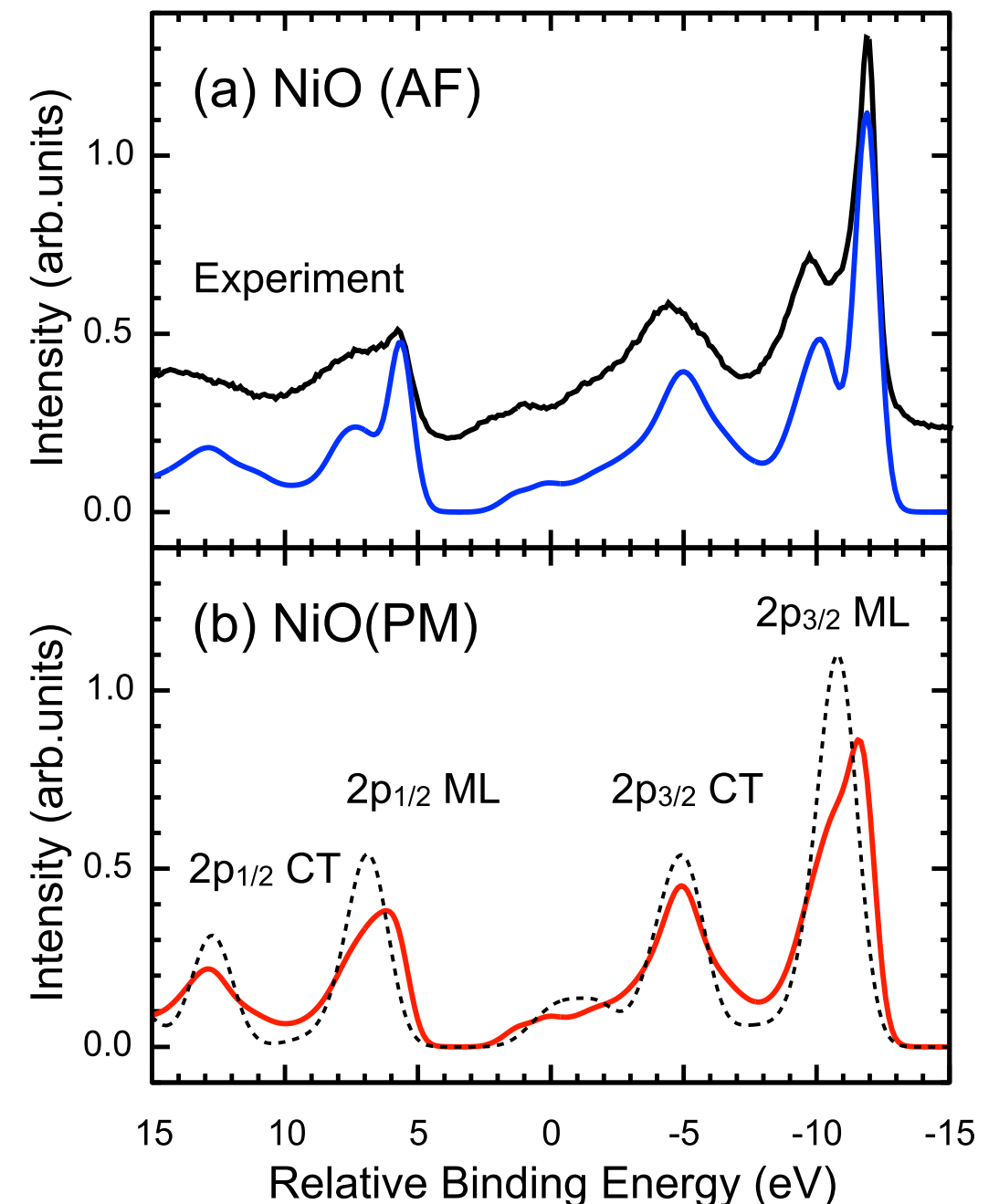
DOI: <https://doi.org/10.1103/PhysRevB.109.195111>

MnO, $T_N \sim 120\text{K}$



Calc. LDA+DMFT Anderson model

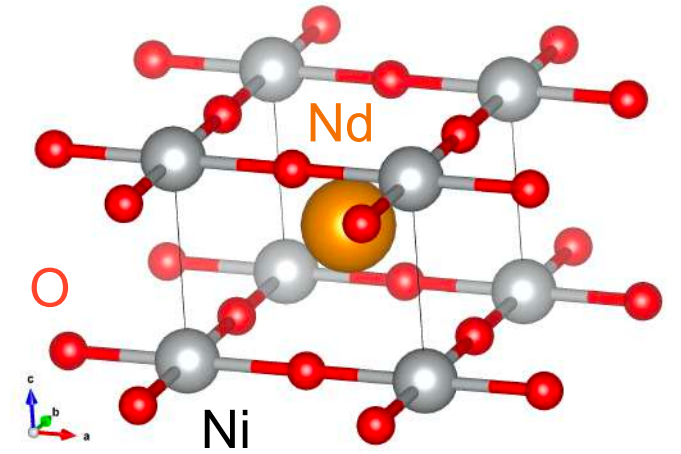
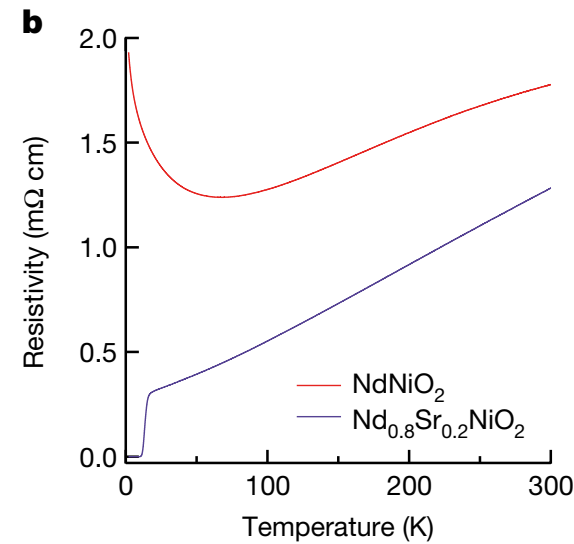
A. Hariki et al., PRB **96**, 045111 (2017)



Superconductivity in an infinite-layer nickelate

Danfeng Li, Kyuho Lee, Bai Yang Wang, Motoki Osada, Samuel Crossley, Hye Ryoung Lee, Yi Cui, Yasuyuki Hikita & Harold Y. Hwang

Nature 572, 624–627 (2019) | Cite this article



- ✓ Two dimensional structure
- ✓ Formally Ni is monovalent (d^9)

Core-Level X-Ray Spectroscopy of Infinite-Layer Nickelate: LDA + DMFT Study

 Keisuke Higashi,¹ Mathias Winder,² Jan Kuneš,² and Atsushi Hariki^{1,*}
¹Department of Physics and Electronics,

Osaka Prefecture University 1-1 Gakuen-cho, Nakaku, Sakai, Osaka 599-8531, Japan

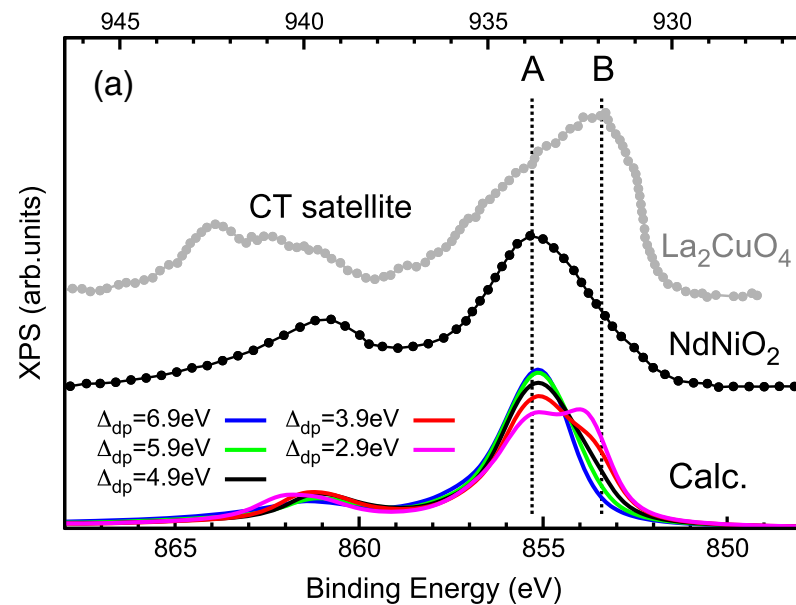
²Institute of Solid State Physics, TU Wien, 1040 Vienna, Austria

(Received 11 May 2021; revised 4 August 2021; accepted 7 September 2021; published 13 October 2021; corrected 11 November 2021 and 23 November 2021)

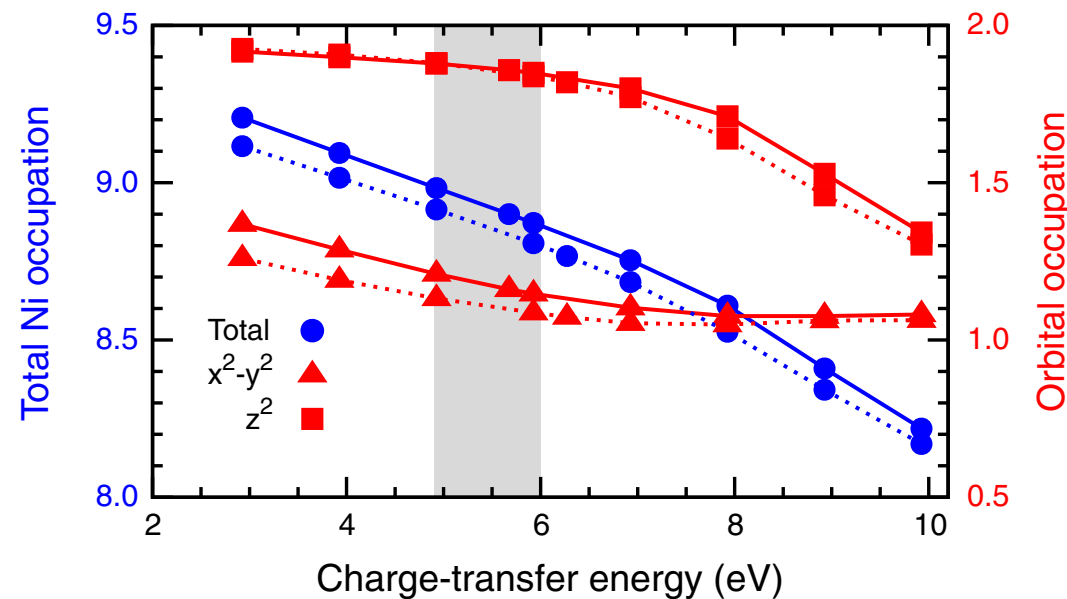
Motivated by recent core-level x-ray photoemission spectroscopy, x-ray absorption spectroscopy (XAS), and resonant inelastic x-ray scattering (RIXS) experiments for the newly discovered superconducting infinite-layer nickelate, we investigate the core-level spectra of the parent compounds NdNiO_2 and LaNiO_2 using the combination of local density approximation and dynamical mean-field theory (LDA + DMFT). Adjusting a charge-transfer energy to match the experimental spectra, we determine the optimal model parameters and discuss the nature of the NdNiO_2 ground state. We find that self-doping from the Nd 5d states in the vicinity of the Fermi energy prohibits opening of a Mott-Hubbard gap in NdNiO_2 . The present Ni L_3 XAS and RIXS calculation for LaNiO_2 cannot explain the difference from NdNiO_2 spectra.

Ni 2p Core-level XPS

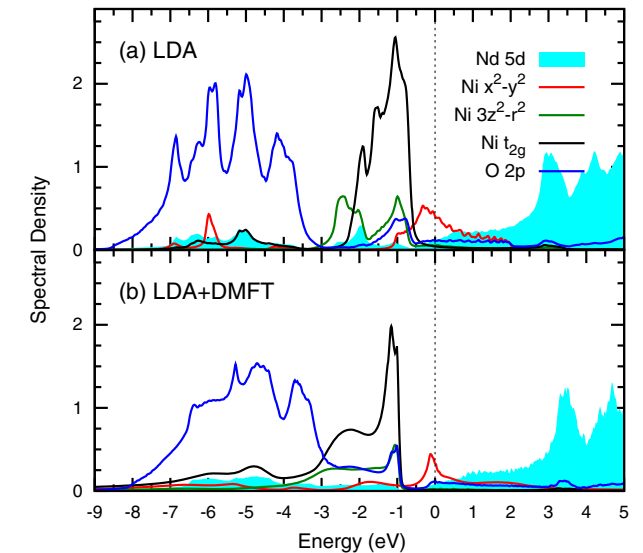
$$\Delta_{dp} = (\epsilon_d^{\text{LDA}} - \mu_{\text{dc}}) + 9U_{dd} - \epsilon_p^{\text{LDA}}$$



Ni valency and orbital occupation



Valence spectra



- ✓ Intermediate regime between the Mott-Hubbard and charge-transfer system
- ✓ Single band (Ni x^2-y^2) model with a small self-doping from Nd 5d states

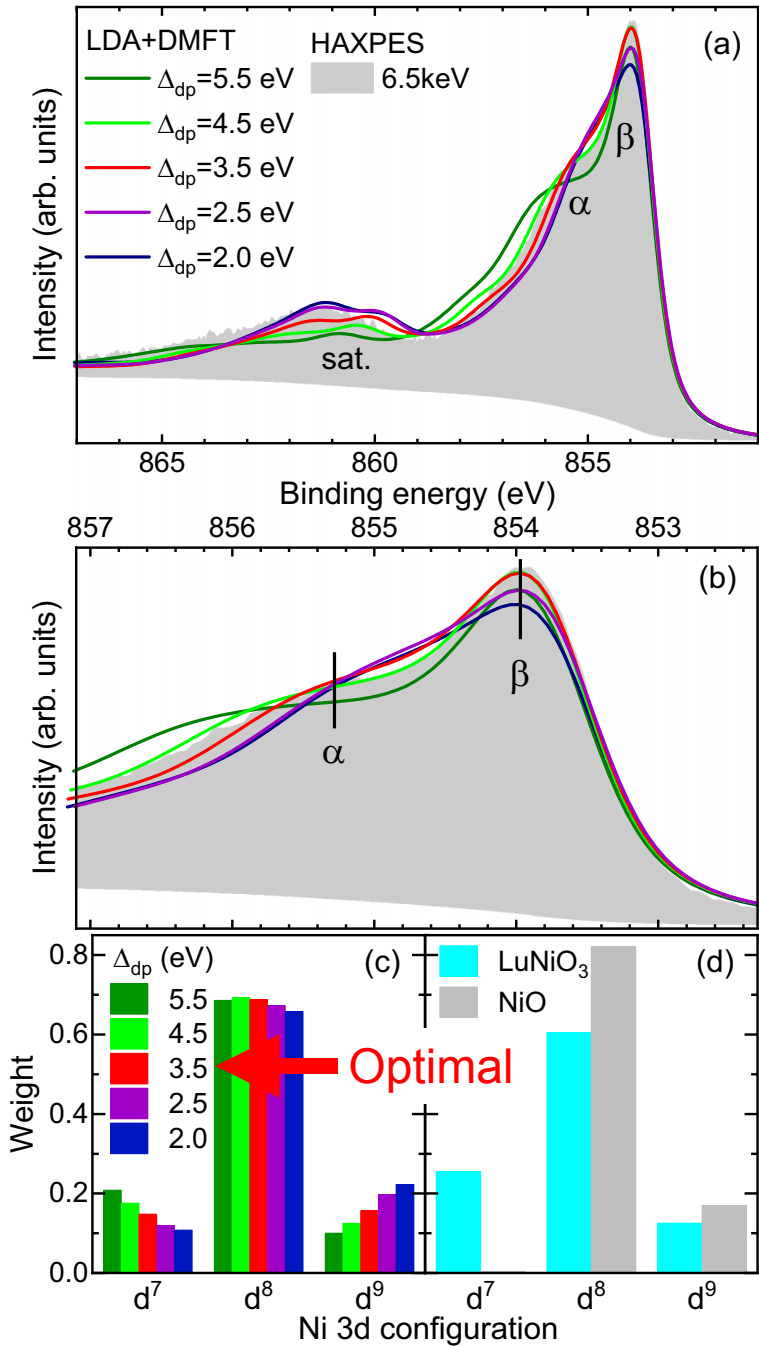
ACCEPTED PAPER

Valence, charge transfer, and orbital-dependent correlation in bilayer nickelates $\text{Nd}_3\text{Ni}_2\text{O}_7$

Daisuke Takegami, Takaki Okauchi, Edgar Abarca Morales, Kouto Fujinuma, Mizuki Furo, Masato Yoshimura, Ku-Ding Tsuei, Grace A. Pan, Dan Ferenc Segedin, Qi Song, Hanjong Paik, Charles M. Brooks, Julia A. Mundy, Takashi Mizokawa, Liu Hao Tjeng, Berit H. Goodge, and Atsushi Hariki

Phys. Rev. B - Accepted 17 March, 2025

Accepted in PRB



$\text{Ni}^{2+} + \text{Ni}^{3+}$?
Different multiplet, hybridization ?

nature

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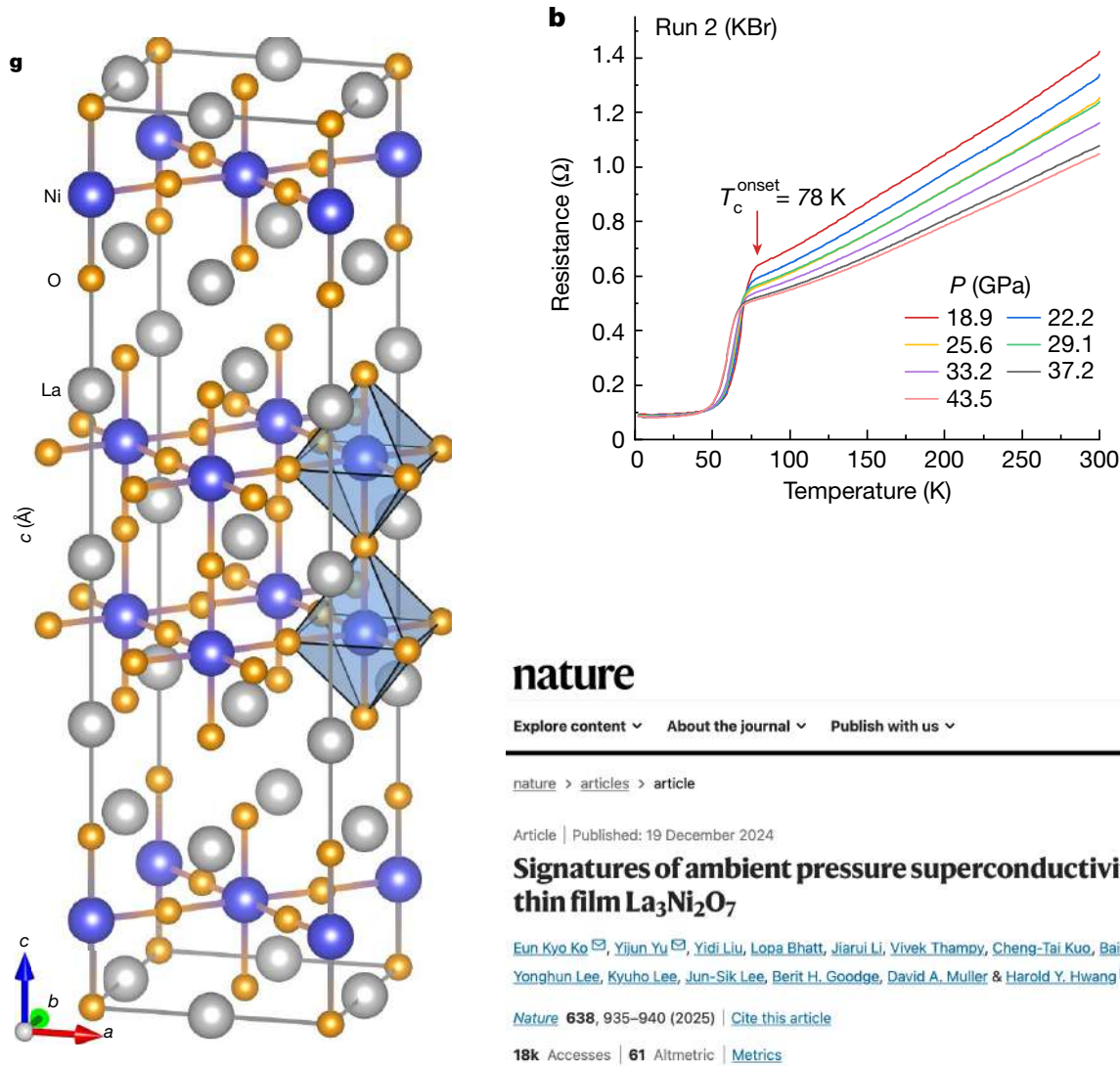
nature > articles > article

Article | Published: 12 July 2023

Signatures of superconductivity near 80 K in a nickelate under high pressure

Hualei Sun, Mengwu Huo, Xunwu Hu, Jingyuan Li, Zengjia Liu, Yifeng Han, Lingyun Tang, Zhongquan Mao, Pengtao Yang, Bosen Wang, Jinguang Cheng, Dao-Xin Yao, Guang-Ming Zhang & Meng Wang

Nature 621, 493–498 (2023) | Cite this article



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Article | Published: 19 December 2024

Signatures of ambient pressure superconductivity in thin film $\text{La}_3\text{Ni}_2\text{O}_7$

Eun Kyo Ko, Yijun Yu, Yidi Liu, Lopa Bhatt, Jiarui Li, Vivek Thampy, Cheng-Tai Kuo, Bai Yang Wang, Yonghun Lee, Kyuho Lee, Jun-Sik Lee, Berit H. Goodge, David A. Muller & Harold Y. Hwang

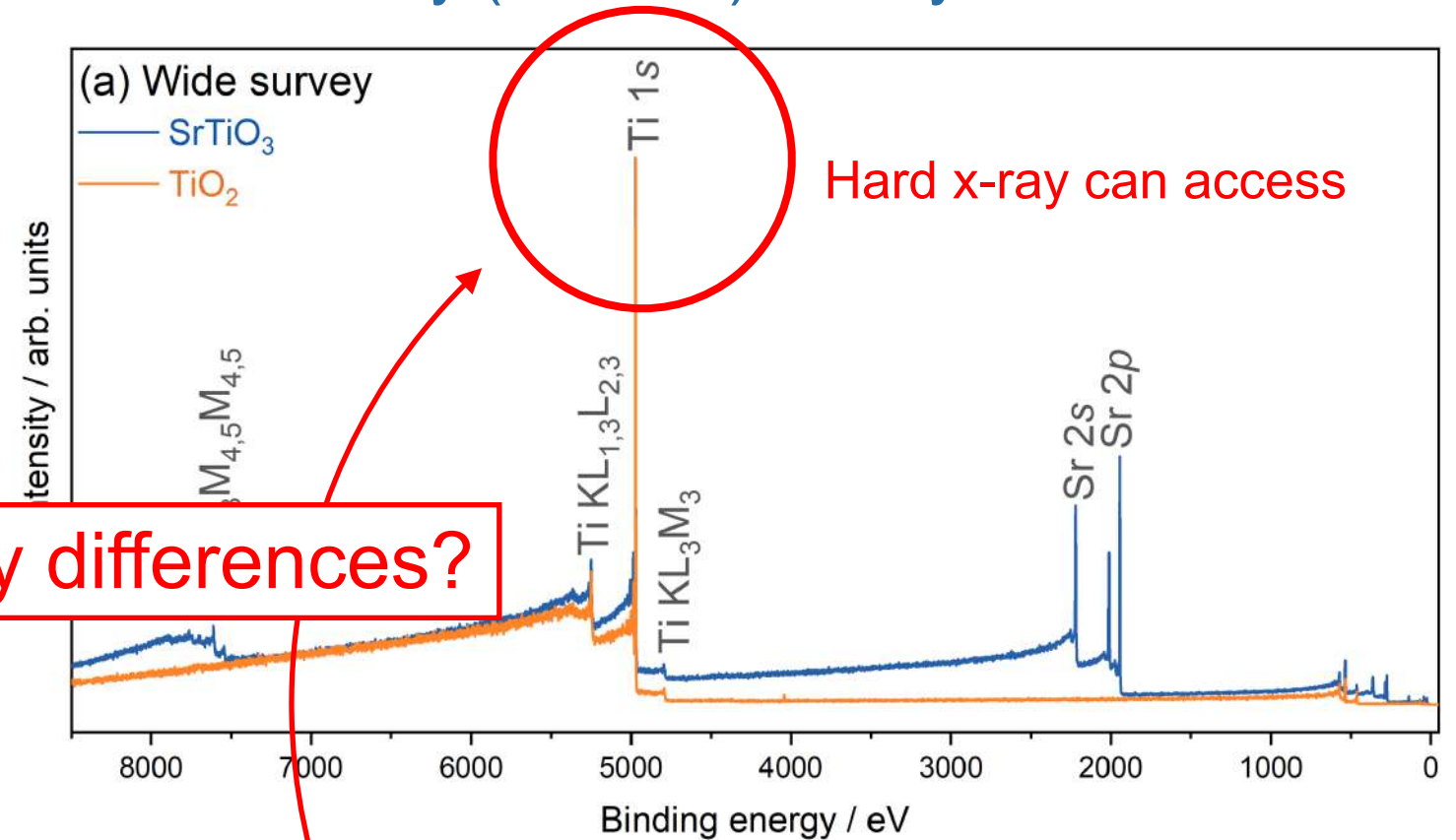
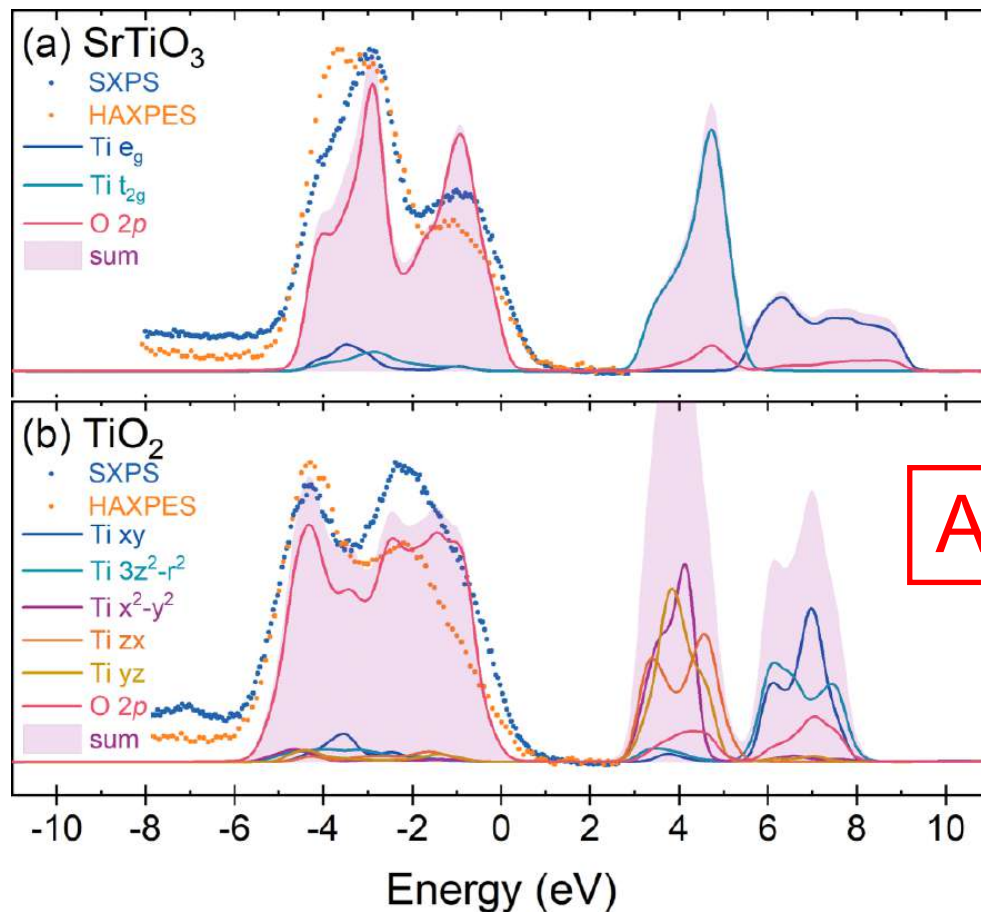
Nature 638, 935–940 (2025) | Cite this article

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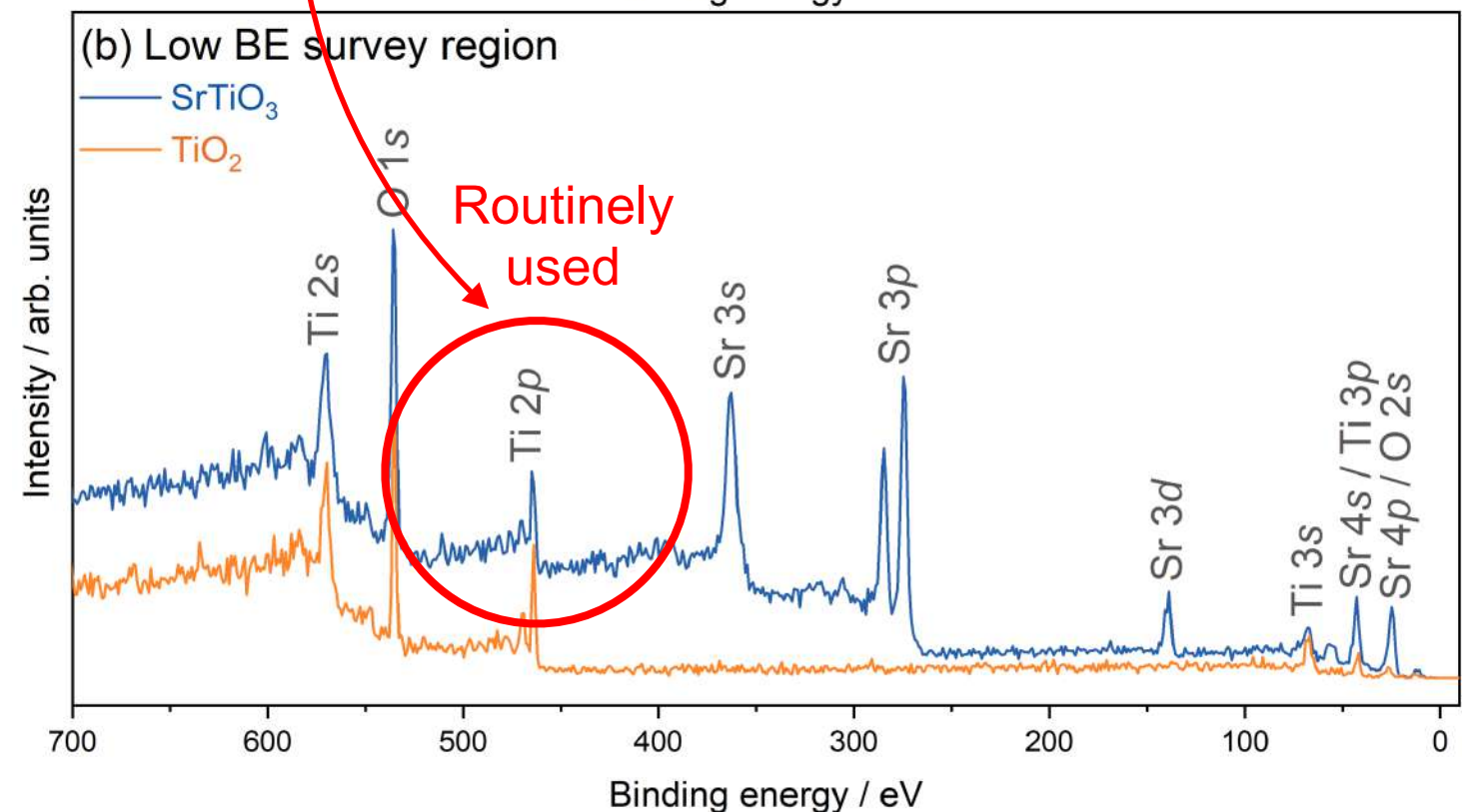
Differences in different core levels? AH et al., Phys. Rev. B. 106, 205138 (2022)

SrTiO₃, TiO₂; band insulator (3d⁰)

Hard x-ray (~10keV) survey of core-levels

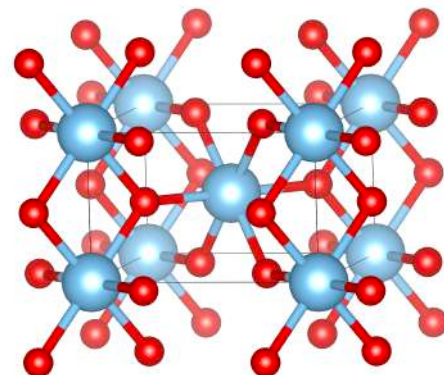
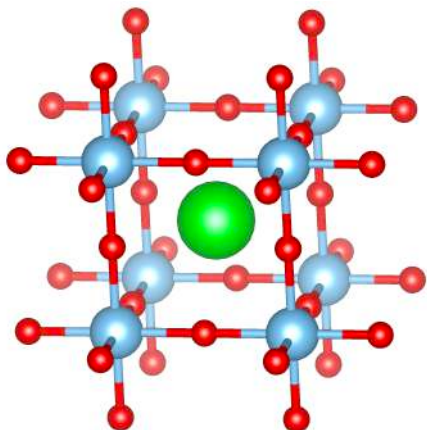


Any differences?



SrTiO₃
(Perovskite structure)

TiO₂
(Rutile structure)

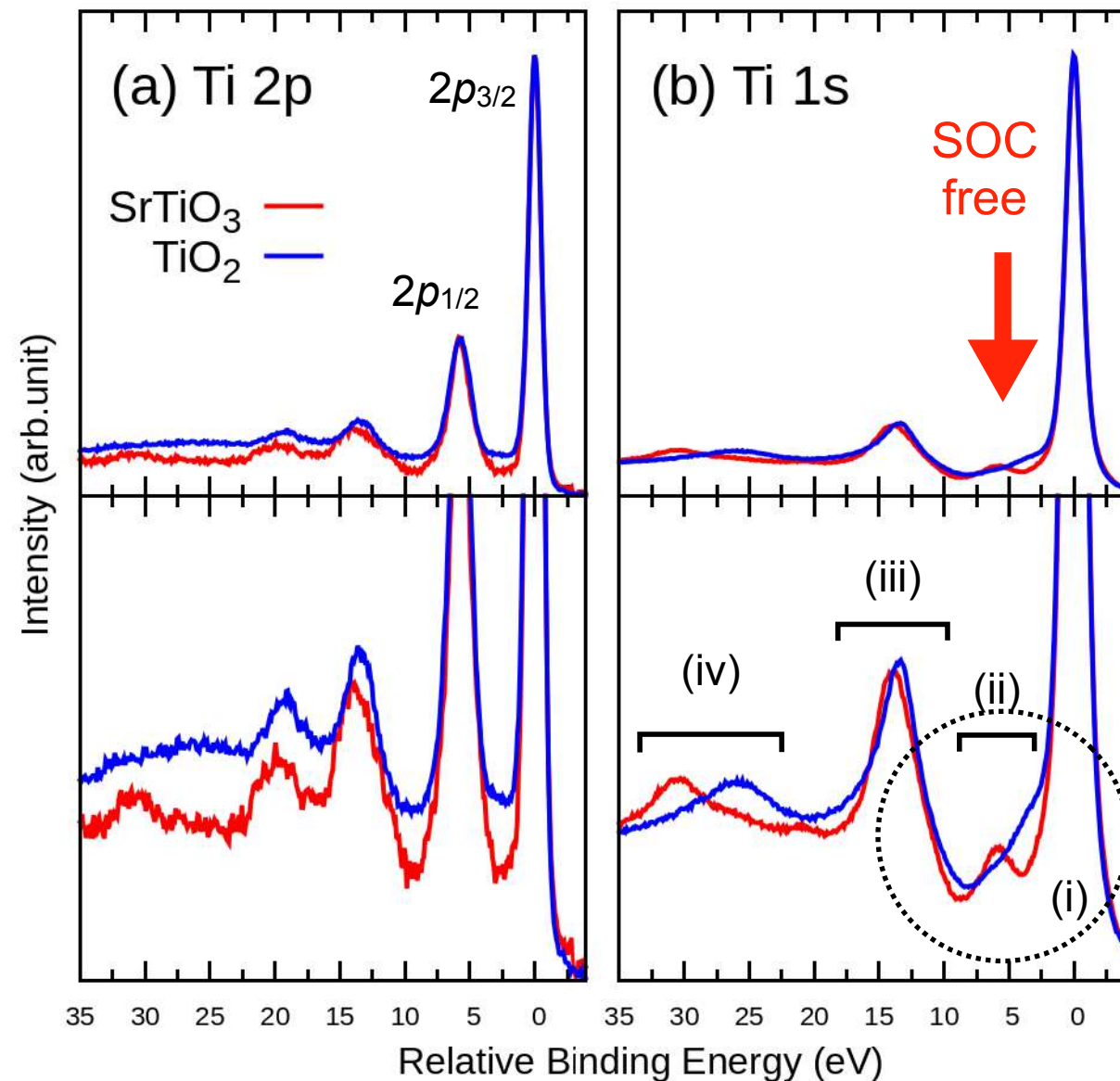


1) Absence of Spin-Orbit Coupling

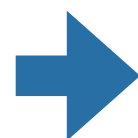
AH et al., Phys. Rev. B. 106, 205138 (2022)

Exp. Ti 1s and 2p HAXPES

First report : J. C. Woicik et al., Phys. Rev. B 101, 245119 (2020)



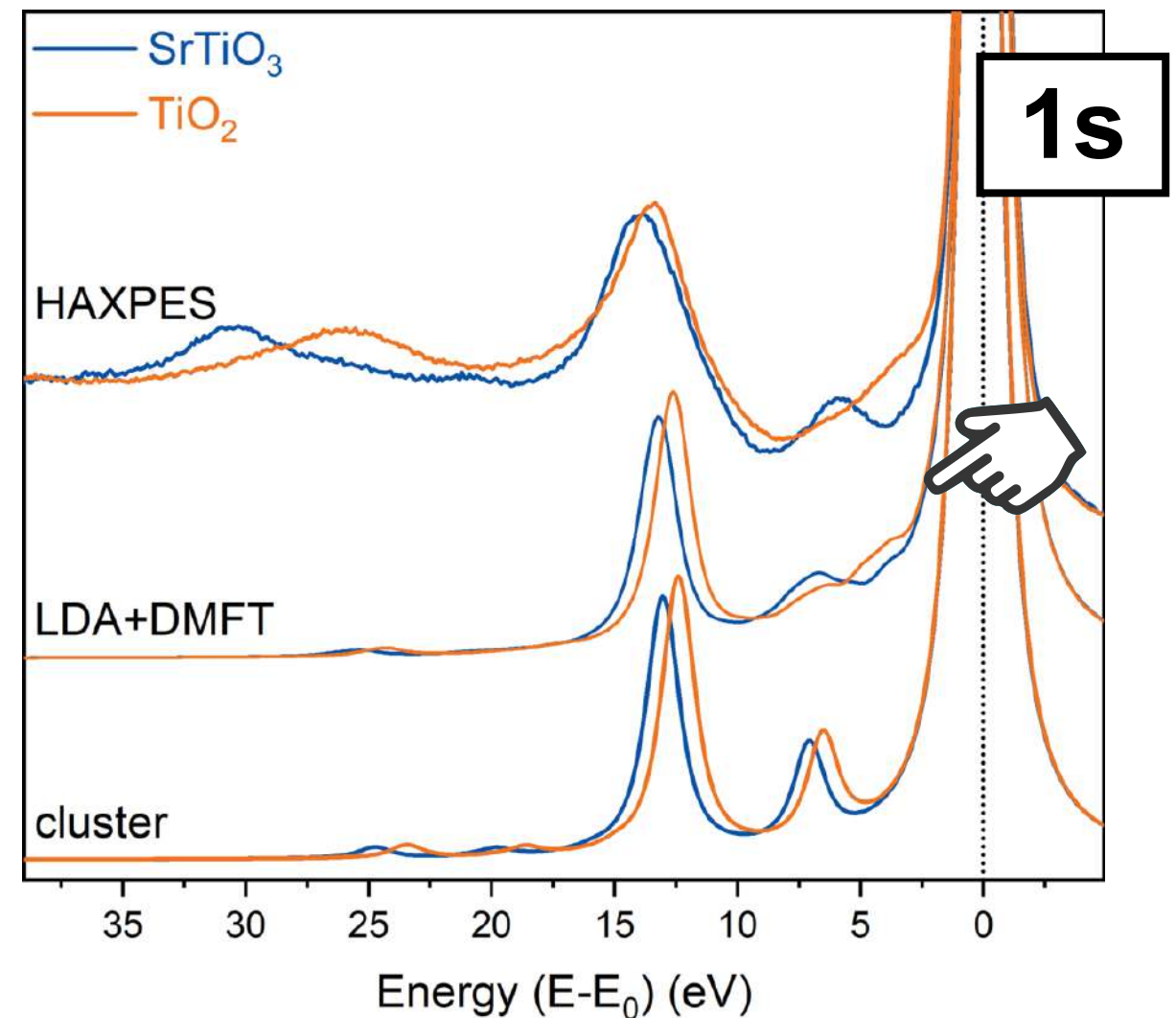
Material-dependent satellite
in SOC-free 1s HAXPES



LDA+DMFT & cluster-model calc.

incl. O bands

incl. only nearest O sites



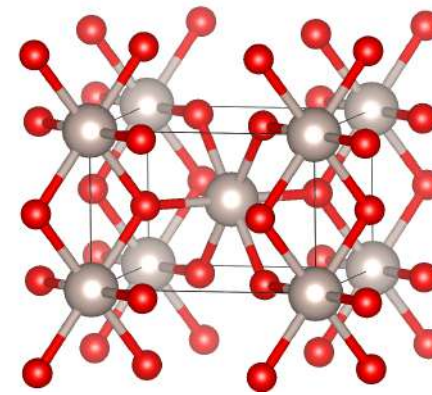
The hidden satellites reflect
hybridization of Ti and O 2p bands

2) Absence of Core-Valence Multiplet

T. Yamaguchi, AH, et al.,
Phys. Rev. B **109**, 205143 (2024)

VO₂ and CrO₂, correlated metals

LDA+DMFT valence band

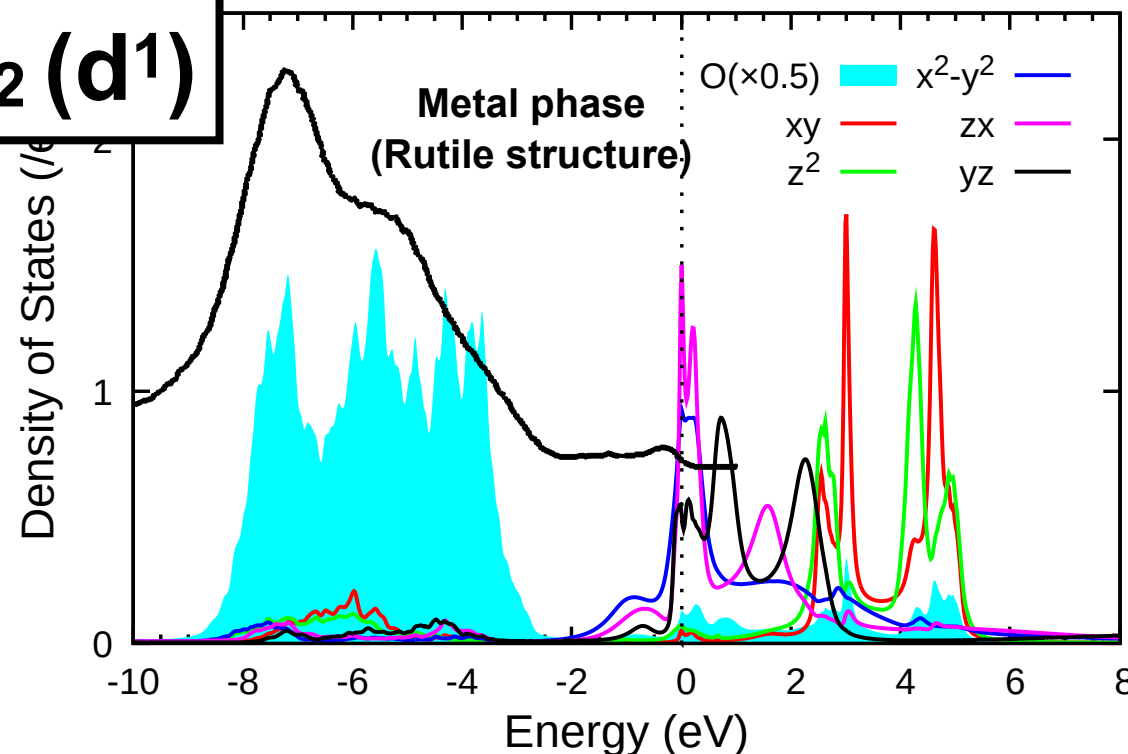


Rutile
structure

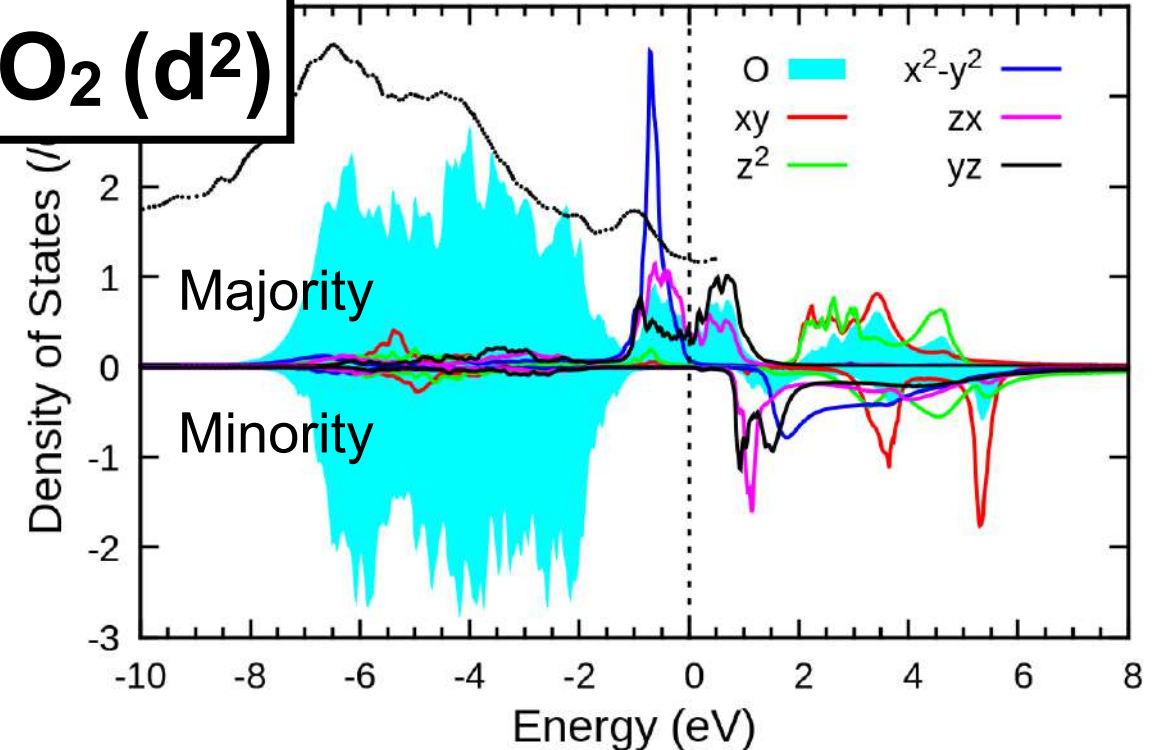
Exp. R. Eguchi et al., Phys. Rev. B **78**, 075115 (2008)

Exp. M. Sperlich et al., Phys. Rev. B **87**, 235138 (2013)

VO₂ (d¹)

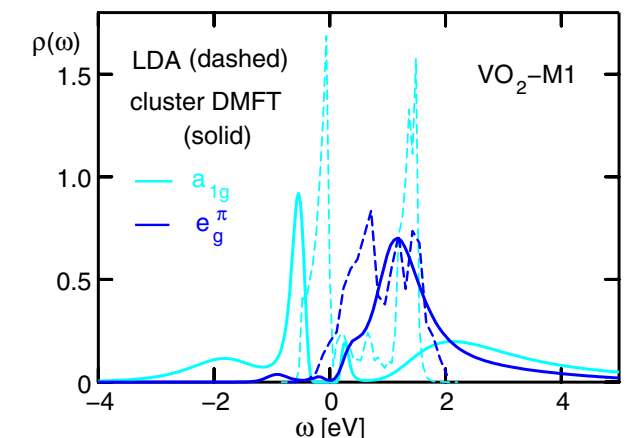


CrO₂ (d²)



VO₂ : Quasiparticle peak & Hubbard bands
CrO₂ : Half-metallic electronic structure

S. Biermann et al., Phys. Rev. Lett. **94**, 026404 (2005)

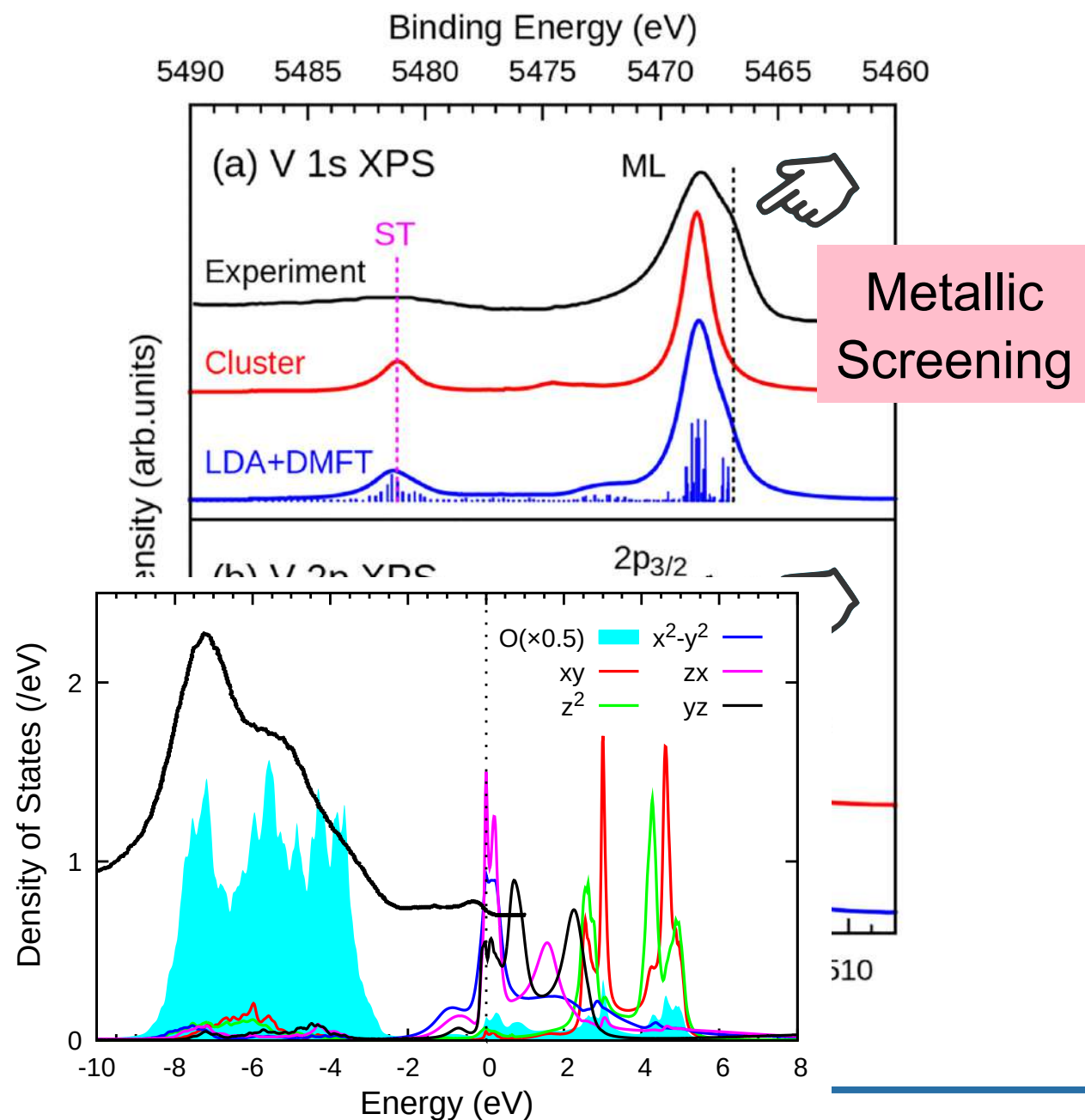


2) Absence of Core-Valence Multiplet

T. Yamaguchi, AH, et al.,
Phys. Rev. B **109**, 205143 (2024)

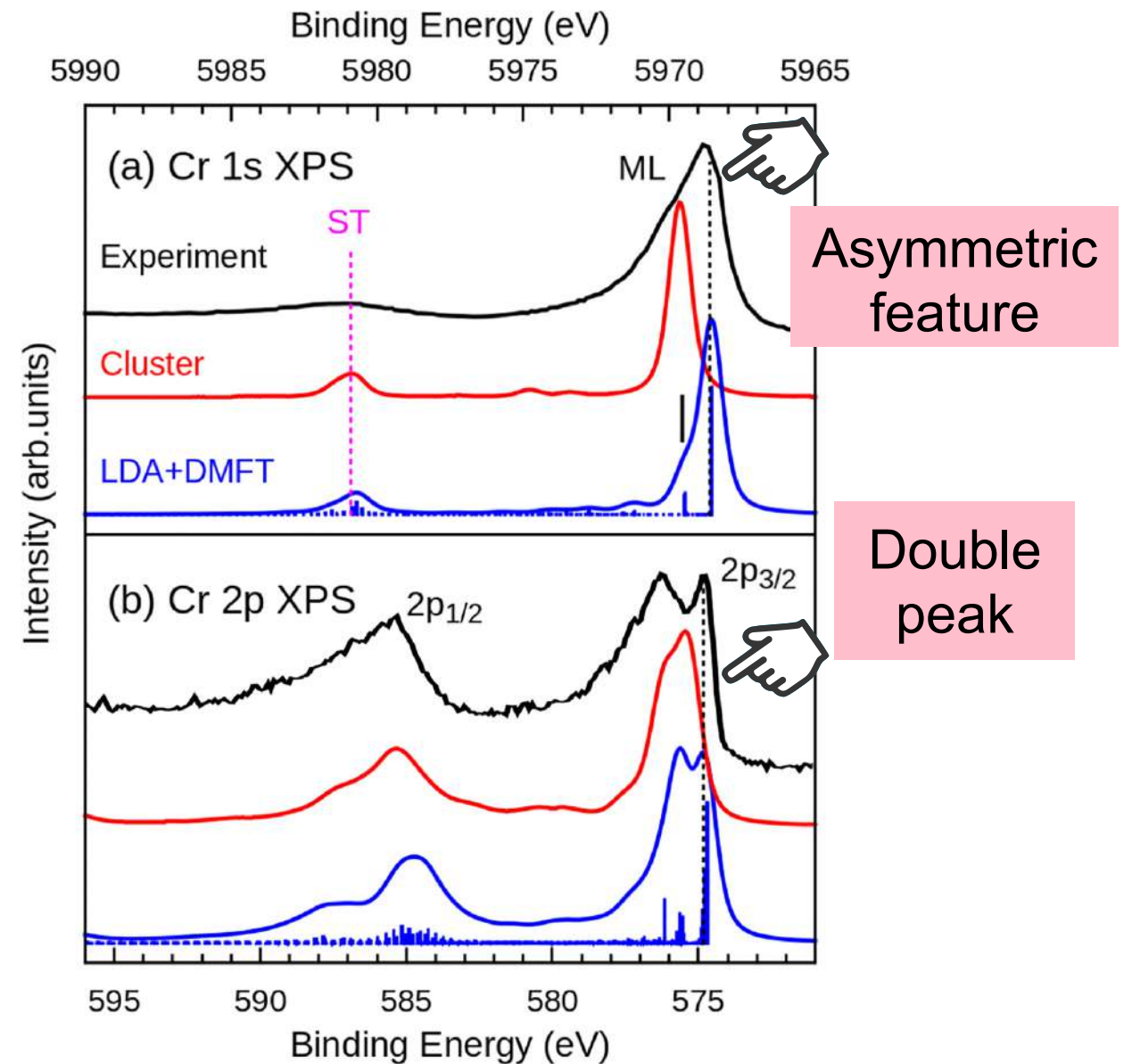
V 1s and 2p HAXPES in VO₂

Exp. R. Eguchi et al., Phys. Rev. B **78**, 075115 (2008)



Cr 1s and 2p HAXPES in CrO₂

Cr 2p data: M. Sperlich et al., Phys. Rev. B **87**, 235138 (2013)



VO₂ : 1s is replica of 2p, with nonlocal metallic screening feature

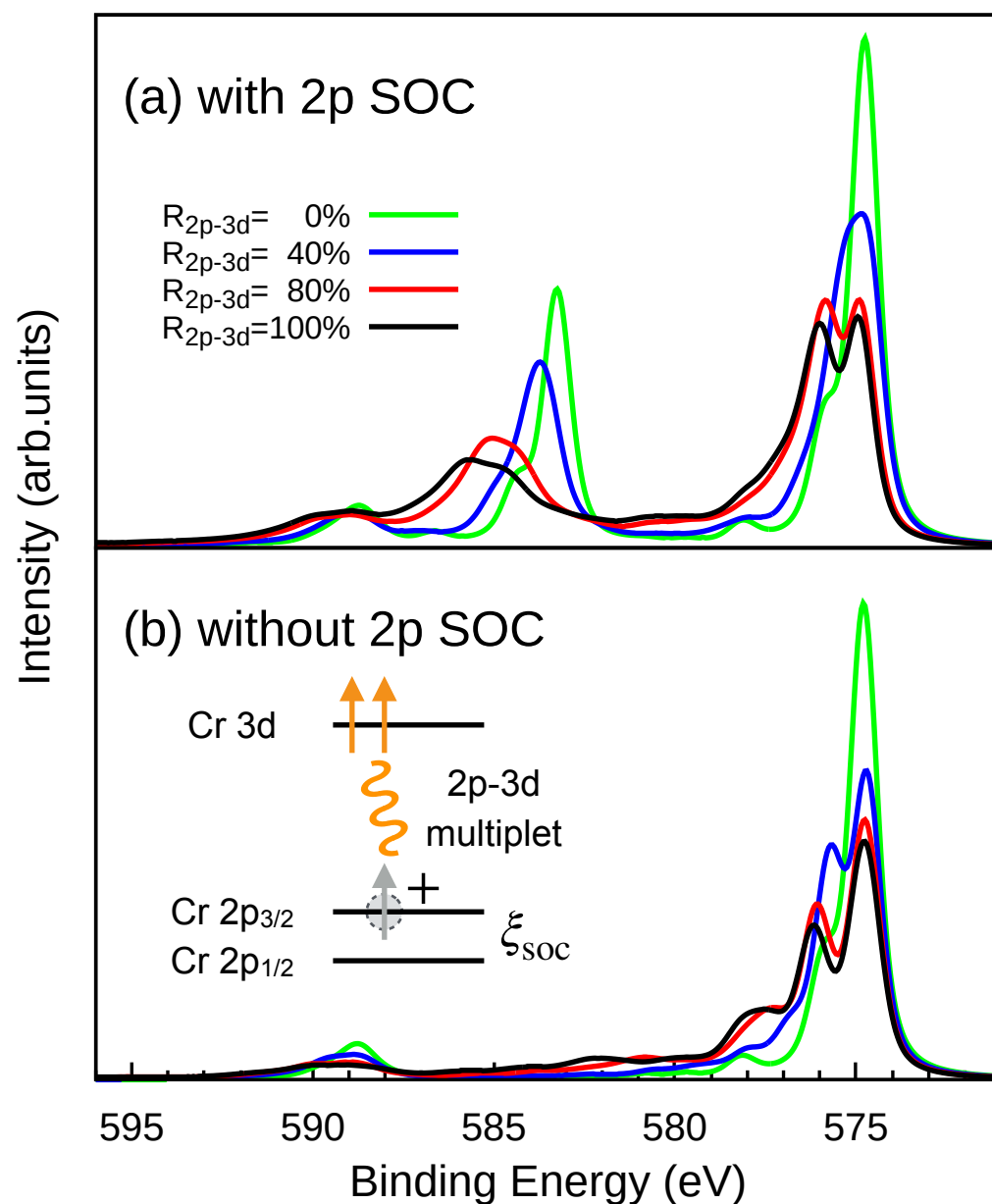
CrO₂ : Very different 1s and 2p line shape → Why not replica ??

2) Absence of Core-Valence Multiplet

T. Yamaguchi, AH, et al.,
Phys. Rev. B **109**, 205143 (2024)

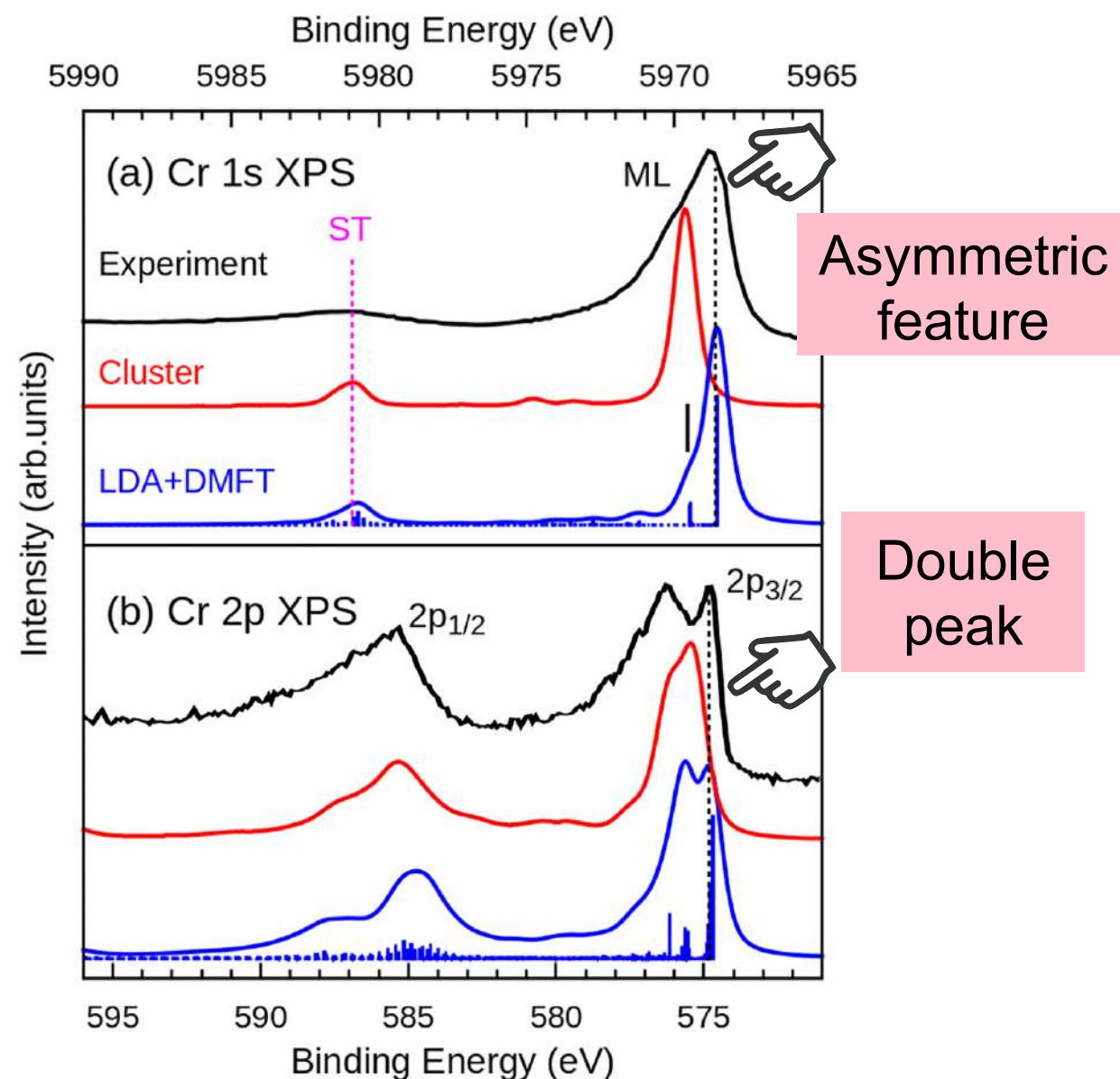
Calc. 2p-3d multiplet dependence

(Modify LDA+DMFT AIM Hamiltonian)



Cr 1s and 2p HAXPES in CrO₂

Cr 2p data: M. Sperlich et al., Phys. Rev. B **87**, 235138 (2013)

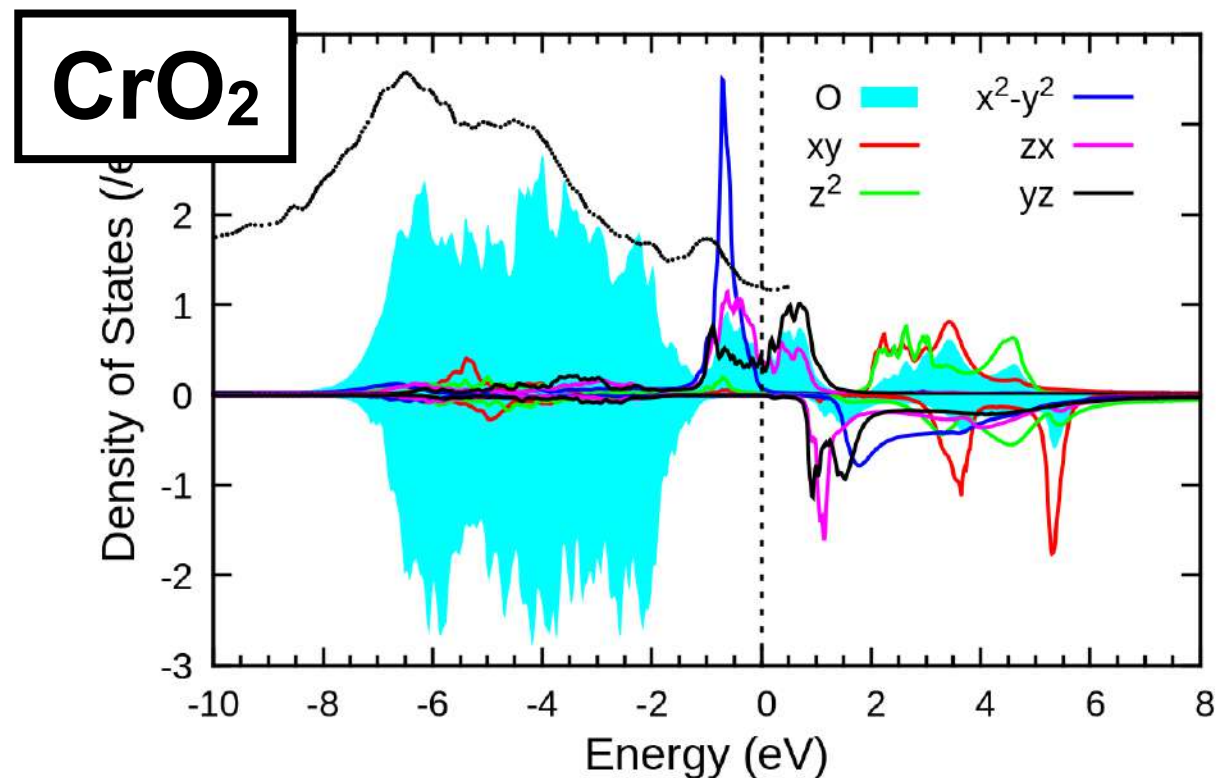


1s HAXPES is suited for studying charge transfer excitations,
when the core-valence multiplet is substantial (Cr, Fe, Mn ...)

2) Absence of Core-Valence Multiplet

T. Yamaguchi, AH, et al.,
Phys. Rev. B **109**, 205143 (2024)

Exp. M. Sperlich et al., Phys. Rev. B **87**, 235138 (2013)



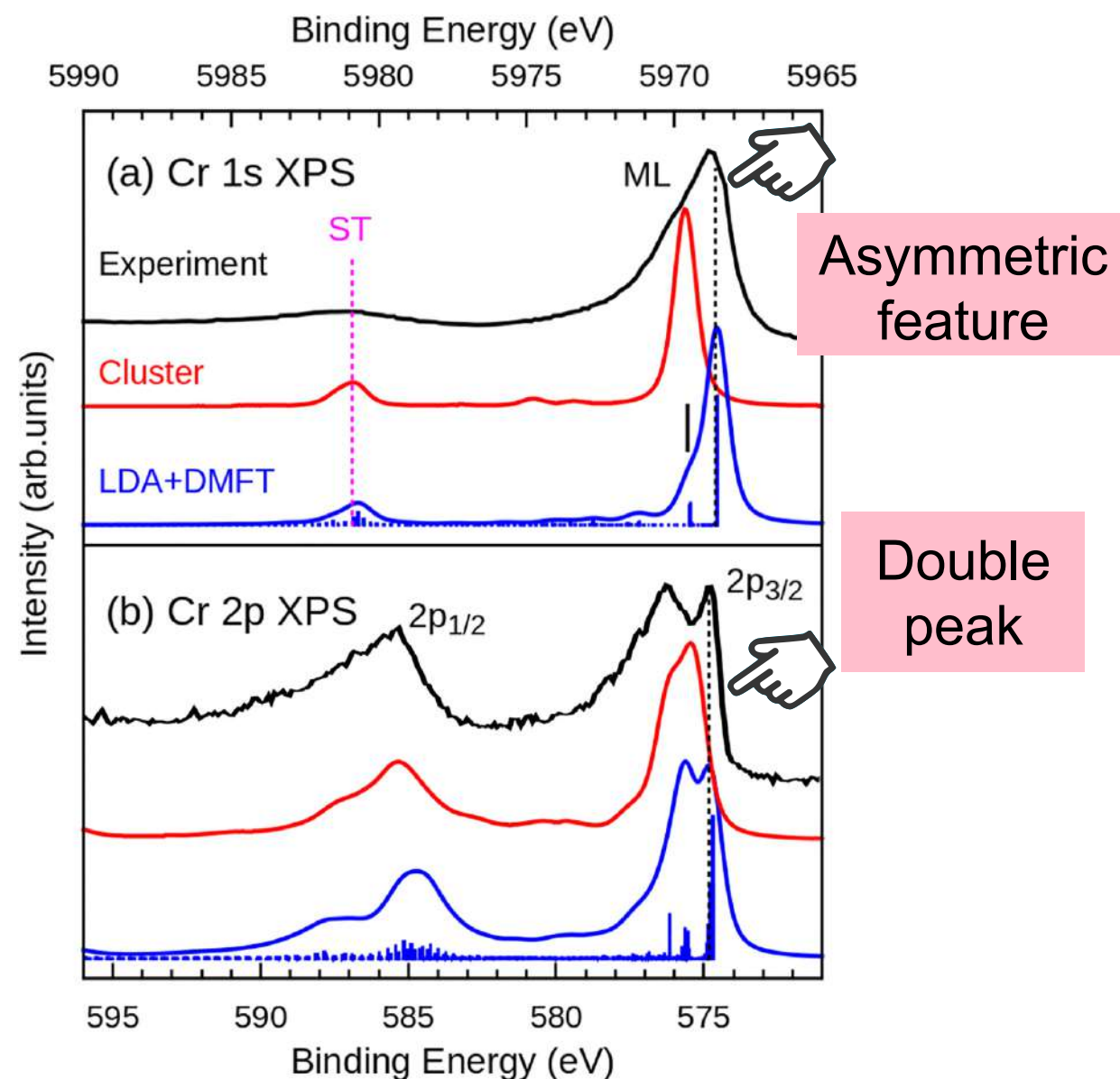
 **Main peak: Metallic screening**



Tail : Local ligand screening

Cr 1s and 2p HAXPES in CrO₂

Cr 2p data: M. Sperlich et al., Phys. Rev. B **87**, 235138 (2013)



**1s HAXPES is suited for studying charge transfer excitations,
when the 2p core-valence multiplet is effective (Cr, Fe, Mn ...)**

Table of contents

1. Core-level X-ray spectroscopy and DFT-based embedding approach

★ **Method.** DFT+ dynamical mean-field theory (DMFT)

A. Hariki, T. Uozumi, and J. Kuneš, Phys. Rev. B **96**, 045111 (2017)

A. Hariki, M. Winder, and J. Kuneš, Phys. Rev. Lett. **121**, 126403 (2018)

A. Hariki, M. Winder, T. Uozumi, and J. Kuneš, Phys. Rev. B **101**, 115130 (2020)

2. Application to various optical processes and compounds

★ **Excitations.** XPS, **XAS**, RIXS ★ **Materials.** *d*, *f* electron systems

★ **Physics.** Magnetism, valence structure, elementary excitations

K. Higashi, M. Winder, J. Kuneš, and A. Hariki, Phys. Rev. X **11**, 041009 (2021)

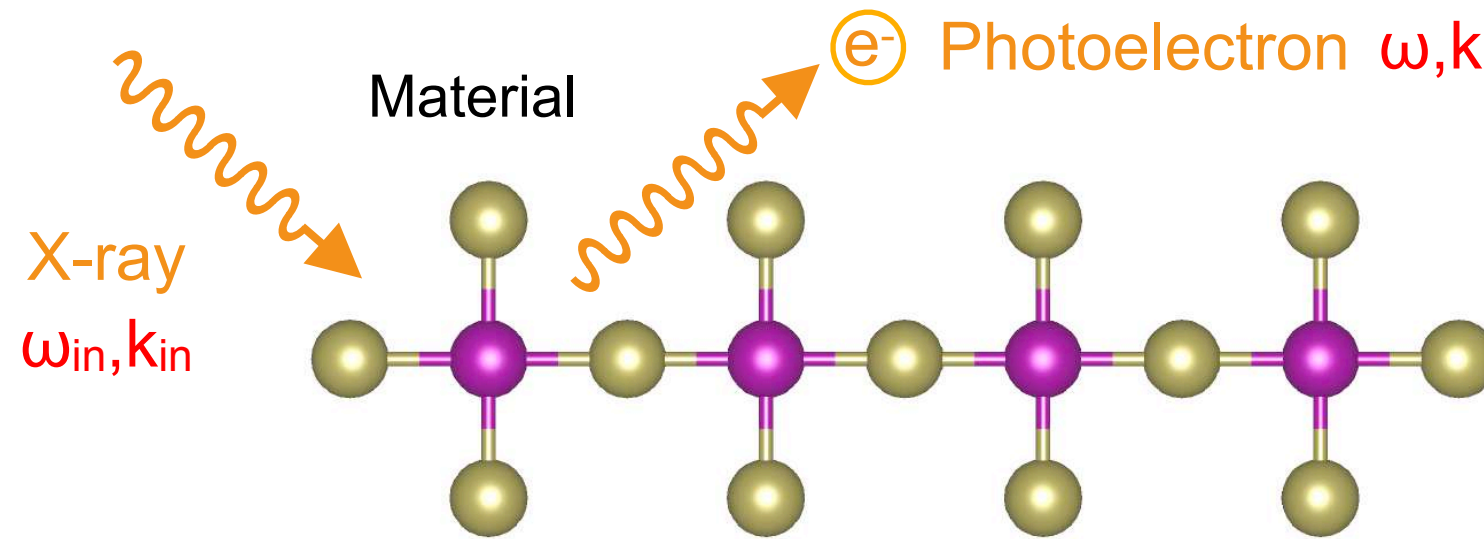
D. Takegami, A. Hariki et al., Phys. Rev. X **12**, 011017 (2022)

M. C. Rahn, K. Kummer, A. Hariki, et al., Nat. Commun. **13**, 6129 (2022)

J. Li, A. Hariki et al., Phys. Rev. X **13**, 011012 (2023)

A. Hariki et al., Phys. Rev. Lett. **132**, 176701 (2024)

Core-level x-ray absorption spectroscopy



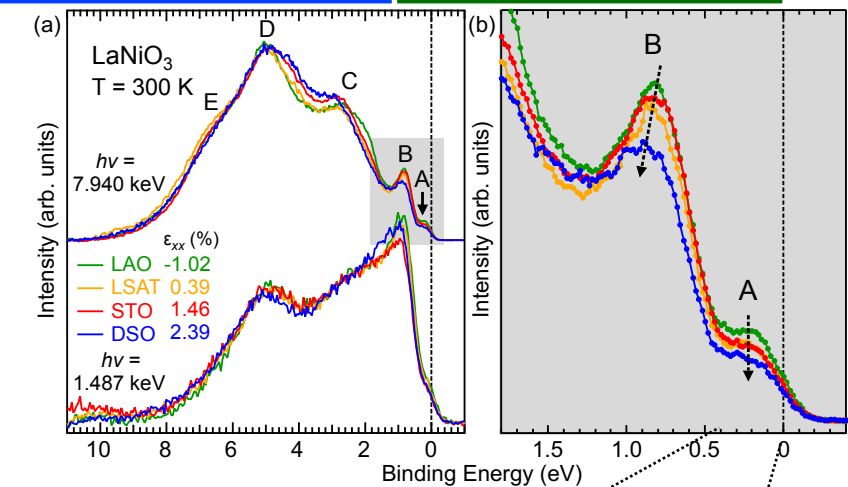
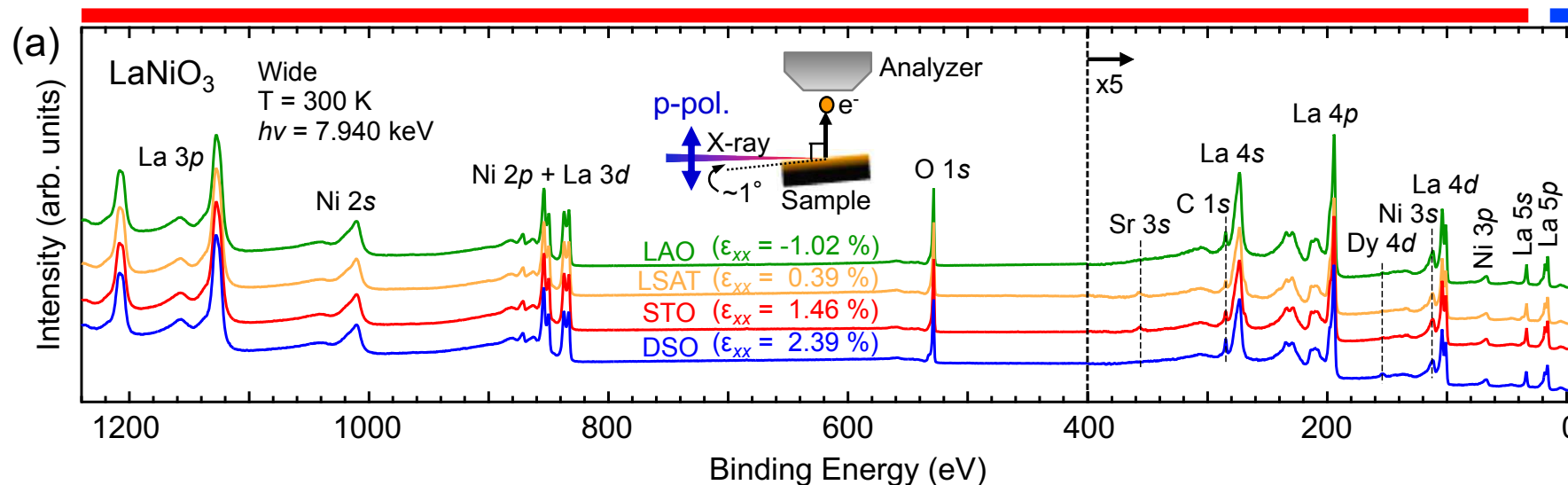
X-ray photoemission spectroscopy:

- Valence-band XPS (ARPES)
directly measure the low-energy states
- Core-level XPS
Site/element specific excitation

XPS spectrum in LaNiO_3 K. Yamagami et al., Appl. Phys. Lett. 118, 161601 (2021)

Core levels

Valence bands Near Fermi (QP)



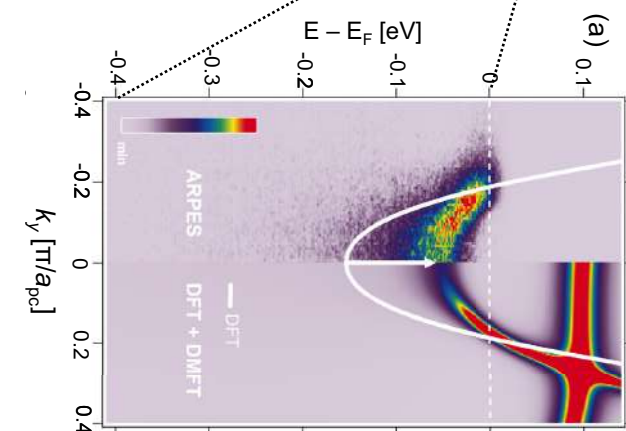
Core levels (no momentum dependence)

Core electrons (holes) completely localized at each ion

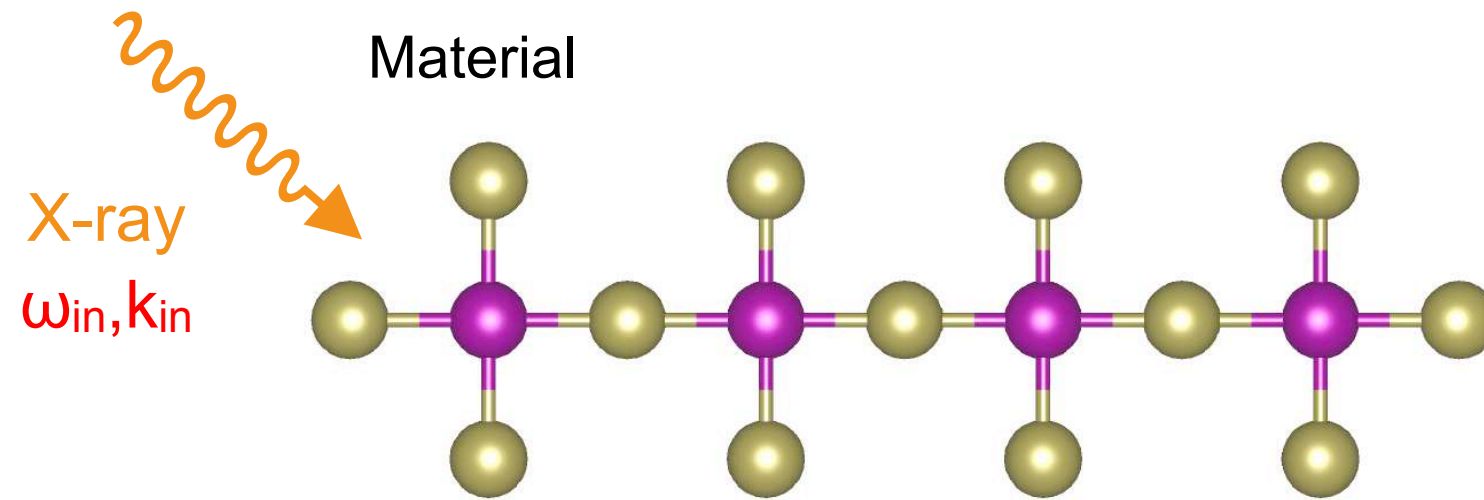
- Element specific information (valency)
- Local electronic structure
(Hund's multiplet, crystal field, and more ...)

ARPES: resolve the momentum

E. A. Nowadnick et al.,
Phys. Rev. B **92**, 245109 (2015)



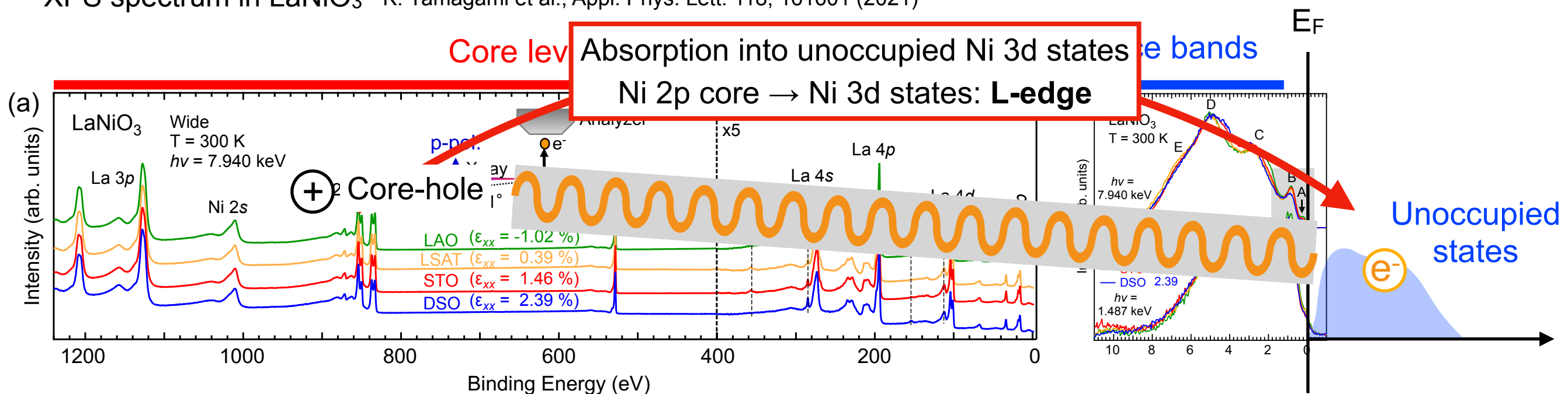
Core-level x-ray absorption spectroscopy



X-ray photoemission spectroscopy:

- Valence-band XPS (ARPES)
directly measure the low-energy states
- Core-level XPS
Site/element specific excitation

XPS spectrum in LaNiO_3 K. Yamagami et al., Appl. Phys. Lett. 118, 161601 (2021)



1-particle
Green's function

$$G_r(\epsilon) =$$

Eigen state with a "core-hole"

$$\langle \Phi_0^{(N)} | c_r \frac{1}{\epsilon - (E_0^{(N)} - \mathcal{H}) + i\delta} c_r^\dagger | \Phi_0^{(N)} \rangle$$

$$\langle \Phi_0^{(N)} | c_r \frac{1}{\epsilon - (\mathcal{H} - E_0^{(N)}) + i\delta} c_r^\dagger | \Phi_0^{(N)} \rangle$$

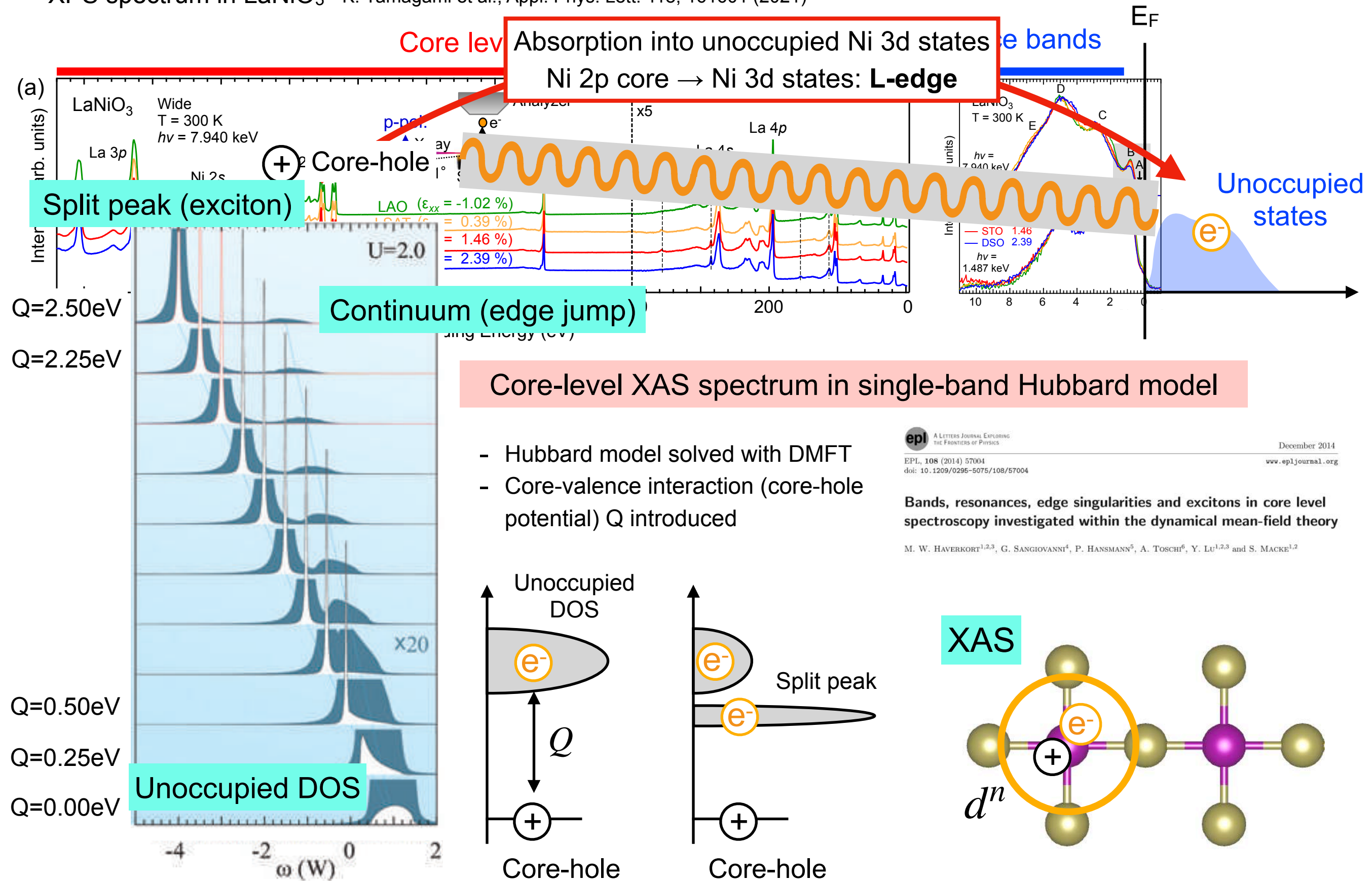
photoemission

$$= \sum_n \left[\frac{|\langle \Phi_n^{(N-1)} | c_r | \Phi_0^{(N)} \rangle|^2}{\epsilon - (E_0^{(N)} - E_n^{(N-1)}) + i\delta} + \frac{|\langle \Phi_n^{(N+1)} | c_r^\dagger | \Phi_0^{(N)} \rangle|^2}{\epsilon - (E_n^{(N+1)} - E_0^{(N)}) + i\delta} \right]$$

Inverse photoemission

Core-level x-ray absorption spectroscopy

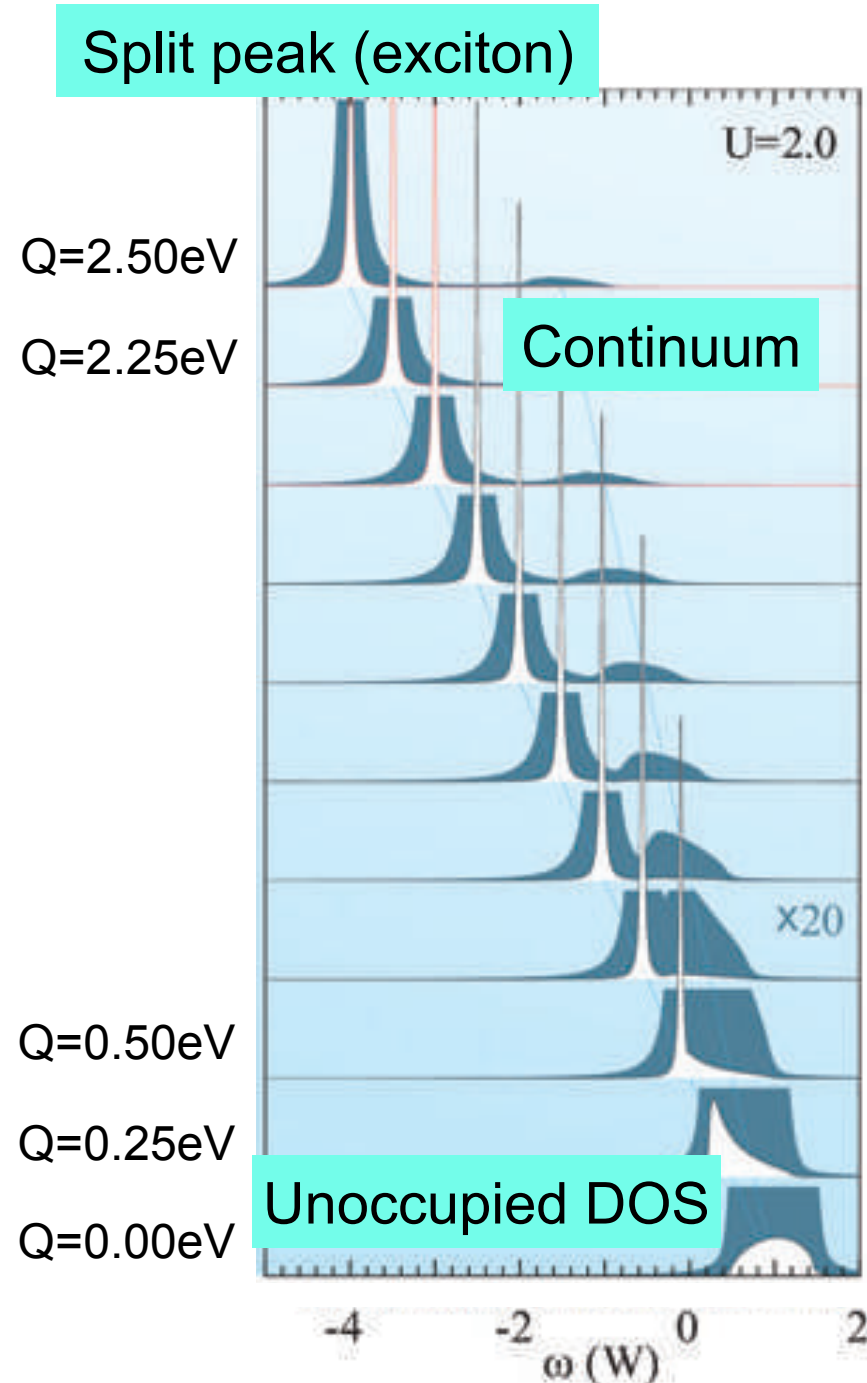
XPS spectrum in LaNiO_3 K. Yamagami et al., Appl. Phys. Lett. 118, 161601 (2021)



Core-level x-ray absorption spectroscopy

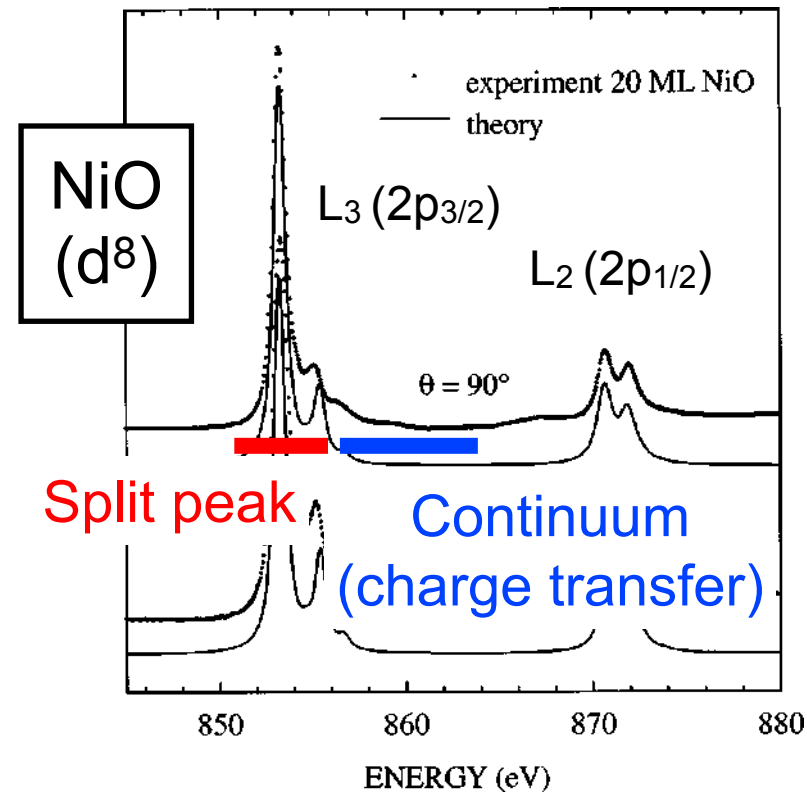
Single-band Hubbard model

M. W. Haverkort et al., EPL **108**, 57004 (2014)

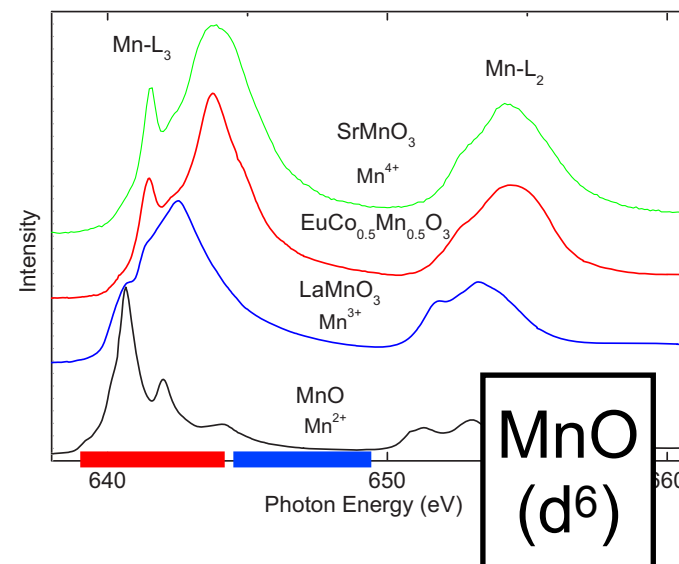
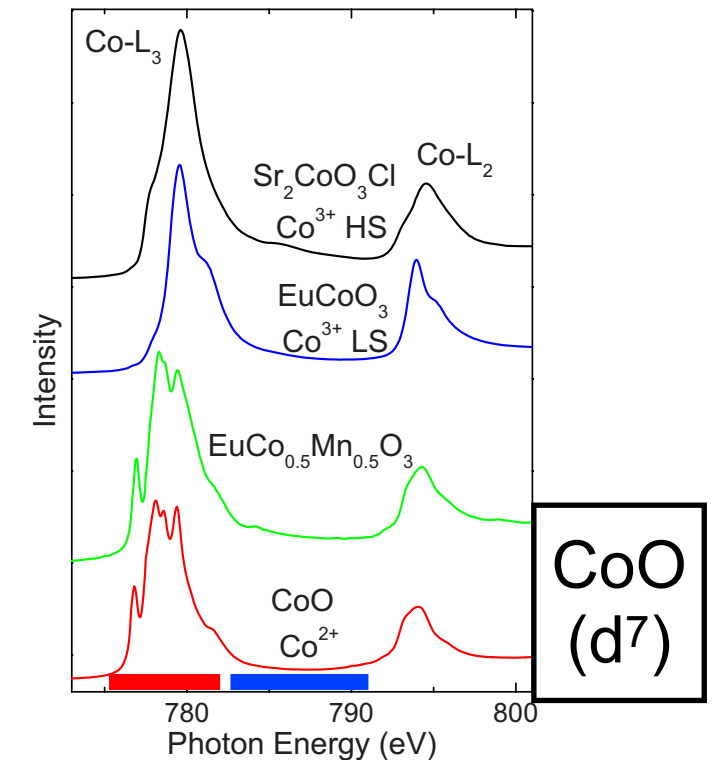


Correlated materials (Mott insulators)

D. Alders et al., PRB **57**, 11623 (1998)



A. N. Vasiliev et al., PRB **77**, 10442 (2008)



Rich inner features in the split peak, sensitive to valency, local crystal structure, spin (magnetic) states etc..

Core-level x-ray absorption spectroscopy

The main peak/part (split, excitonic) in localized electron systems can be well captured by ionic (atomic) model with a core-hole

PHYSICAL REVIEW B

VOLUME 42, NUMBER 9

15 SEPTEMBER 1990-II

2p x-ray absorption of 3d transition-metal compounds: An atomic multiplet description including the crystal field

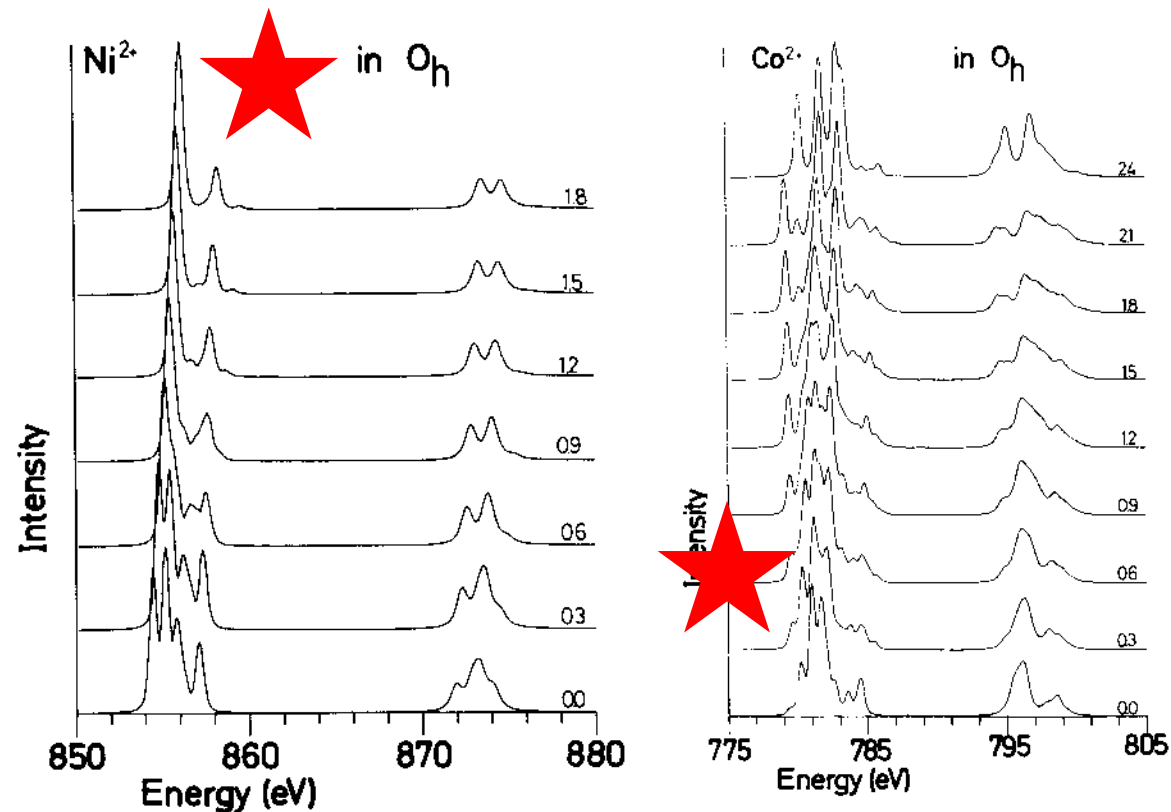
F. M. F. de Groot and J. C. Fuggle

Research Institute for Materials, University of Nijmegen, Toernooiveld, 6525 ED Nijmegen, The Netherlands

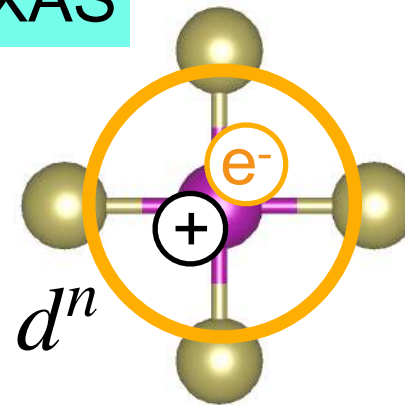
B. T. Thole and G. A. Sawatzky

Materials Science Centre, University of Groningen, Nijenborgh 18, Paddepoel, 9747 AG Groningen, The Netherlands

(Received 30 January 1990; revised manuscript received 4 June 1990)

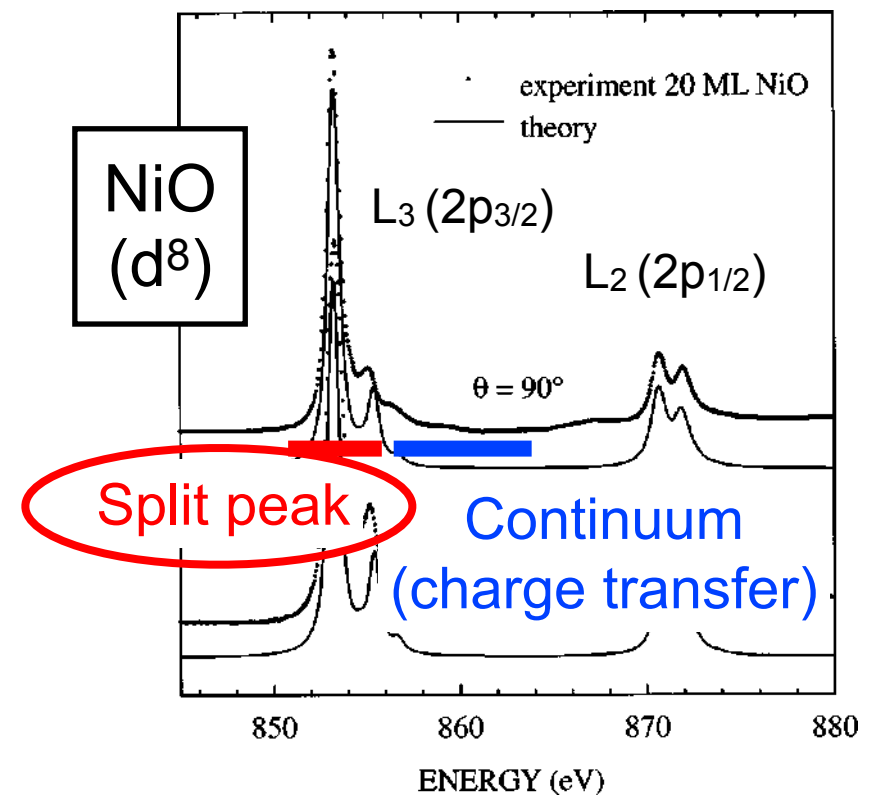


XAS

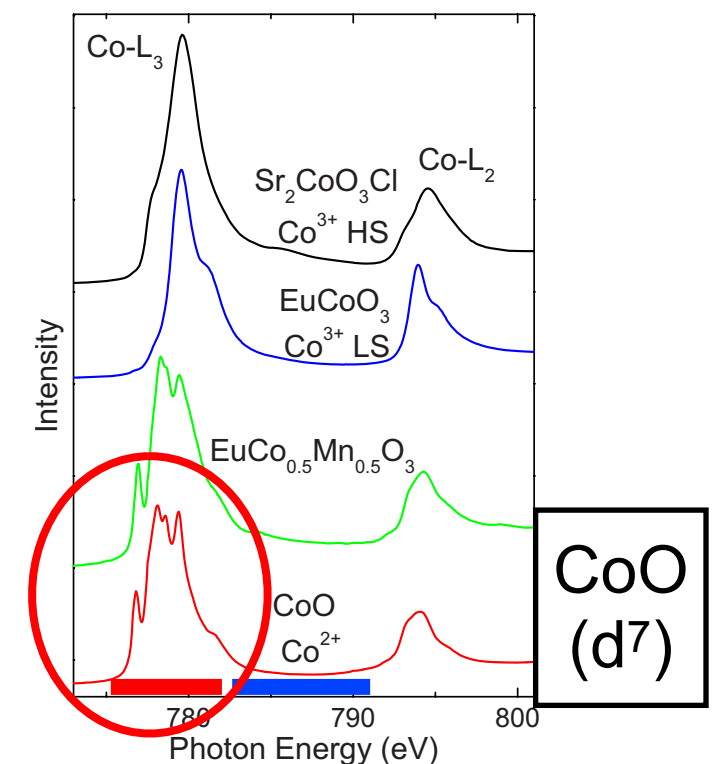


Multiplet
fine features
of excitons
(core hole + d^{n+1})

D. Alders et al., PRB **57**, 11623 (1998)

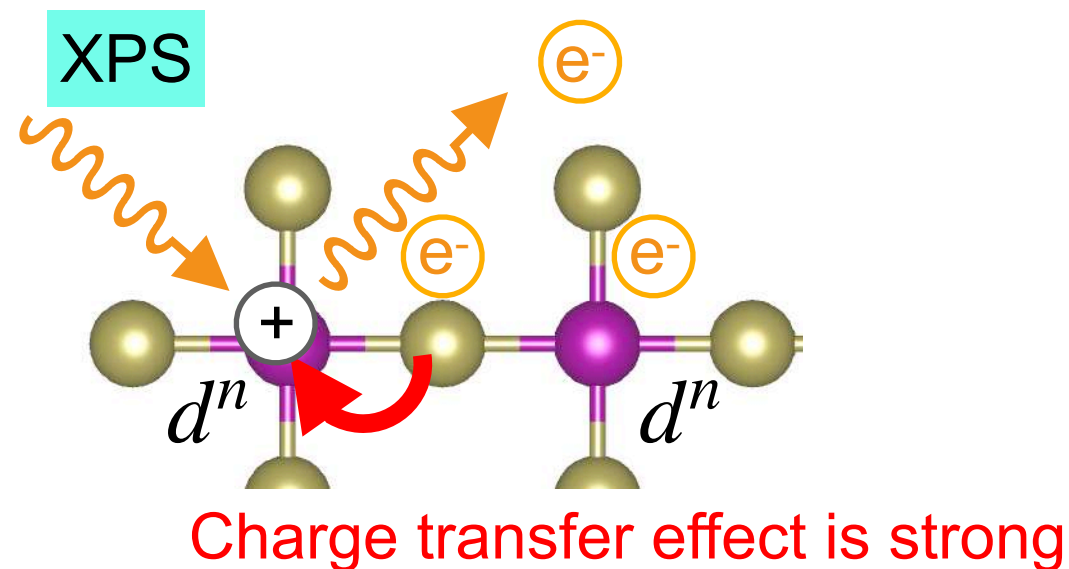
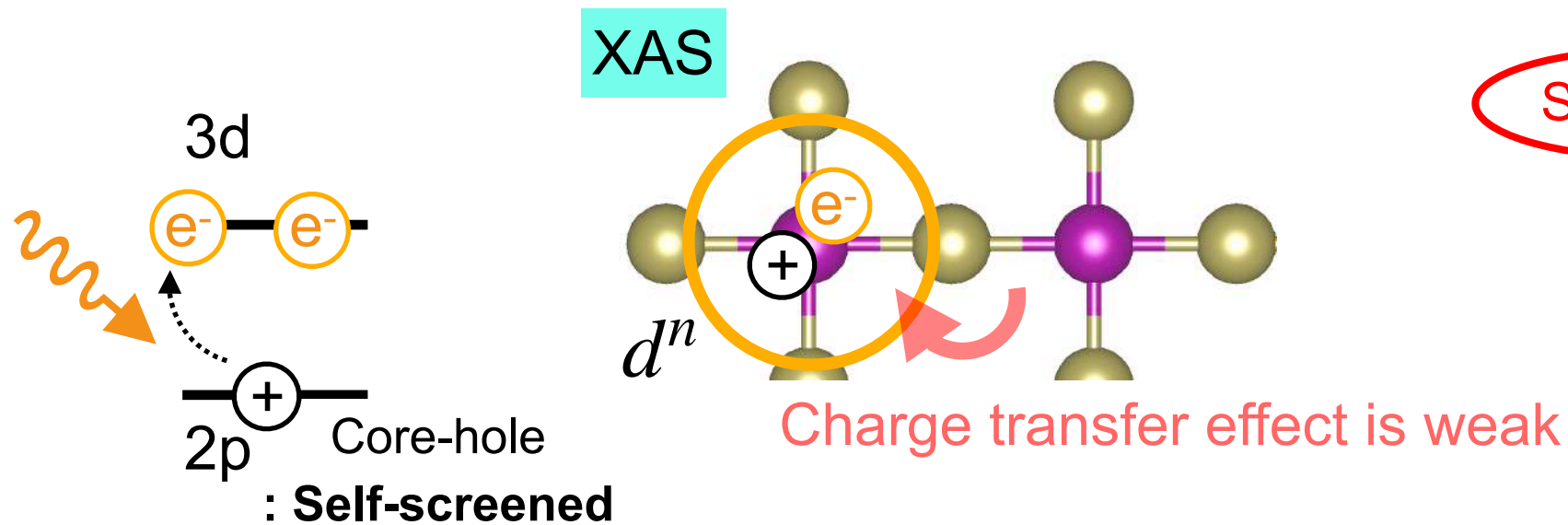


A. N. Vasiliev et al., PRB **77**, 10442 (2008)

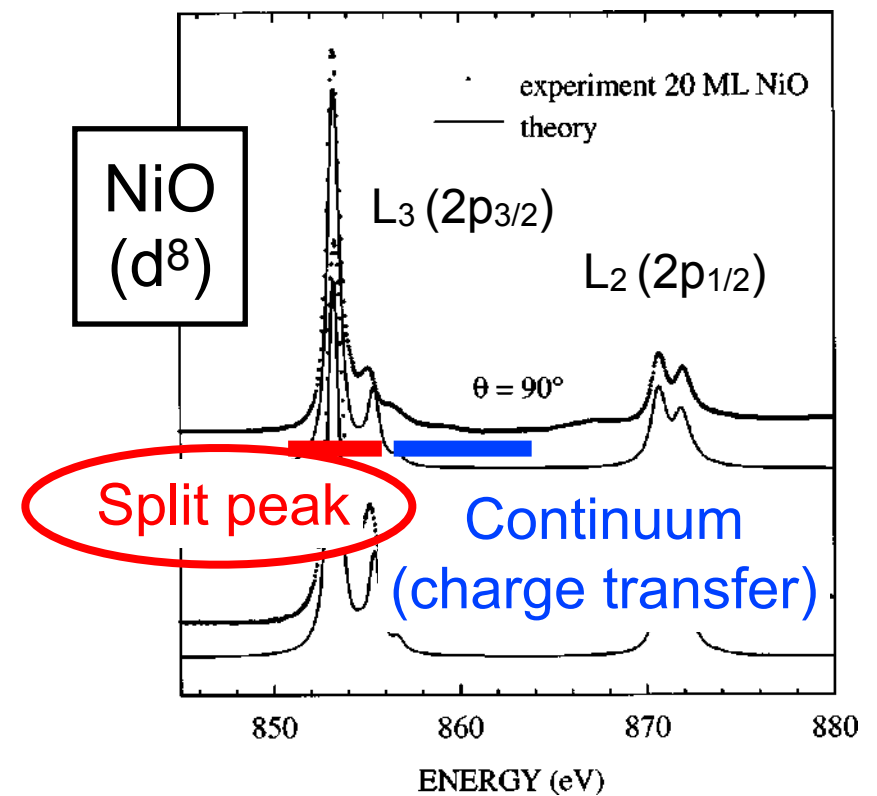


Core-level x-ray absorption spectroscopy

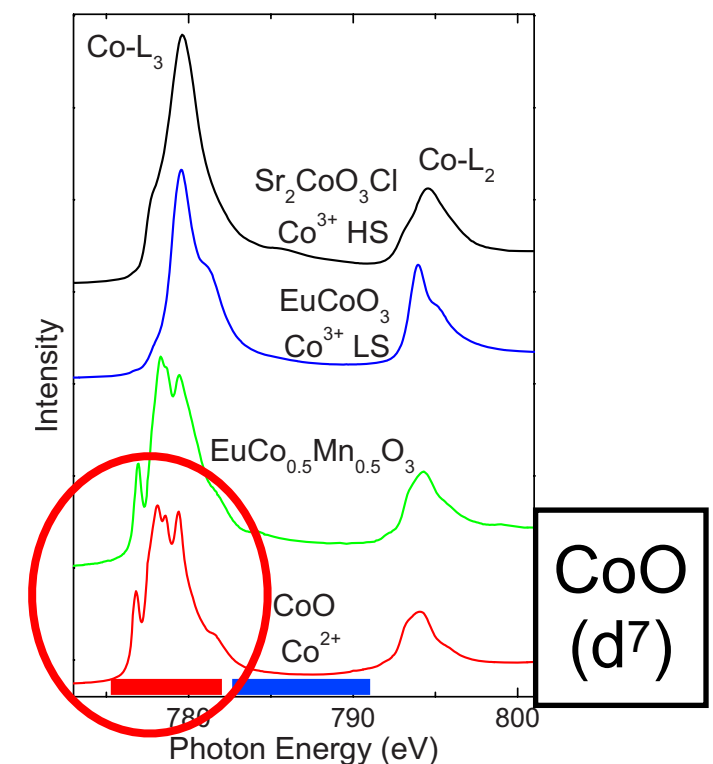
The main peak/part (split, excitonic) in localized electron systems can be well captured by ionic (atomic) model with a core-hole



D. Alders et al., PRB **57**, 11623 (1998)



A. N. Vasiliev et al., PRB **77**, 10442 (2008)



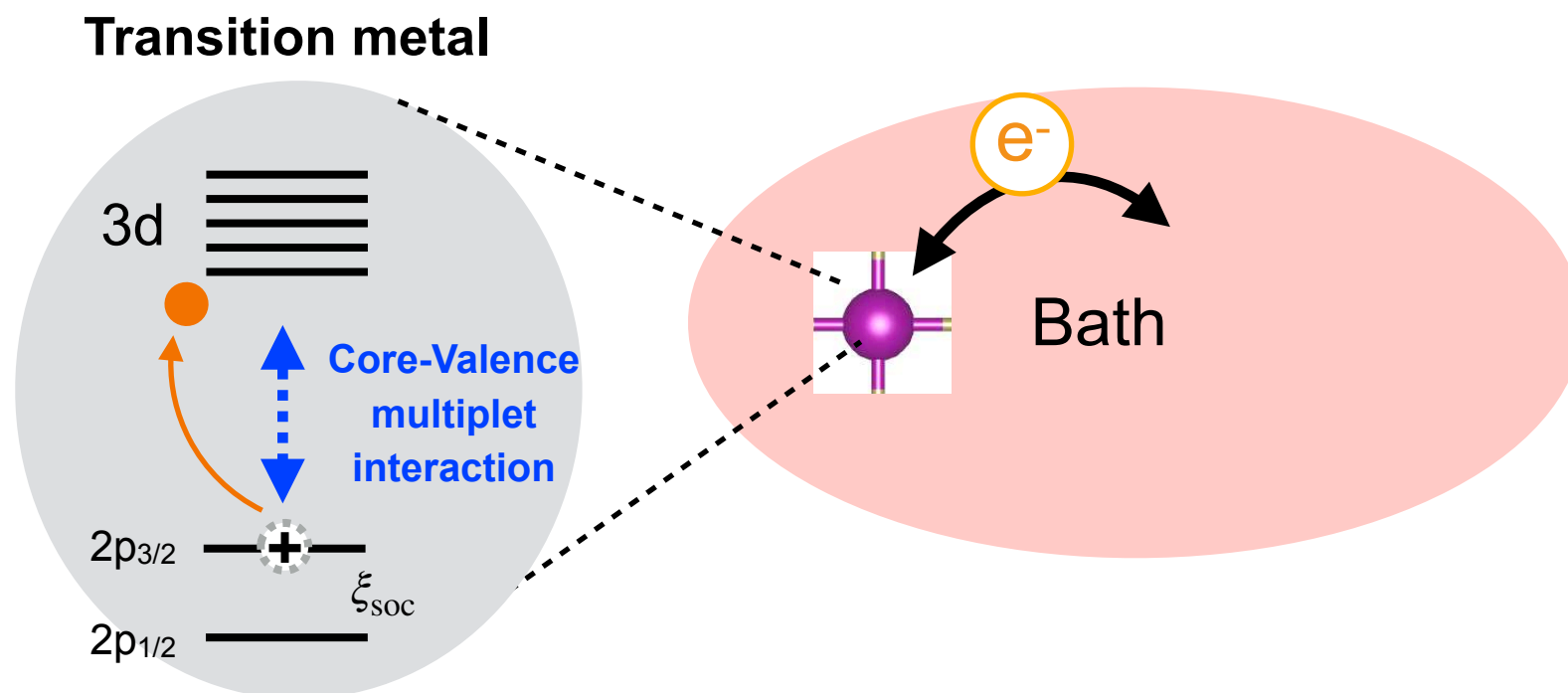
Core-level x-ray spectroscopies in solid

- ✓ Simpler DFT approach (DFT DOS + core-level) works for noninteracting (weakly correlated) systems

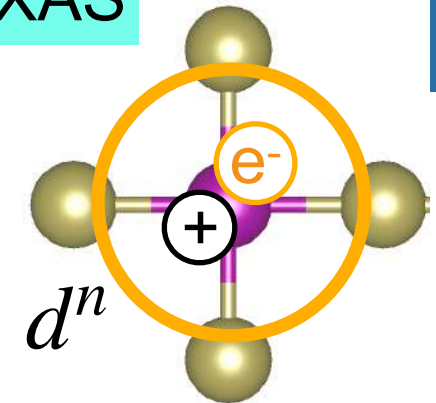
In intermediate or strong coupling regime

- In addition to the unoccupied bands above E_F
1. Local core-hole potential needs to be included
 2. Fine multiplet interaction needs to be described

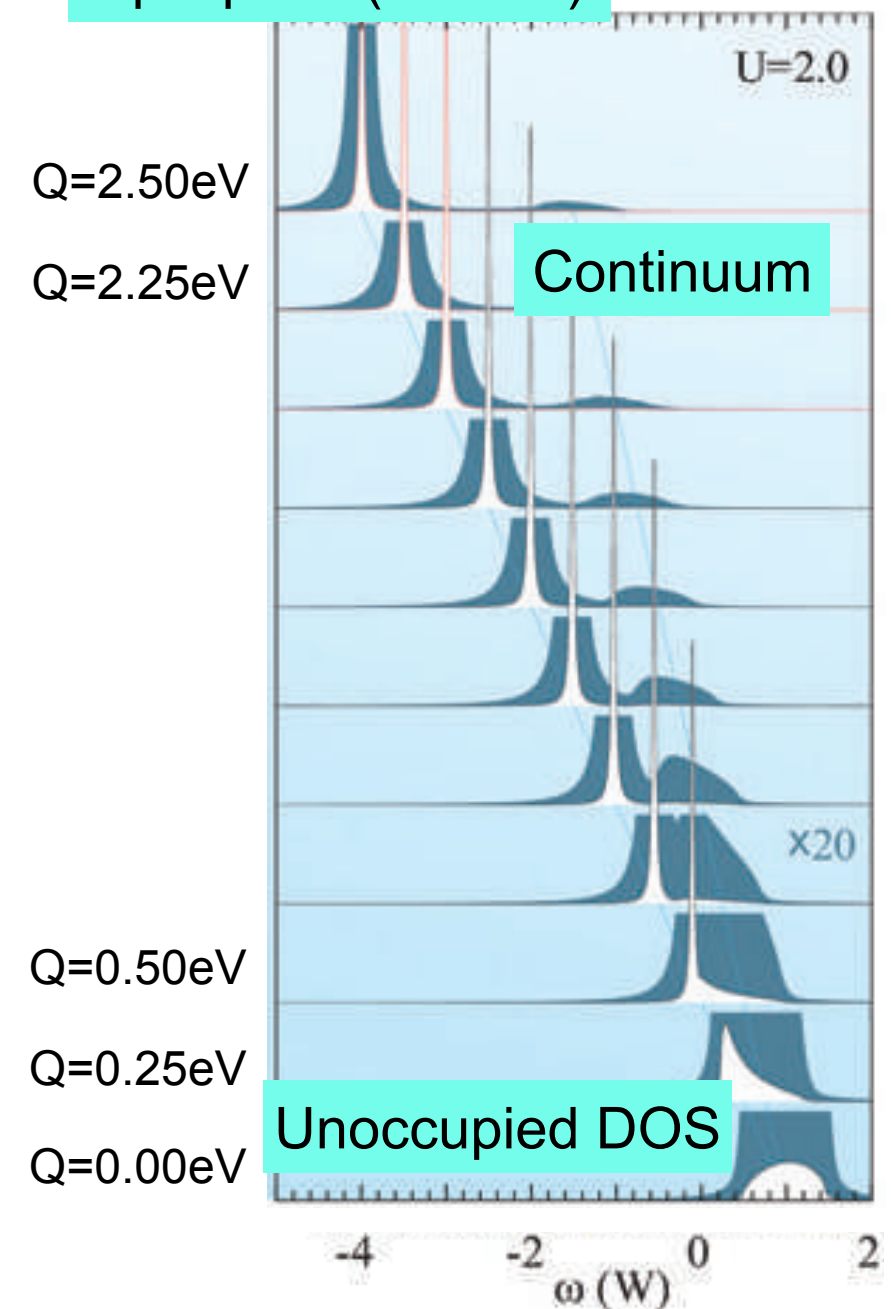
➔ **DFT+DMFT embedding approaches covers the two limits!**



XAS



Split peak (exciton)




LDA + DMFT approach to resonant inelastic x-ray scattering in correlated materials

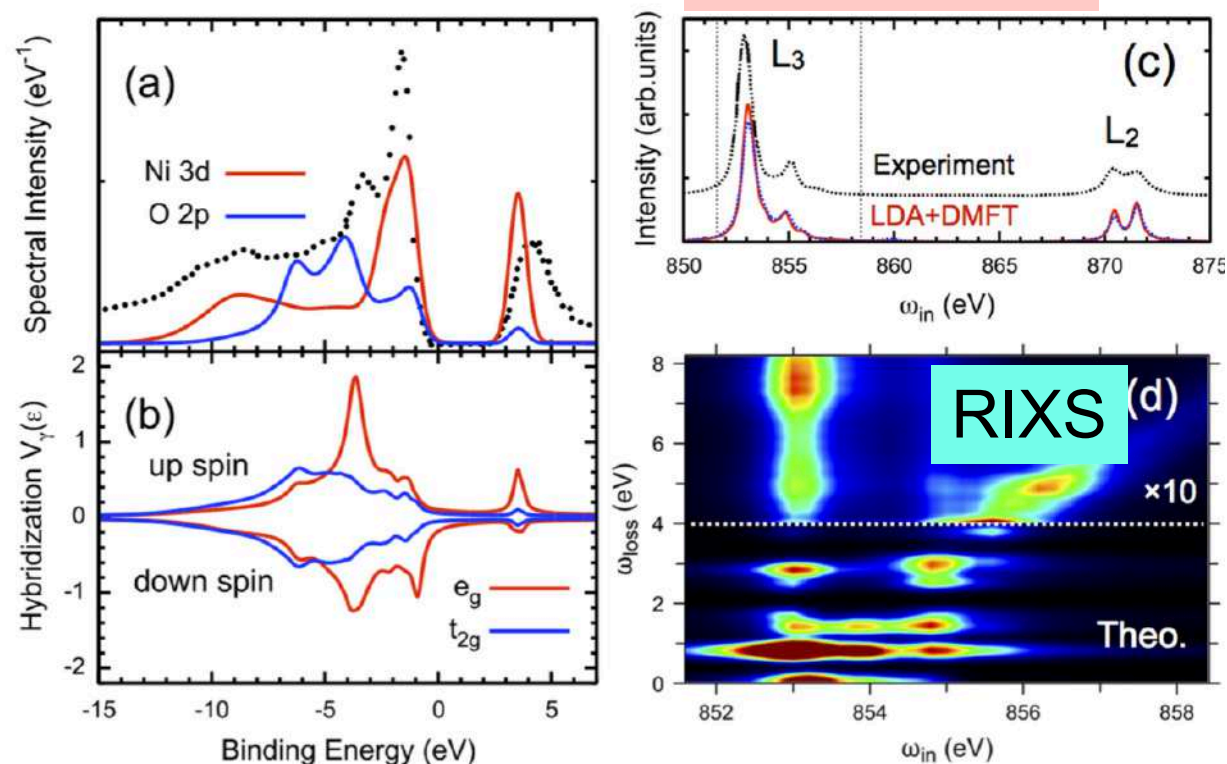
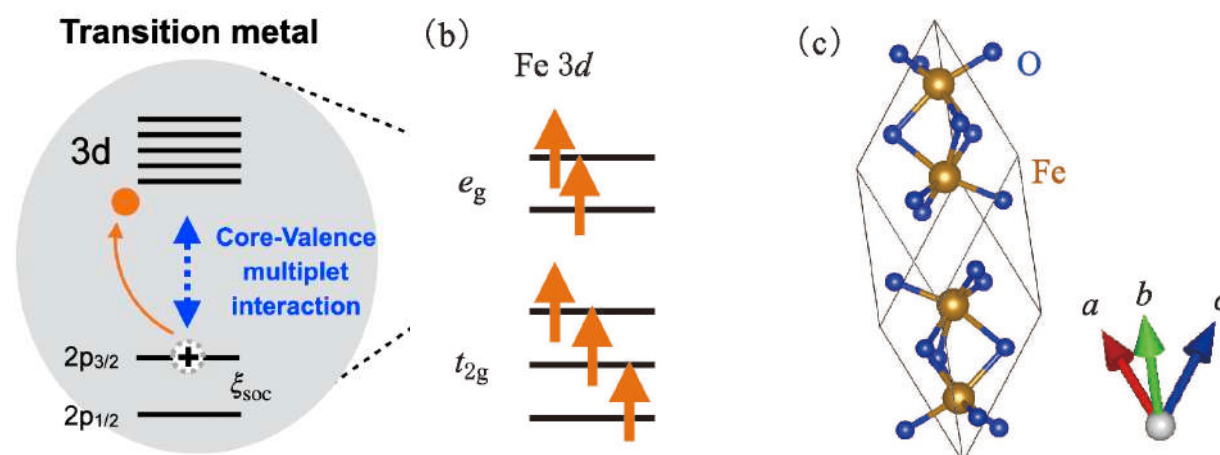
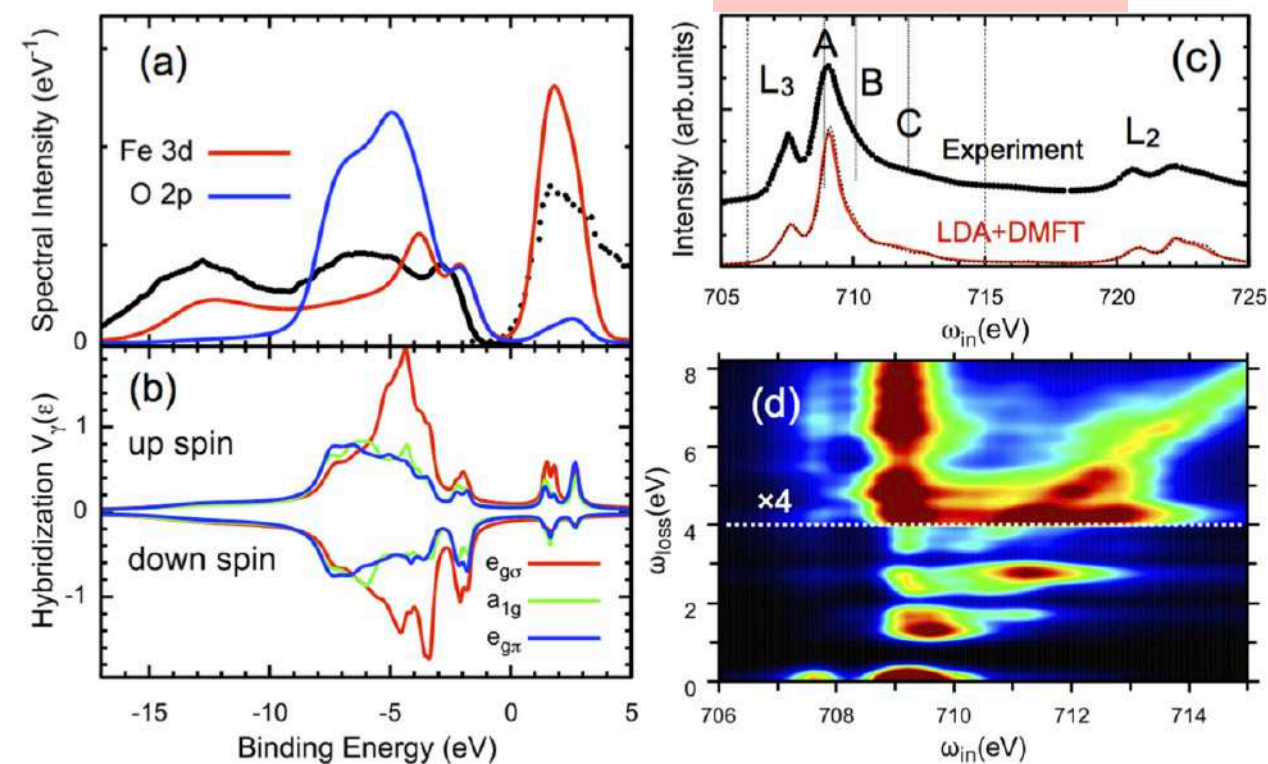
 Atsushi Hariki^{1,*}, Mathias Winder,^{1,*} Takayuki Uozumi,² and Jan Kuneš^{1,3}
¹*Institute of Solid State Physics, TU Wien, 1040 Vienna, Austria*
²*Department of Physics and Electronics, Graduate School of Engineering, Osaka Prefecture University 1-1 Gakuen-cho, Nakaku, Sakai, Osaka 599-8531, Japan*
³*Institute of Physics, Czech Academy of Sciences, Na Slovance 2, 182 21 Praha 8, Czechia*

(Received 30 November 2019; accepted 21 February 2020; published 18 March 2020)

解説

 共鳴非弾性 X 線散乱で見る
強相関電子系の励起スペクトル

大阪公立大学大学院工学研究科 播木 敦

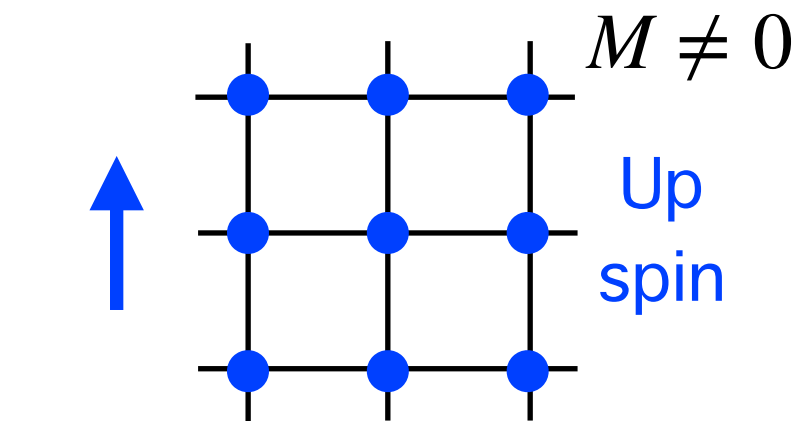
NiO
L-edge XAS

Fe₂O₃
L-edge XAS


What is Altermagnet?

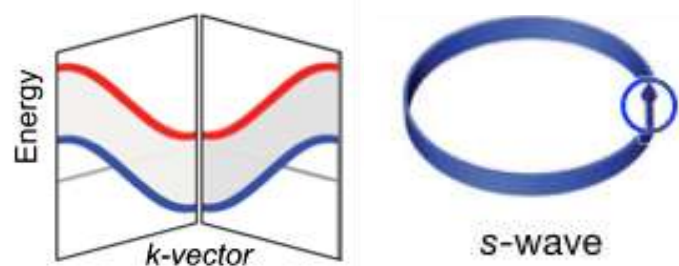
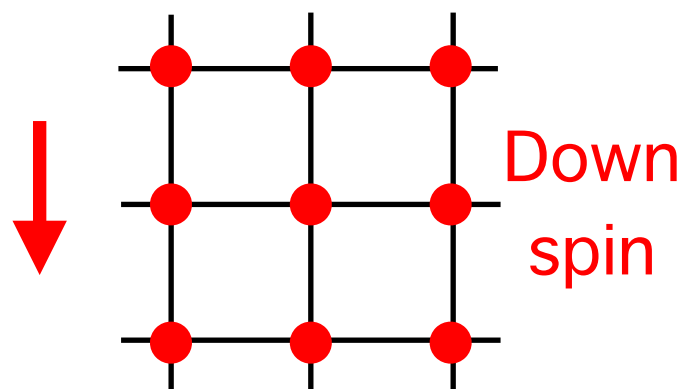
L. Šmejkal et al., Phys. Rev. X 12, 040501 (2022)

Altermagnet: a new class in collinear magnets (w/o spin-orbit coupling)

Ferromagnet

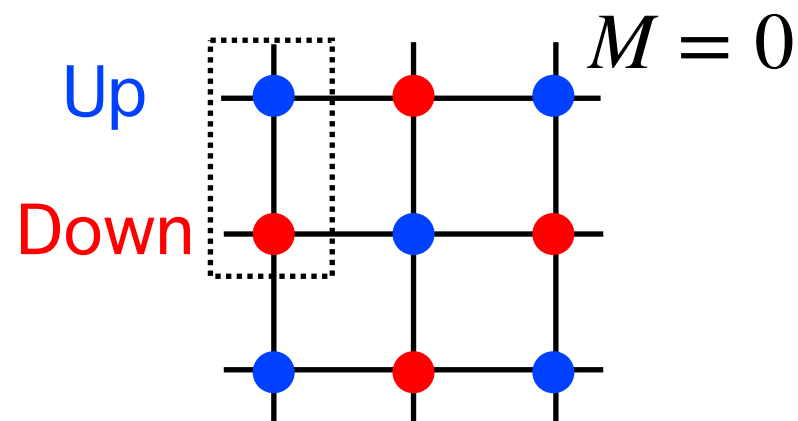


Time reversal $\mathcal{T}$  

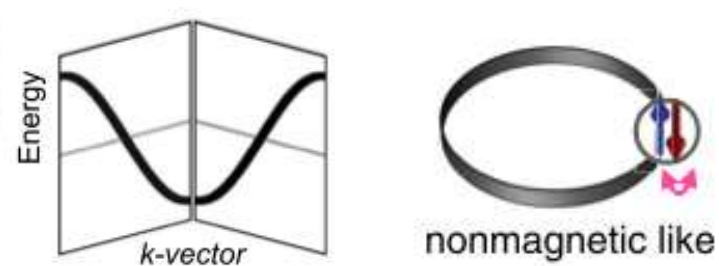
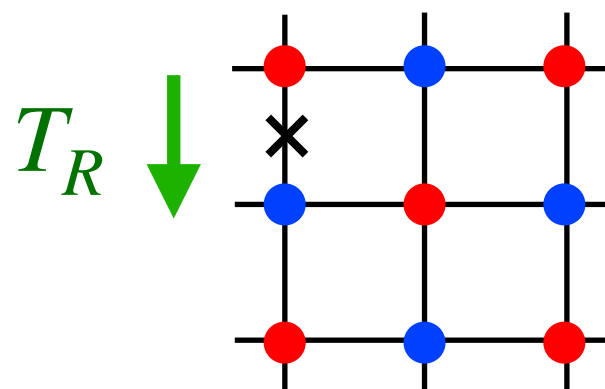


(Uniform) Zeeman splitting in band structure ($\mathcal{T}$ -broken)

Antiferromagnet

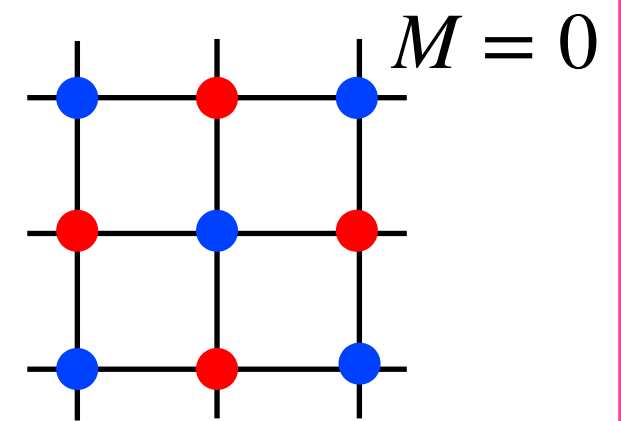


$\mathcal{T}$   T_R, P

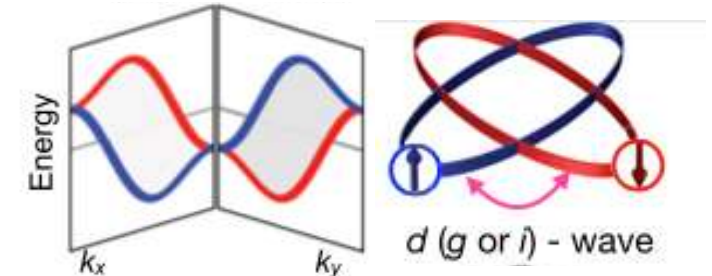
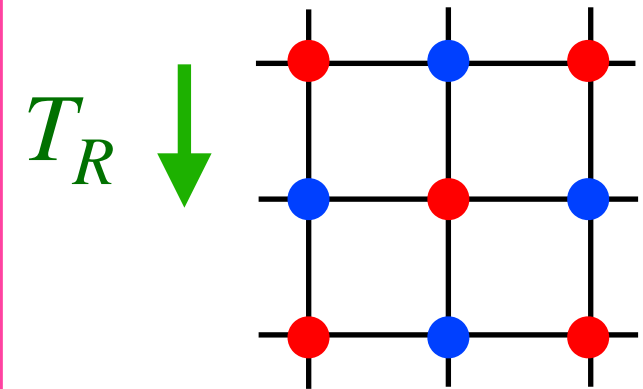


Spin degenerated bands (with $\mathcal{T}$ symmetry)

Altermagnet



$\mathcal{T}$  



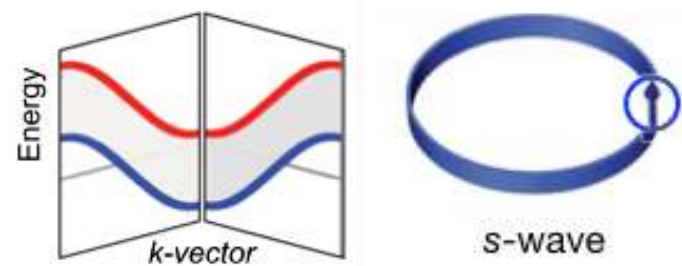
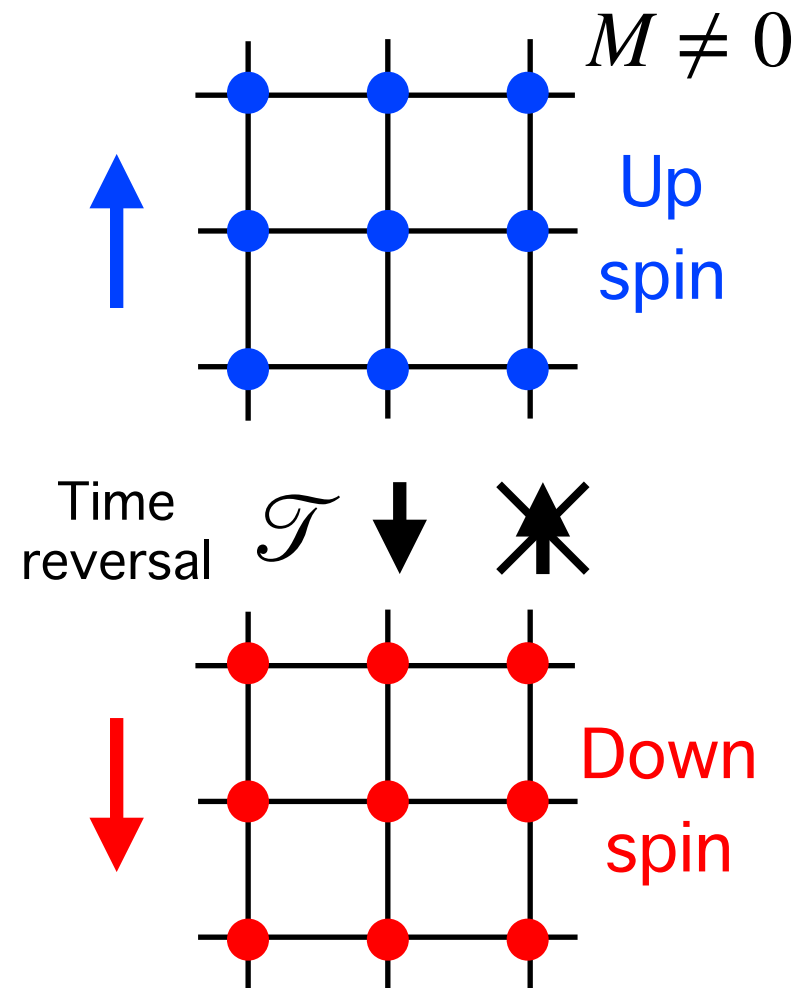
$\mathcal{T}$ -broken bands with d/g/i-wave spin texture

What is Altermagnet?

L. Šmejkal et al., Phys. Rev. X 12, 040501 (2022)

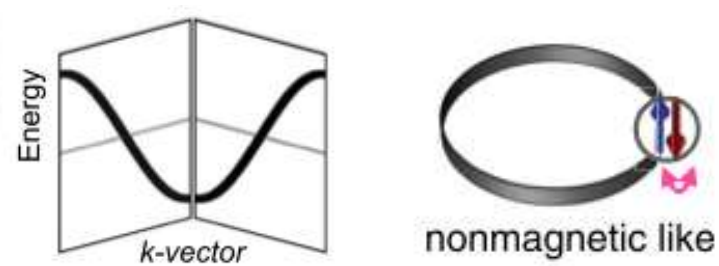
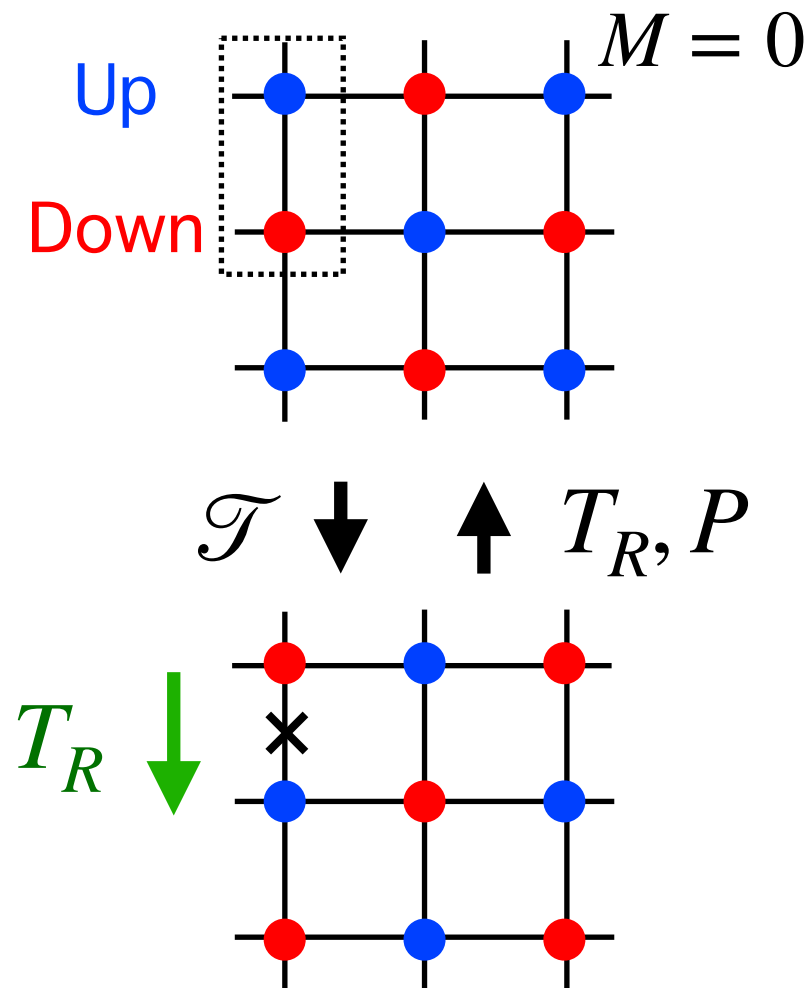
Altermagnet: a new class in collinear magnets, split from antiferromagnets

Ferromagnet



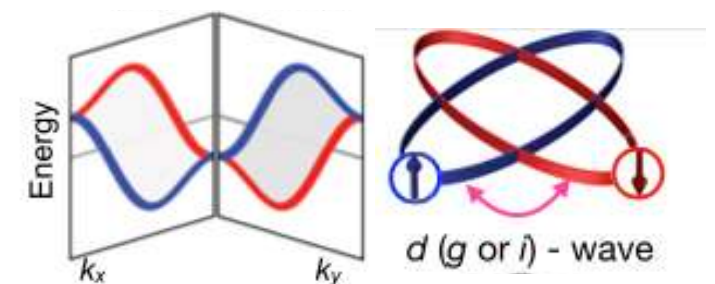
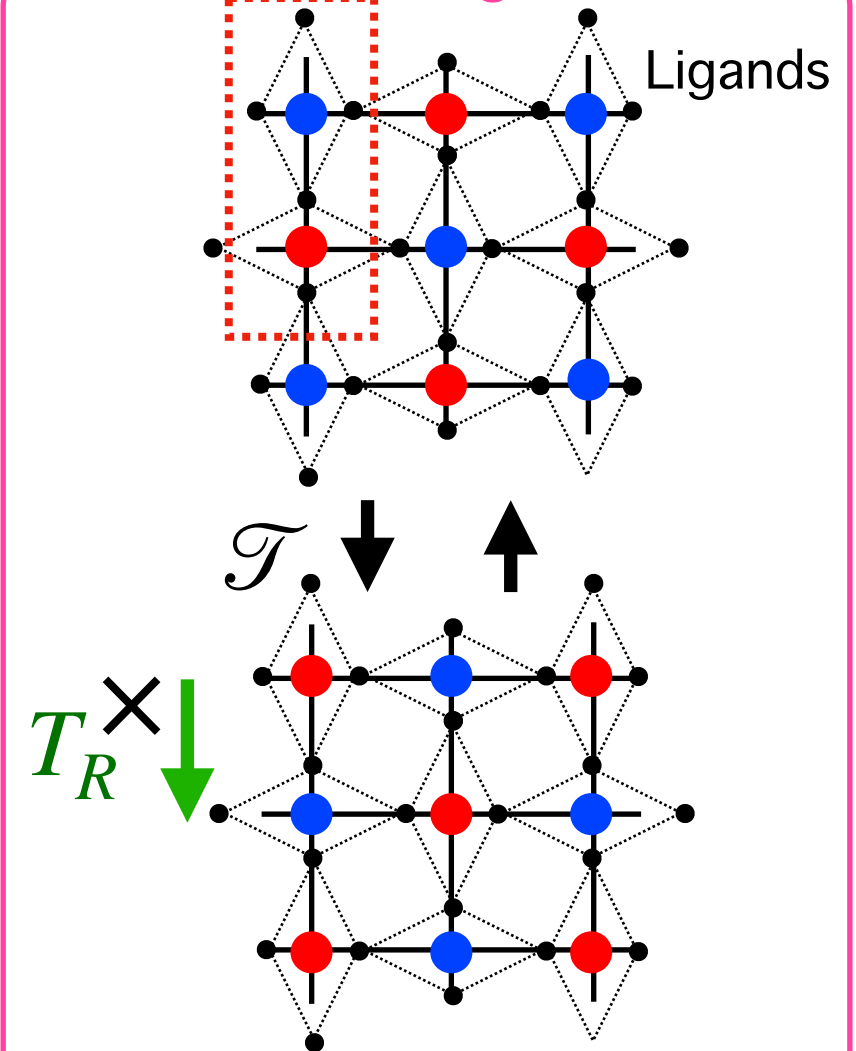
(Uniform) Zeeman splitting in band structure ($\mathcal{T}$ -broken)

Antiferromagnet



Spin degenerated bands (with $\mathcal{T}$ symmetry)

Altermagnet



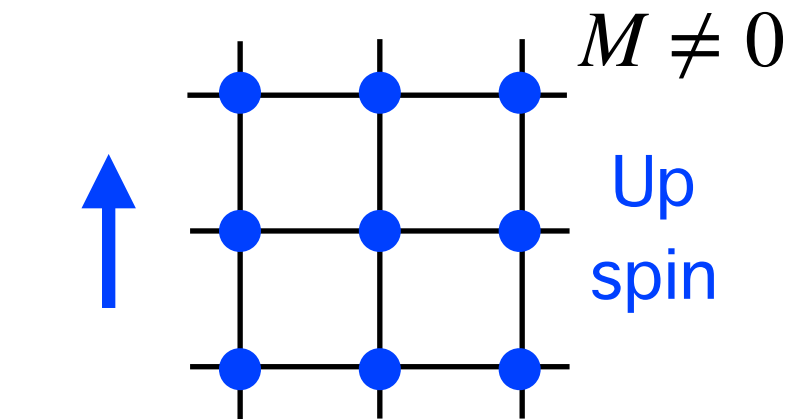
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What is Altermagnet?

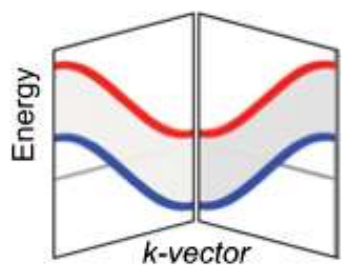
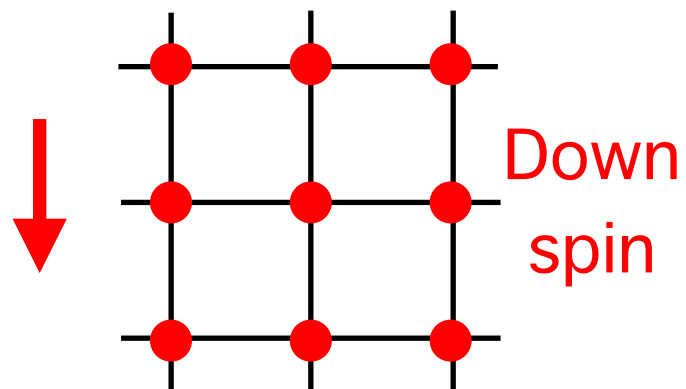
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Altermagnet: a new class in collinear magnets, split from antiferromagnets

Ferromagnet

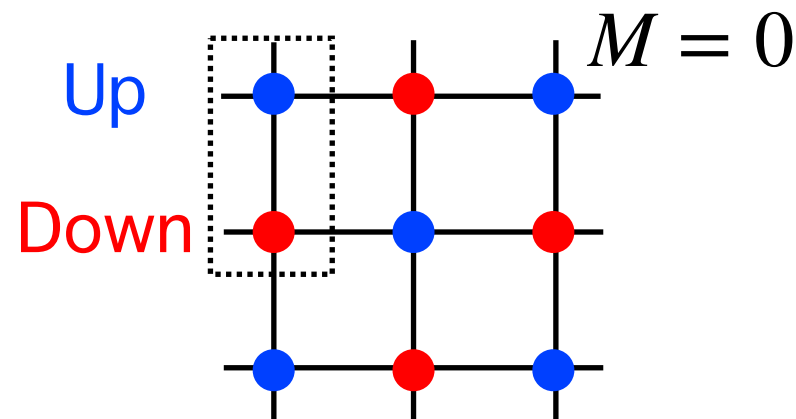


Time reversal $\mathcal{T}$ ↓ ✗

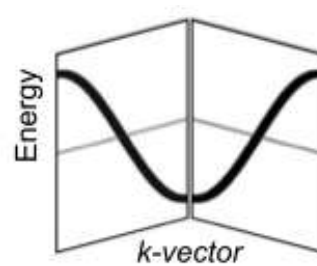
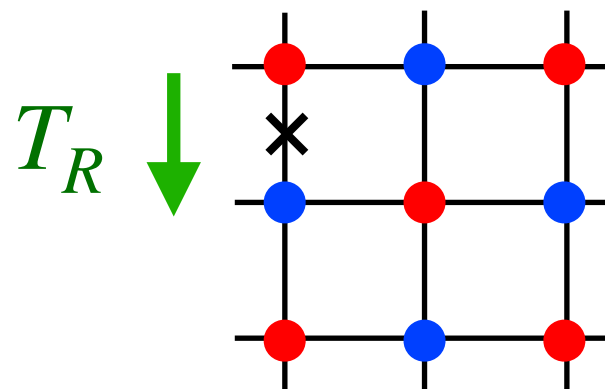


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Antiferromagnet

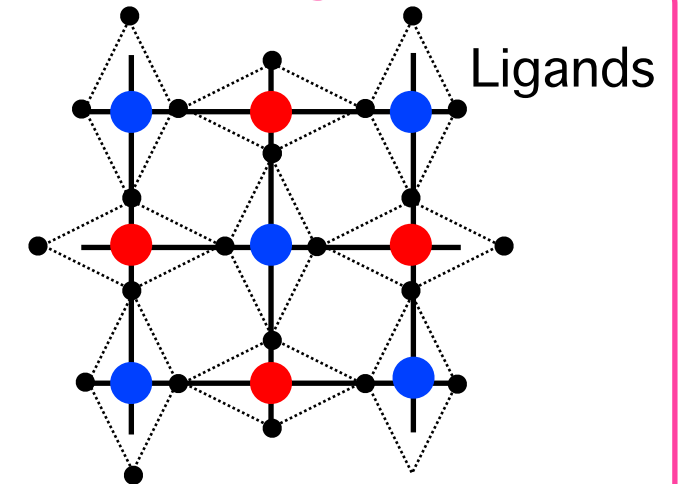


$\mathcal{T}$ ↓ ↑ T_R, P

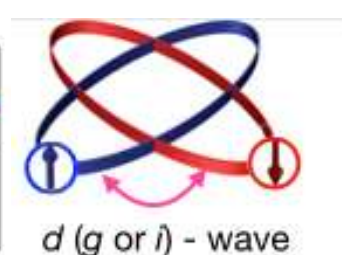
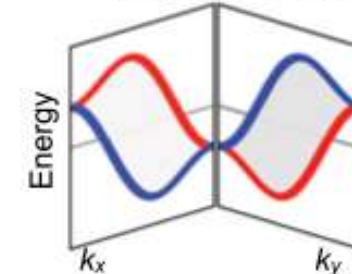
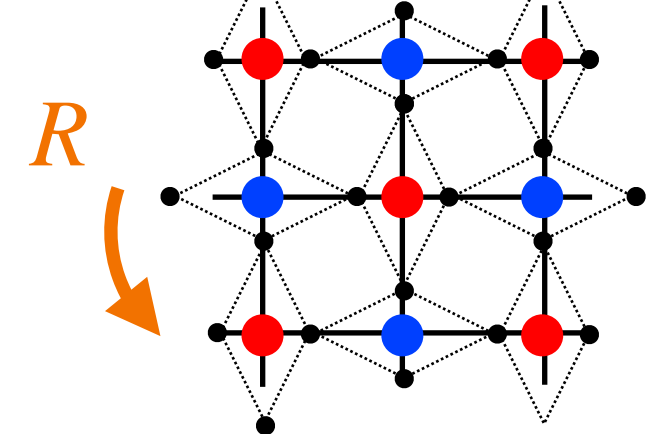


Spin degenerated bands (with $\mathcal{T}$ symmetry)

Altermagnet



$\mathcal{T}$ ↓ ↑ R



$\mathcal{T}$ -broken bands with d/g/i-wave spin texture

What is Altermagnet?

PHYSICAL REVIEW B **99**, 184432 (2019)

Antiferromagnetism in RuO_2 as d -wave Pomeranchuk instability

Kyo-Hoon Ahn,¹ Atsushi Hariki,² Kwan-Woo Lee,^{1,3} and Jan Kuneš^{2,4}

¹Division of Display and Semiconductor Physics, Korea University, Sejong 30019, Korea

²Institute of Solid State Physics, TU Wien, 1040 Vienna, Austria

³Department of Applied Physics, Graduate School, Korea University, Sejong 30019, Korea

⁴Institute of Physics, Czech Academy of Sciences, Na Slovance 2, 182 21 Praha 8, Czechia

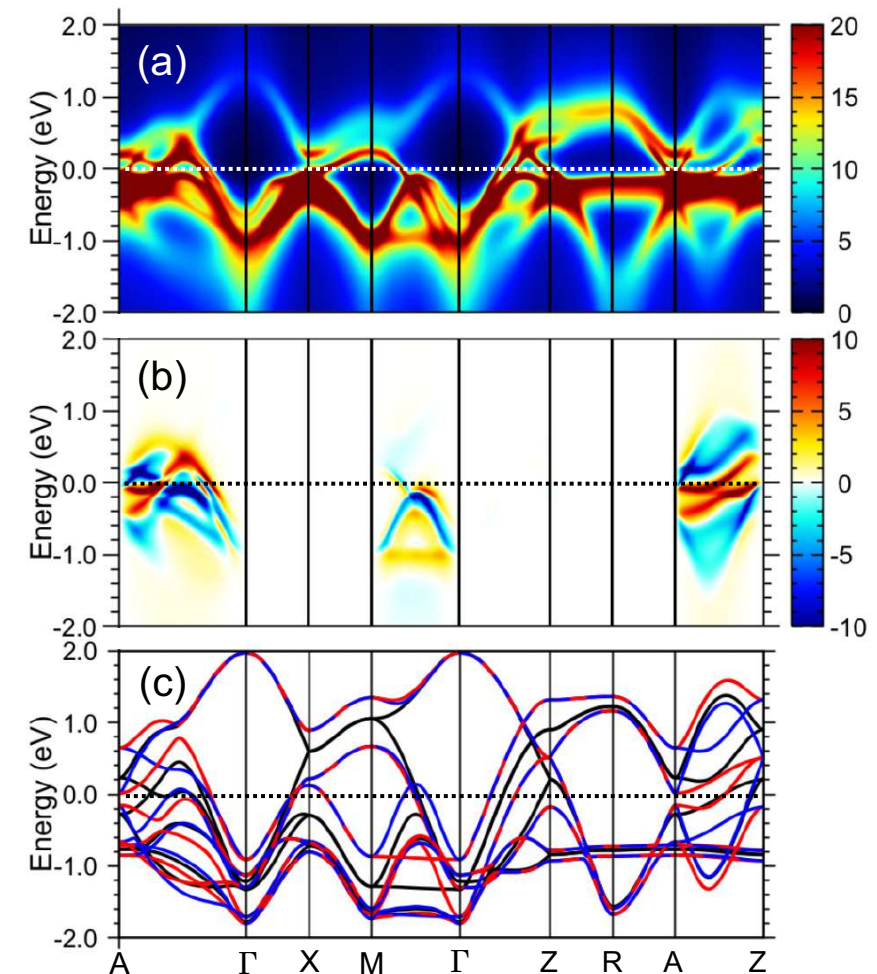
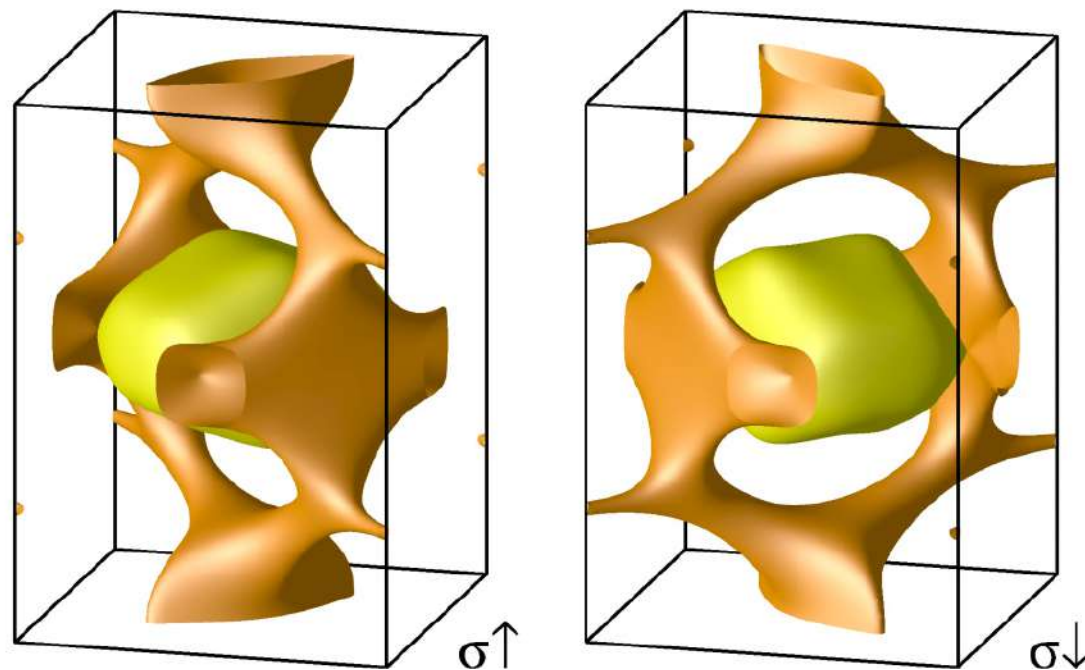


FIG. 1. (a) DFT+DMFT band structure, the spectral function $A_{\uparrow\uparrow}(\omega) + A_{\downarrow\downarrow}(\omega)$, along the high-symmetry lines in BZ. (b) The spin polarization of the band structure is calculated as $A_{\uparrow\uparrow}(\omega) - A_{\downarrow\downarrow}(\omega)$. (c) HF band structure: paramagnetic (black) and AFM ($\uparrow$ red; $\downarrow$ blue). The energy is measured from the Fermi level.

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Spin current generation in organic antiferromagnets

Makoto Naka , Satoru Hayami, Hiroaki Kusunose, Yuki Yanagi, Yukitoshi Motome & Hitoshi Seo

[Nature Communications](#) **10**, Article number: 4305 (2019) | [Cite this article](#)

 RESEARCH ARTICLE MATERIALS SCIENCE

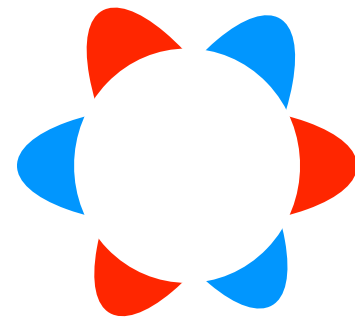
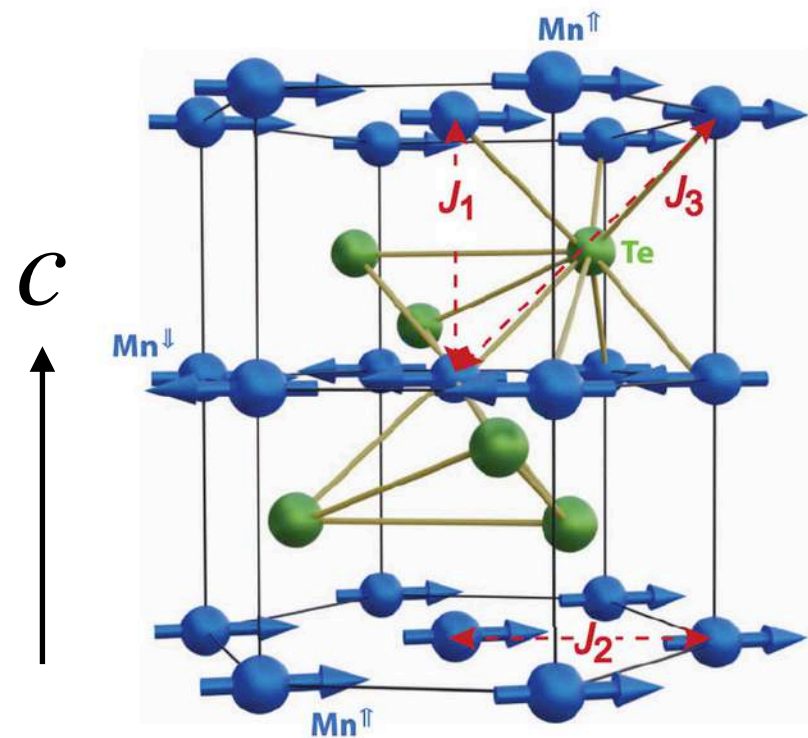
     

Crystal time-reversal symmetry breaking and spontaneous Hall effect in collinear antiferromagnets

LIBOR ŠMEJKAL , RAFAEL GONZÁLEZ-HERNÁNDEZ, T. JUNGWIRTH , AND J. SINOVA  [Authors Info & Affiliations](#)

SCIENCE ADVANCES • 5 Jun 2020 • Vol 6, Issue 23 • DOI: 10.1126/sciadv.aaz8809

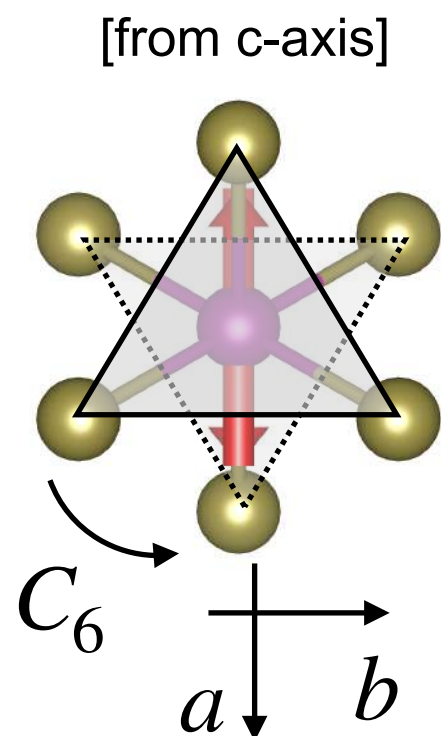
α -MnTe as altermagnet



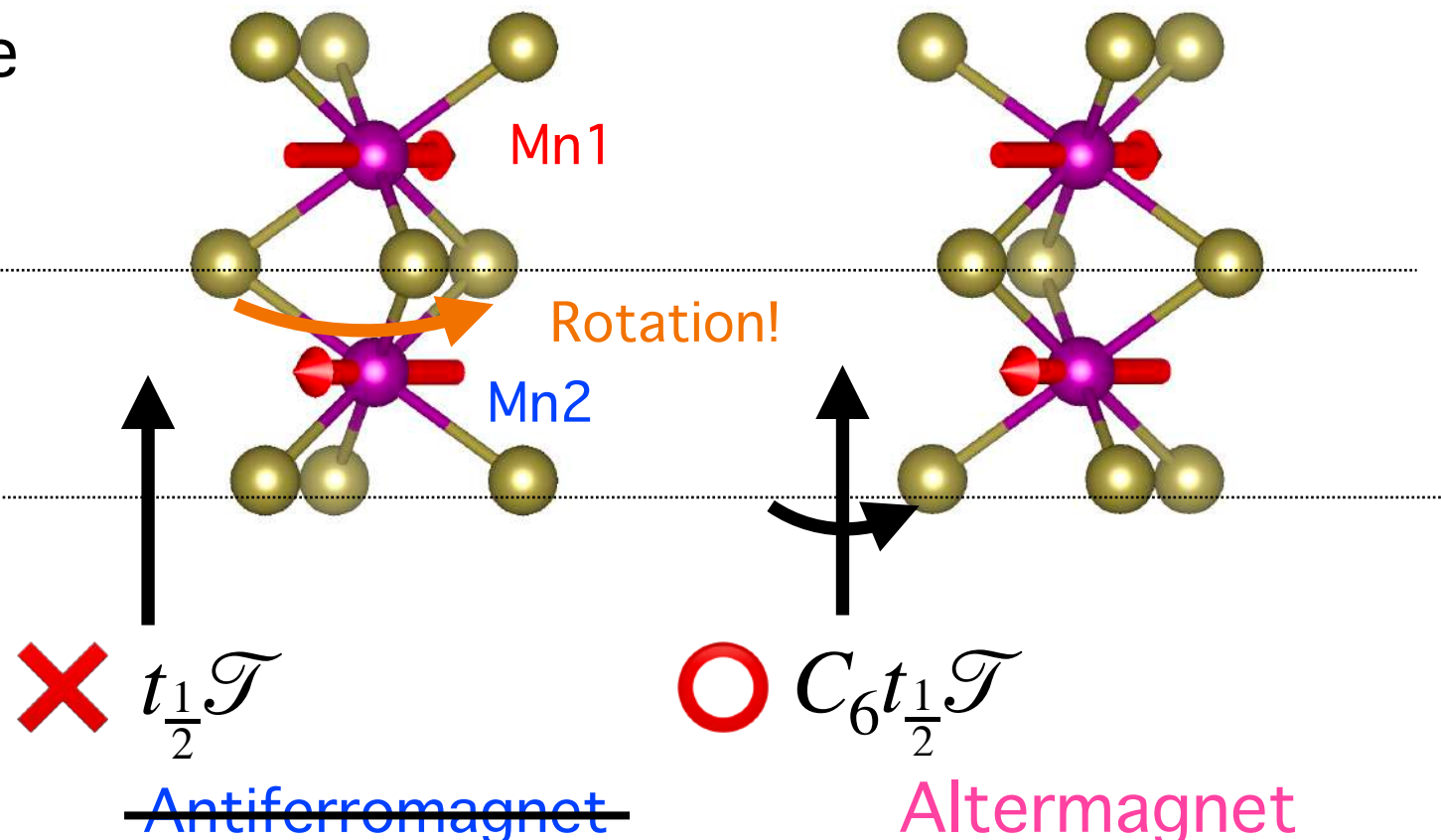
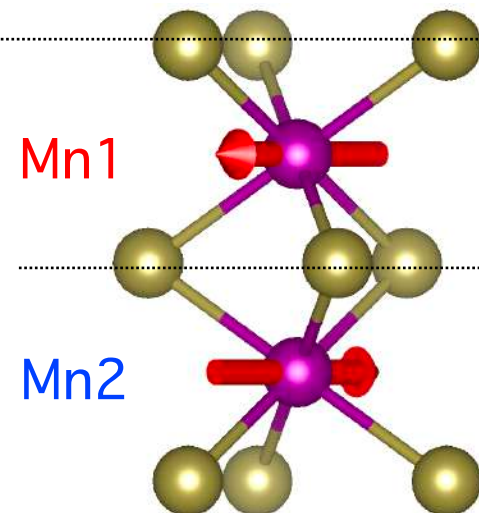
: g-wave spin splitting in band structure

- Mn atoms on hexagonal planes
- Te atoms at non-centrosymmetric positions
- Inversion at Mn (does not connect the magnetic sublattices)

$\text{Mn}^{2+} : d^5 \ S=5/2$

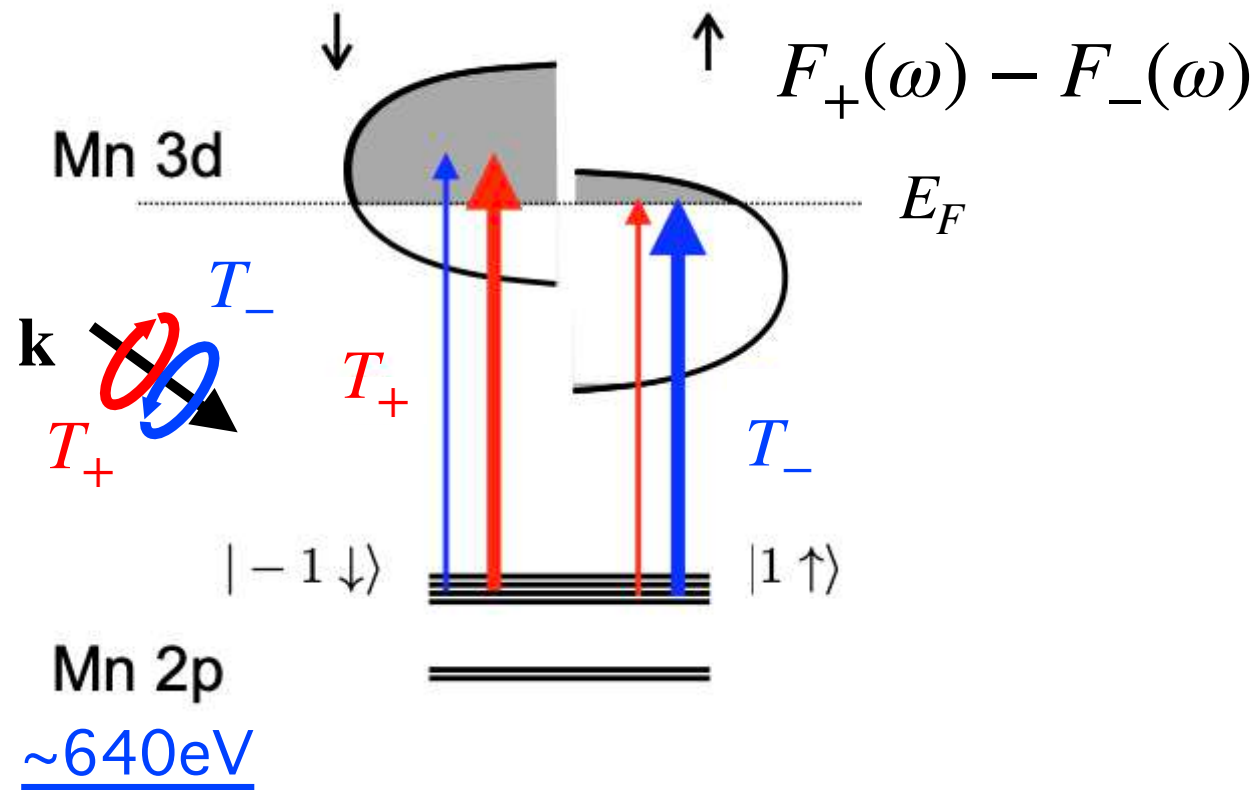


NiAs structure
($P6_3/mmc$)



X-ray magnetic circular dichroism in altermagnet

X-ray magnetic circular dichroism (XMCD)



$$F_{\text{XMCD}}(\omega) \sim 2 \operatorname{Im} \mathbf{h}(\omega) \cdot \underline{\hat{\mathbf{k}}}$$

Wave vector

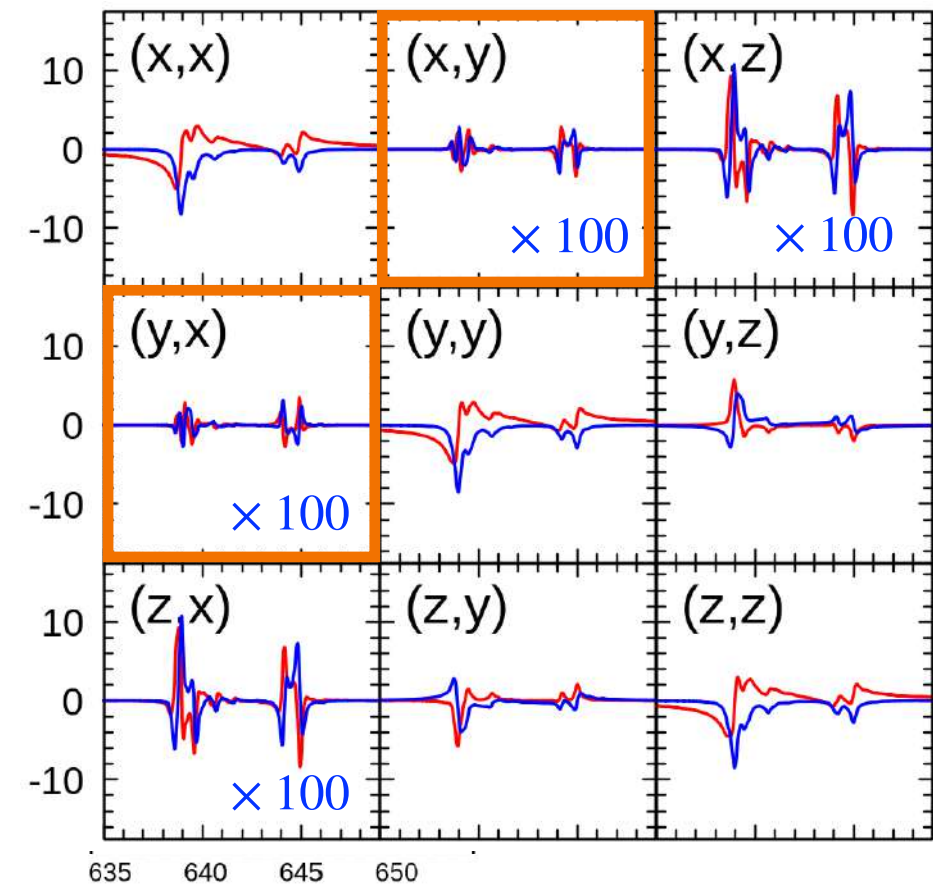
$$\mathbf{h}(\omega) = \left(\sigma_{zy}^a(\omega), \sigma_{xz}^a(\omega), \sigma_{yx}^a(\omega) \right)$$

at Mn 2p core energy ~ 640eV

antisymmetric components of (dipole) optical tensor
(thus, the same symmetry with AHE)

Optical (electric dipole)
transition : $j = x, y, z$

$$F_{i,j}(\omega) \sim \langle g | T_i^\dagger \frac{1}{\omega - H} T_j | g \rangle$$



Anti symmetric part : XMCD

$$\sigma_{yx}^a(\omega) = F_{y,x}(\omega) - F_{x,y}(\omega)$$

Theory vs Experiment: Mn L_{2,3}-edge XMCD in α -MnTe

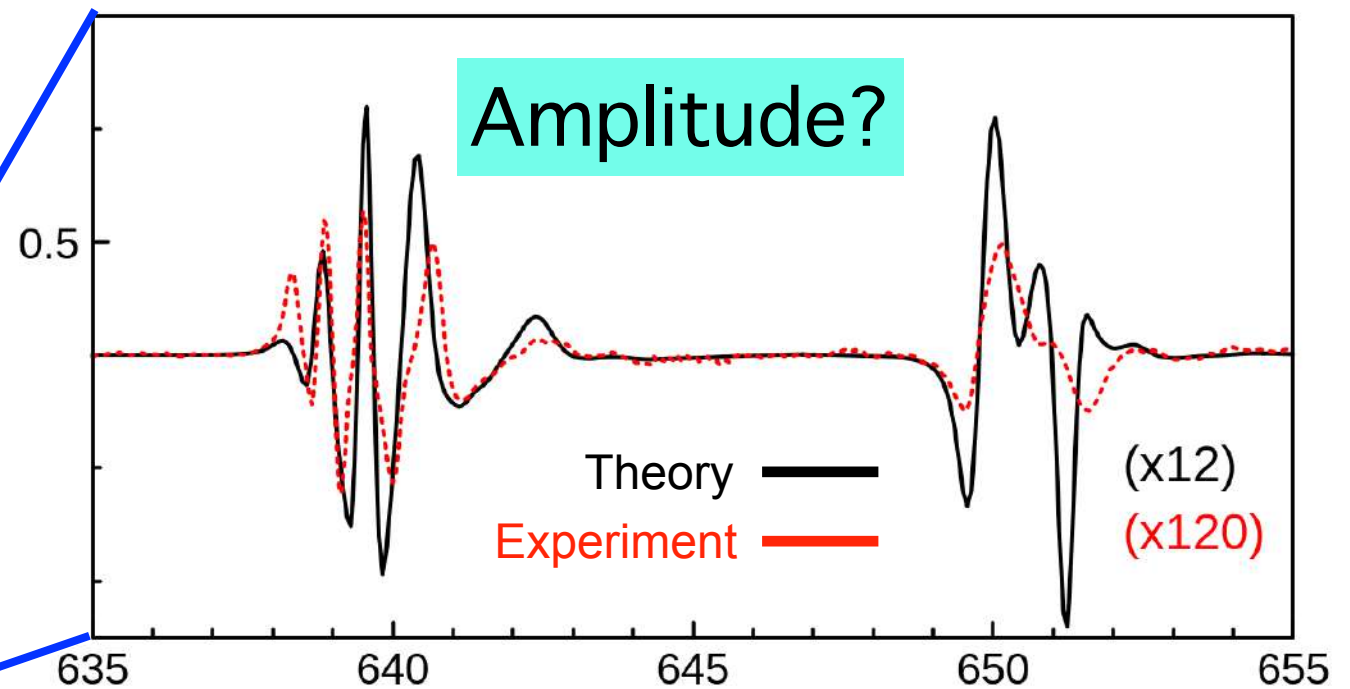
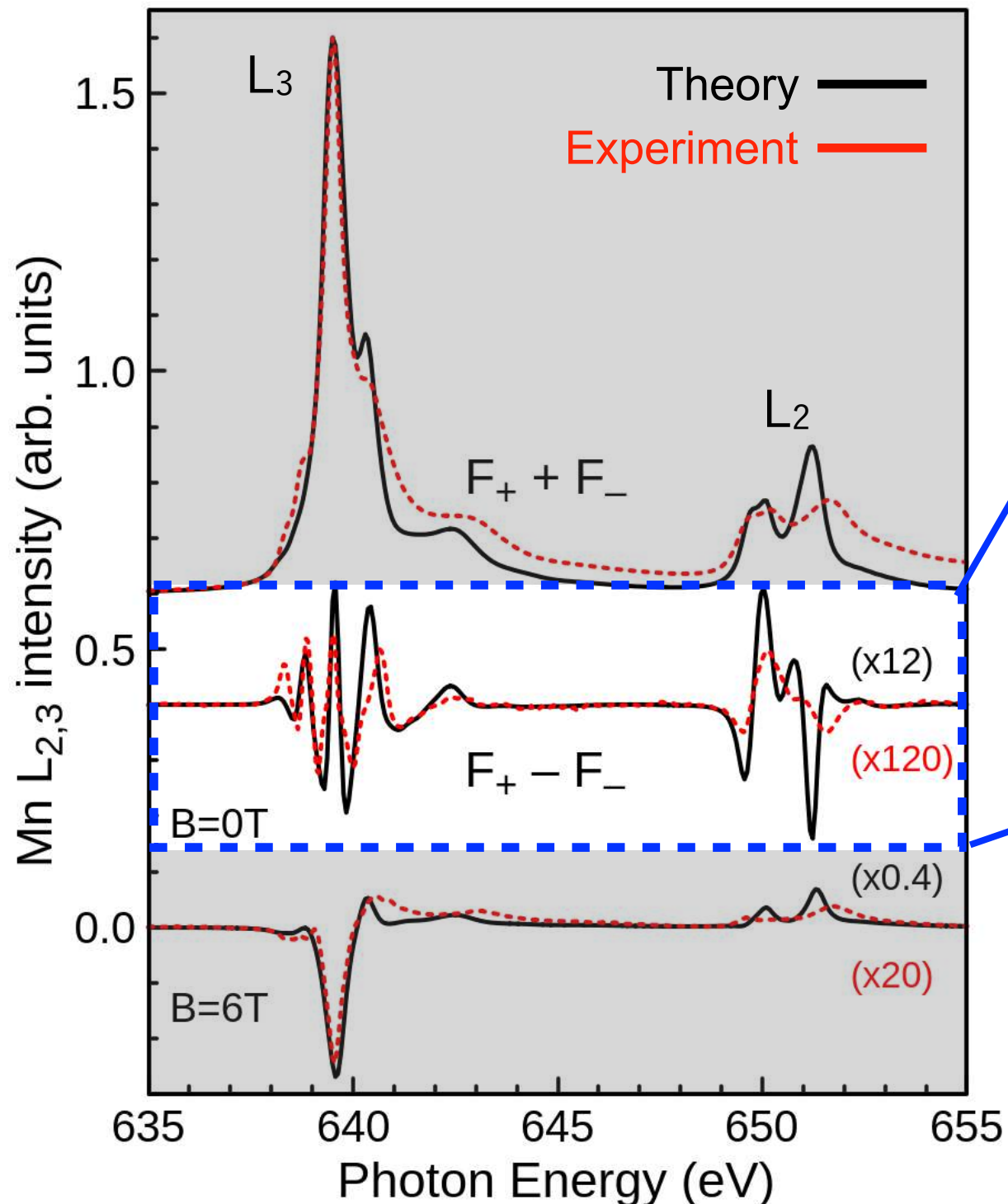
Experiment and Theory

(@ Diamond Light Source)

A. Hariki et al., Phys. Rev. Let. **132**, 176701 (2024)

Experiment $\mathbf{k} || \mathbf{c}$

- Cooled below T_c in field B(6T) $\parallel$ C
- Measured in B=0



Wiggly XMCD shape
= fingerprint of altermagnetic MnTe
is confirmed experimentally

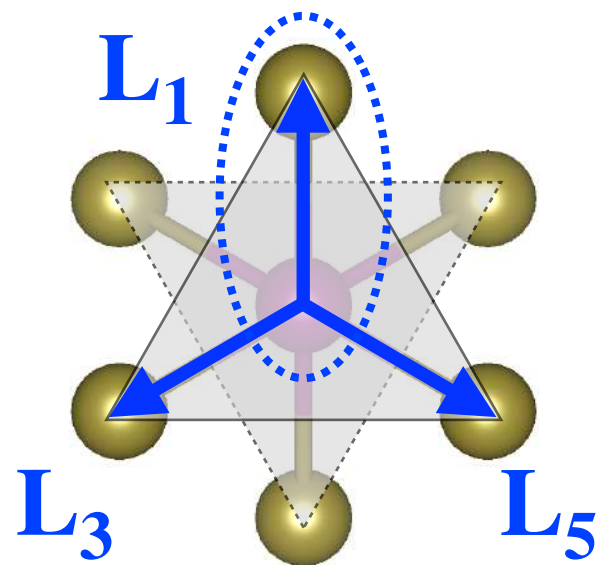
Theory vs Experiment: Mn L_{2,3}-edge XMCD in α -MnTe

Experiment $\Delta F_{\text{avg}}(\omega) = \left(\sum_{p=0}^5 (-)^p \times w_p \right) \Delta F(\omega)$ Theory

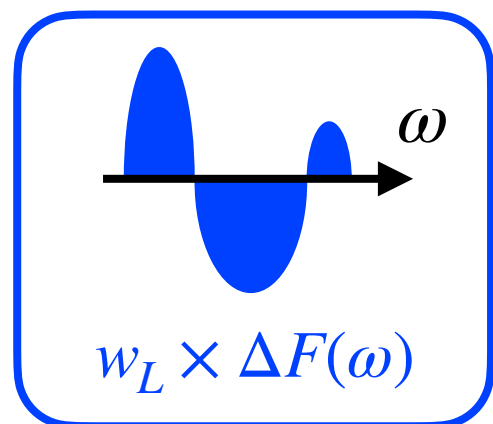
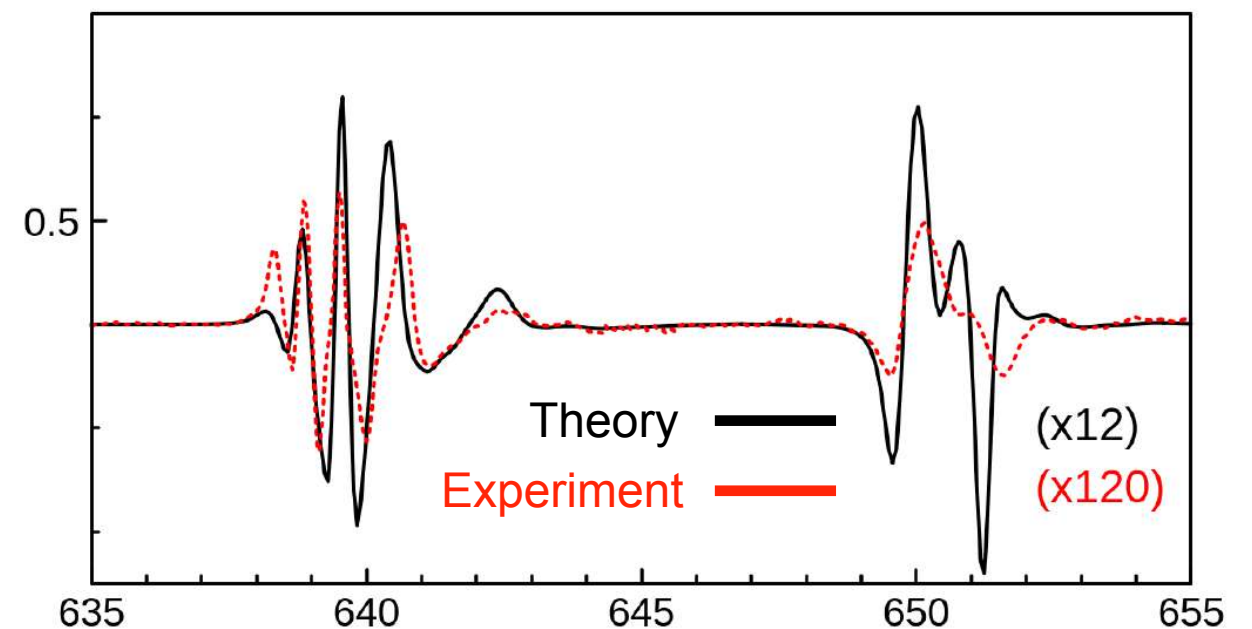
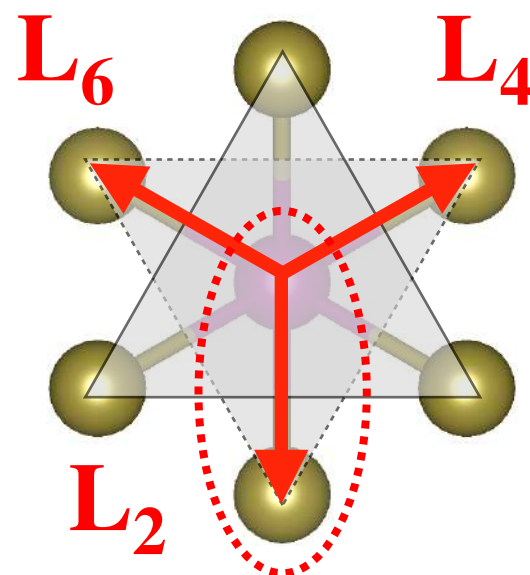
Domain weights

: minus for time-reversal Néel state

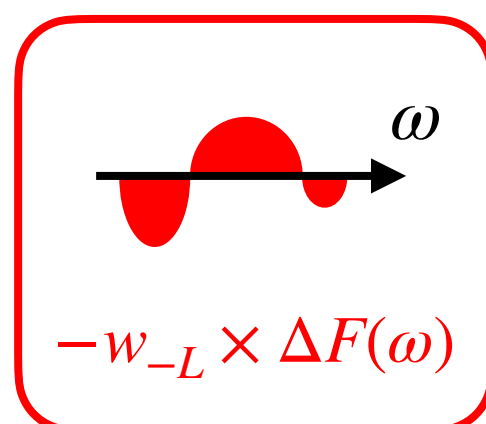
+L domains



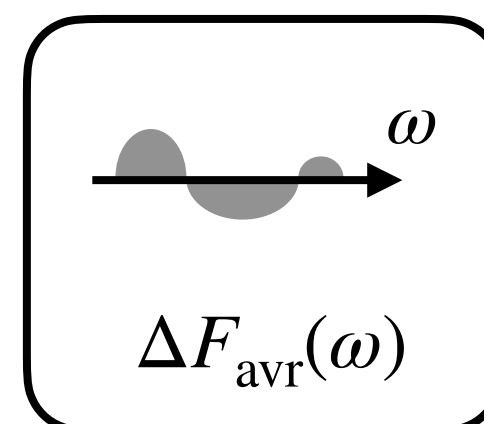
-L domains



+



=

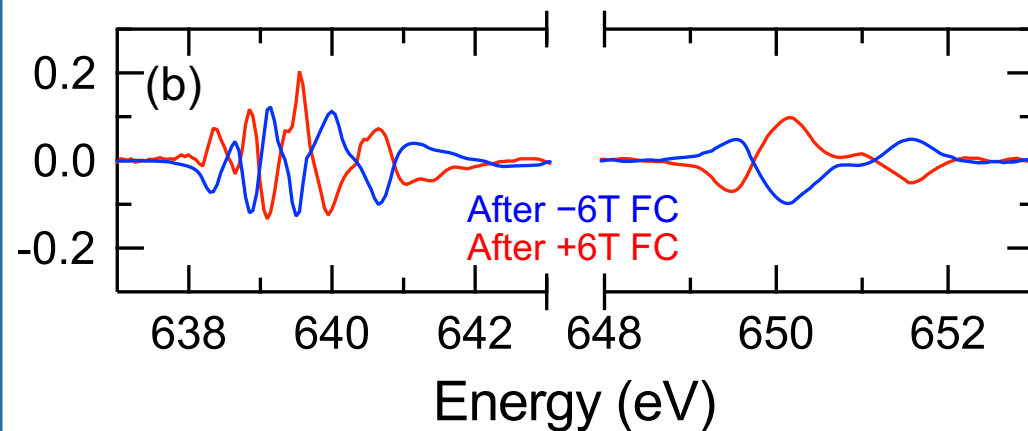


Imbalance

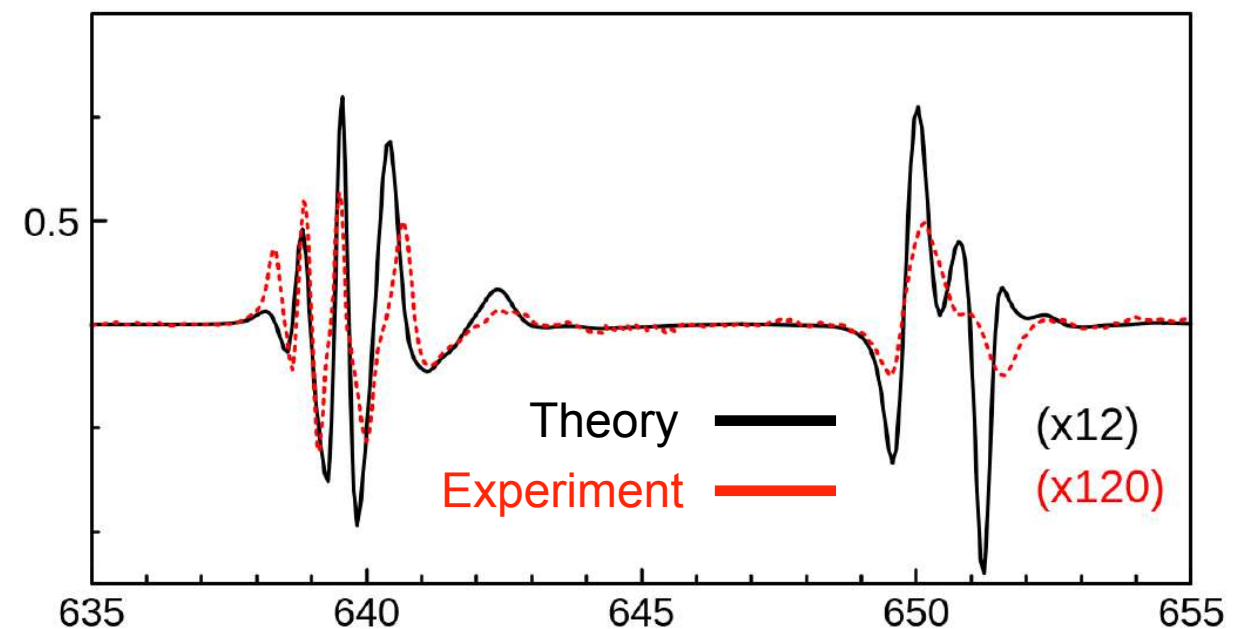
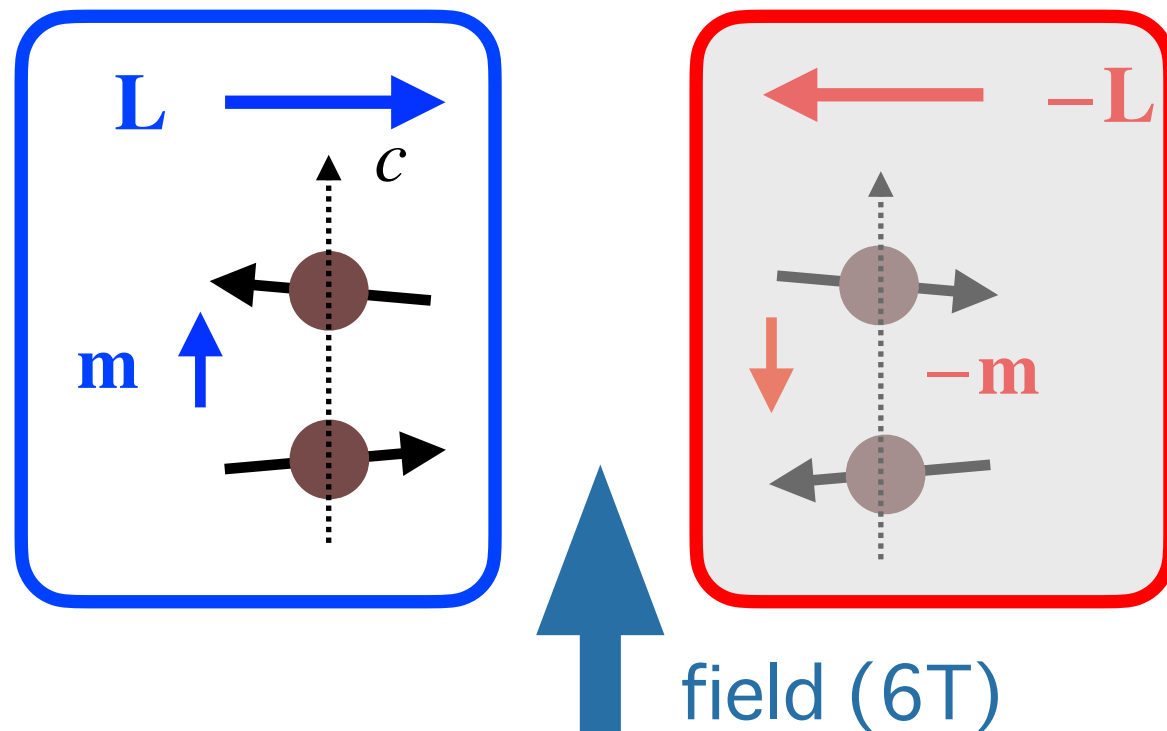
$w_L - w_{-L}$

Theory vs Experiment: Mn L_{2,3}-edge XMCD in α -MnTe

Supplemental Experiment



- Cooled below T_c in field $B(=+6T, -6T) \parallel C$
- Measured in $B=0$



$w_L \times \Delta F(\omega)$

$-w_{-L} \times \Delta F(\omega)$

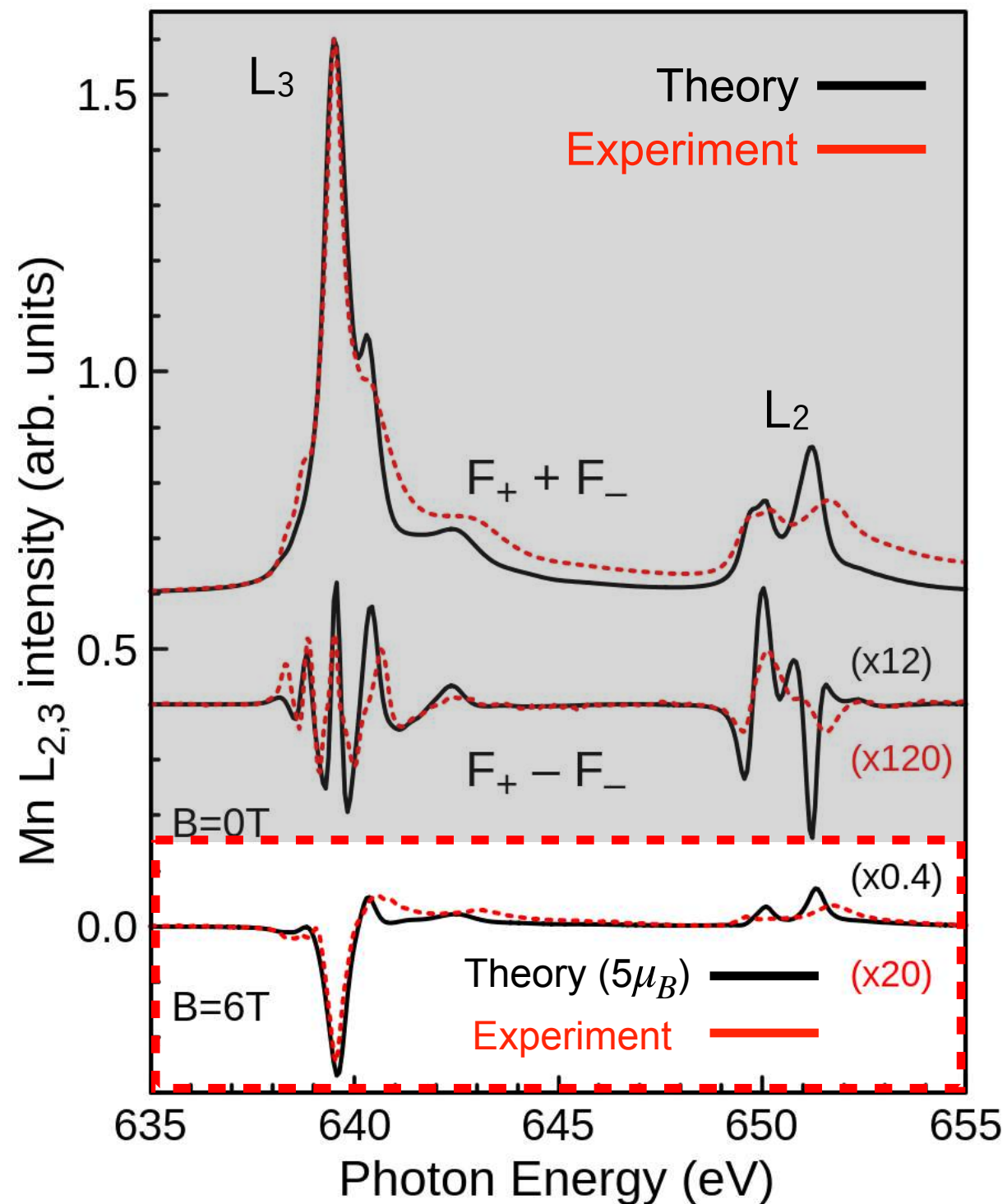
$\Delta F_{avr}(\omega)$

Imbalance
 $w_L - w_{-L}$

Theory vs Experiment: Mn L_{2,3}-edge XMCD in α -MnTe

Experiment and Theory

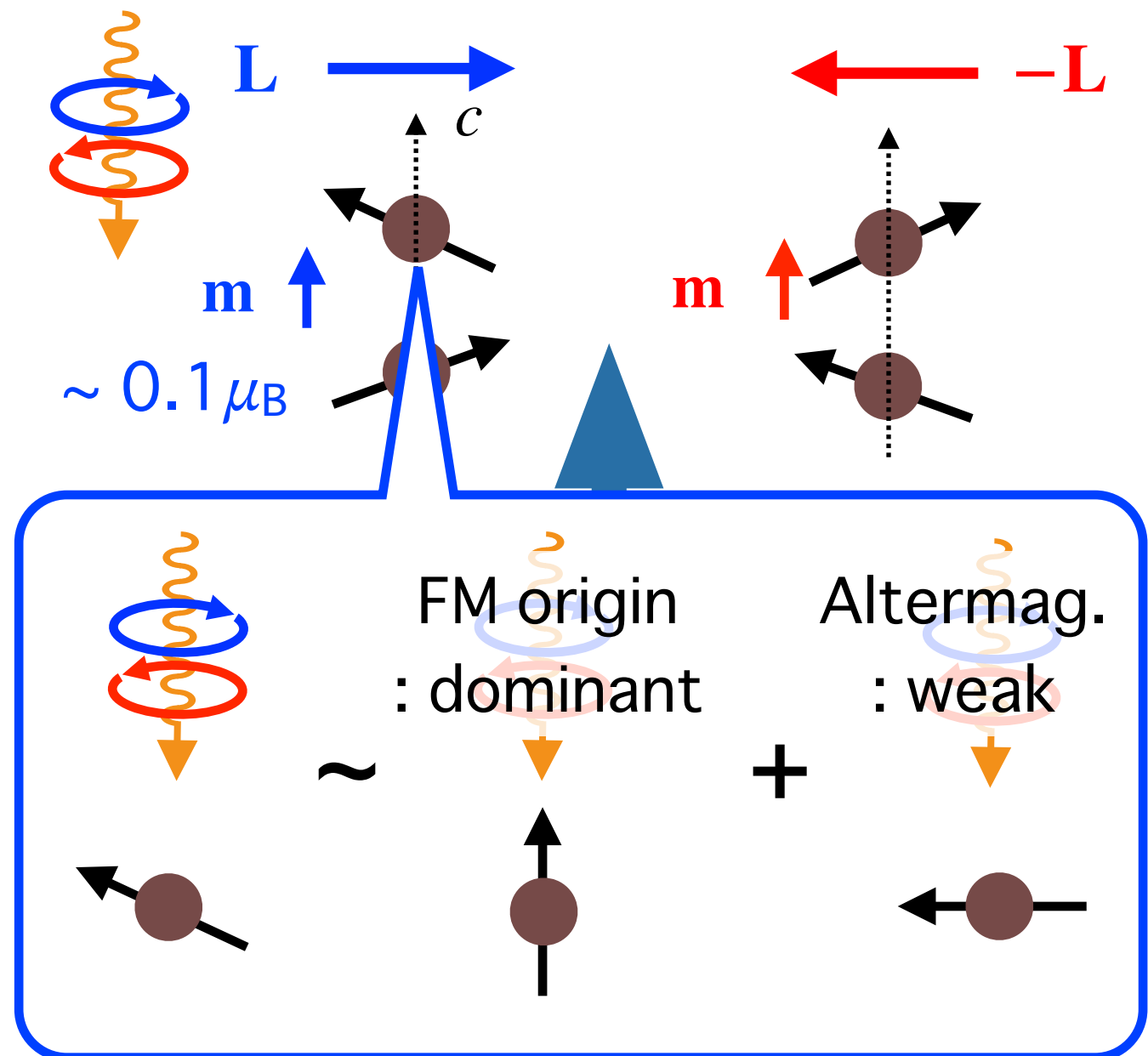
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A. Hariki et al., Phys. Rev. Let. **132**, 176701 (2024)

Experiment $\mathbf{k} || \mathbf{c}$

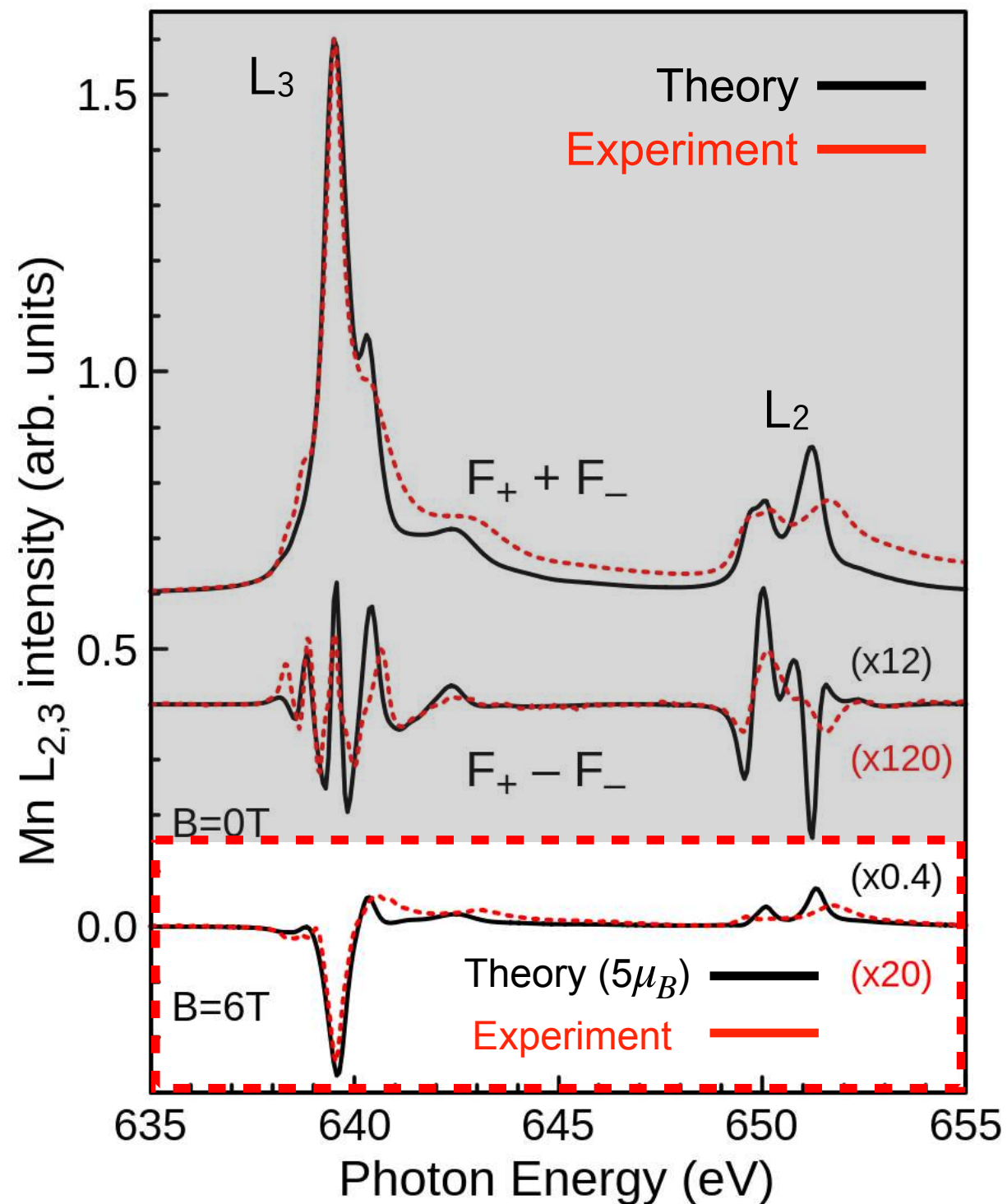
- Cooled below T_c in field $B(6T) || C$
- Measured in the field B



Theory vs Experiment: Mn L_{2,3}-edge XMCD in α -MnTe

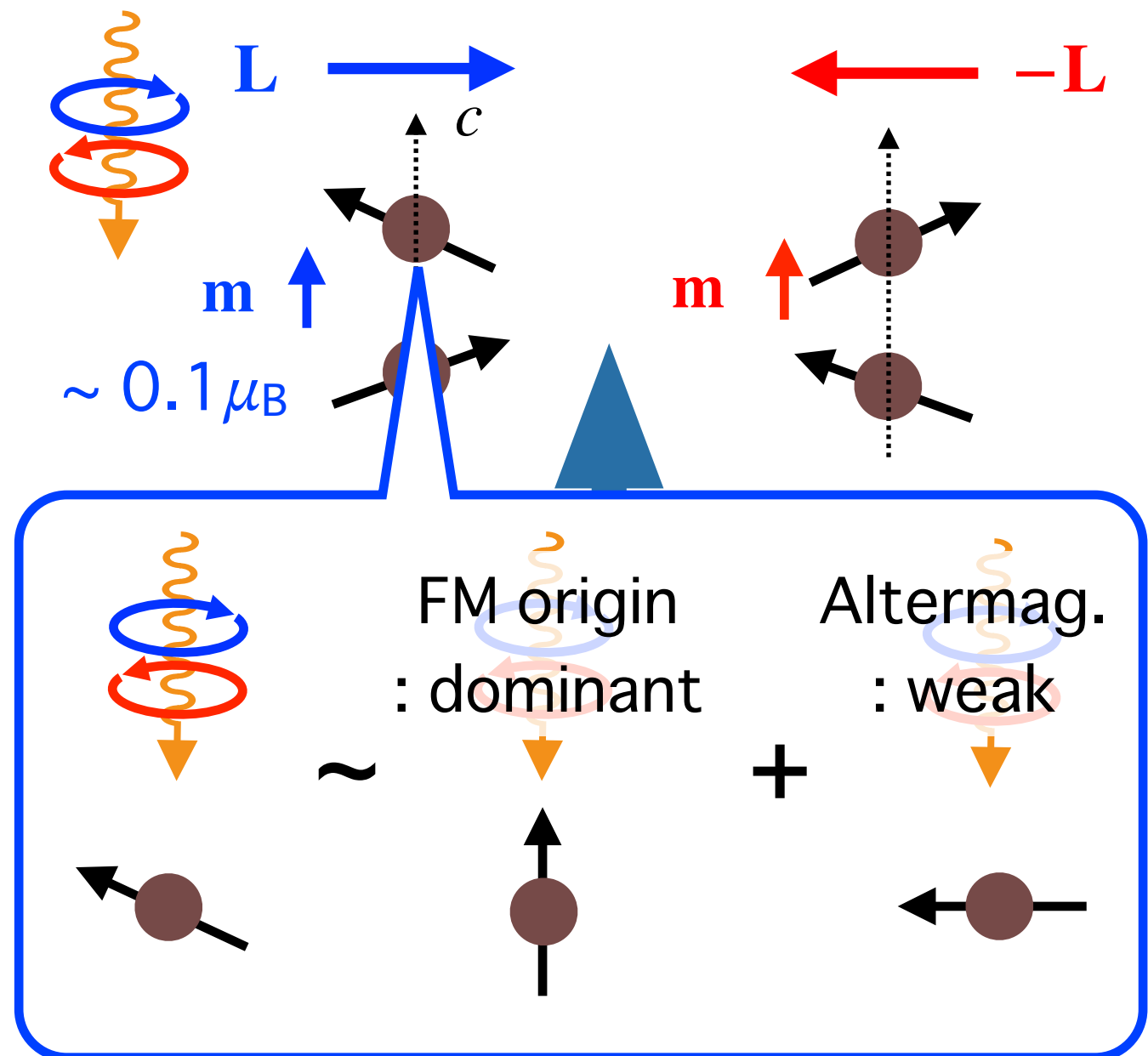
Experiment and Theory

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Experiment $\mathbf{k} \parallel \mathbf{c}$

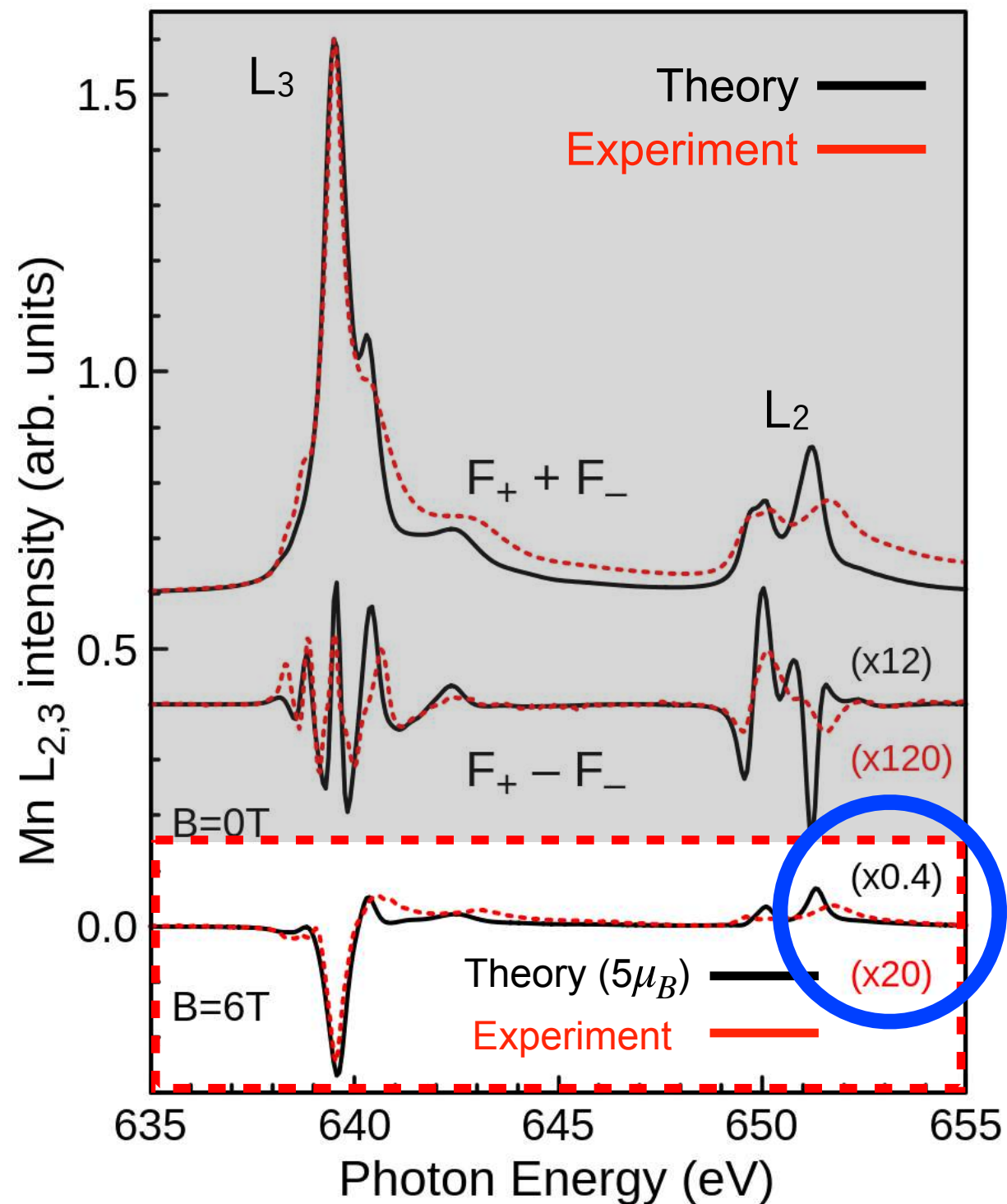
- Cooled below T_c in field $B(6T) \parallel C$
- Measured in the field B



Theory vs Experiment: Mn L_{2,3}-edge XMCD in α -MnTe

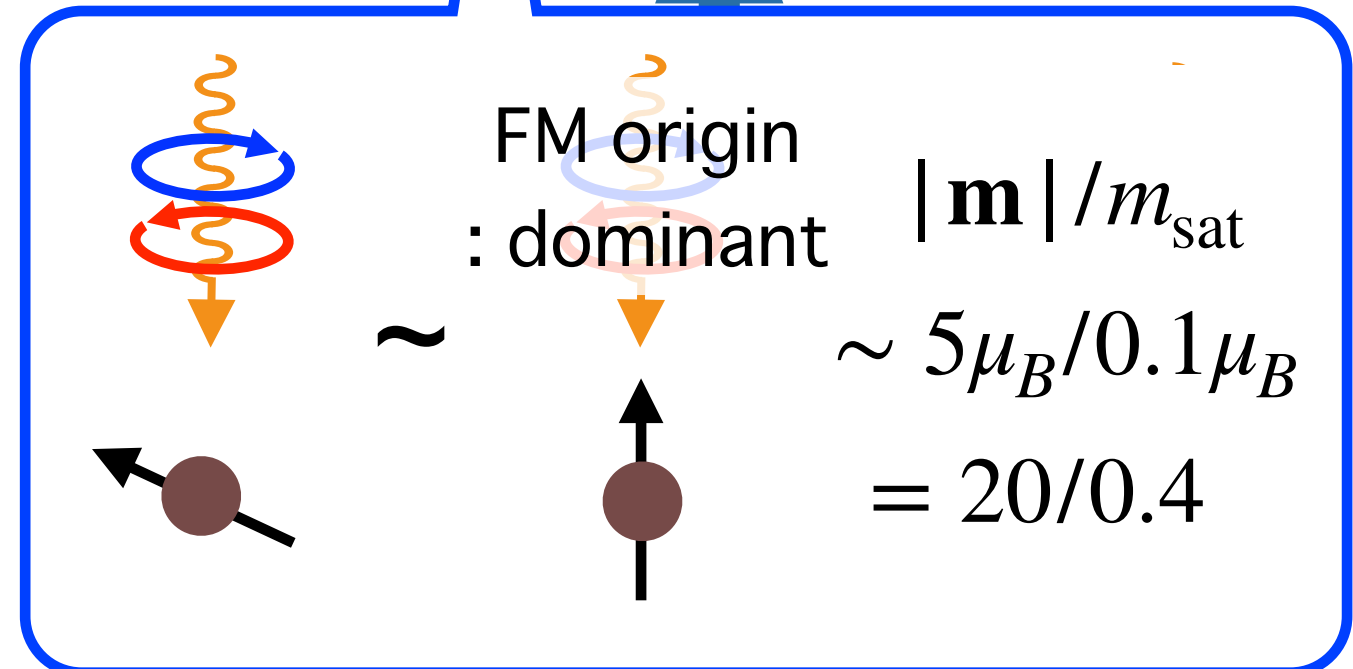
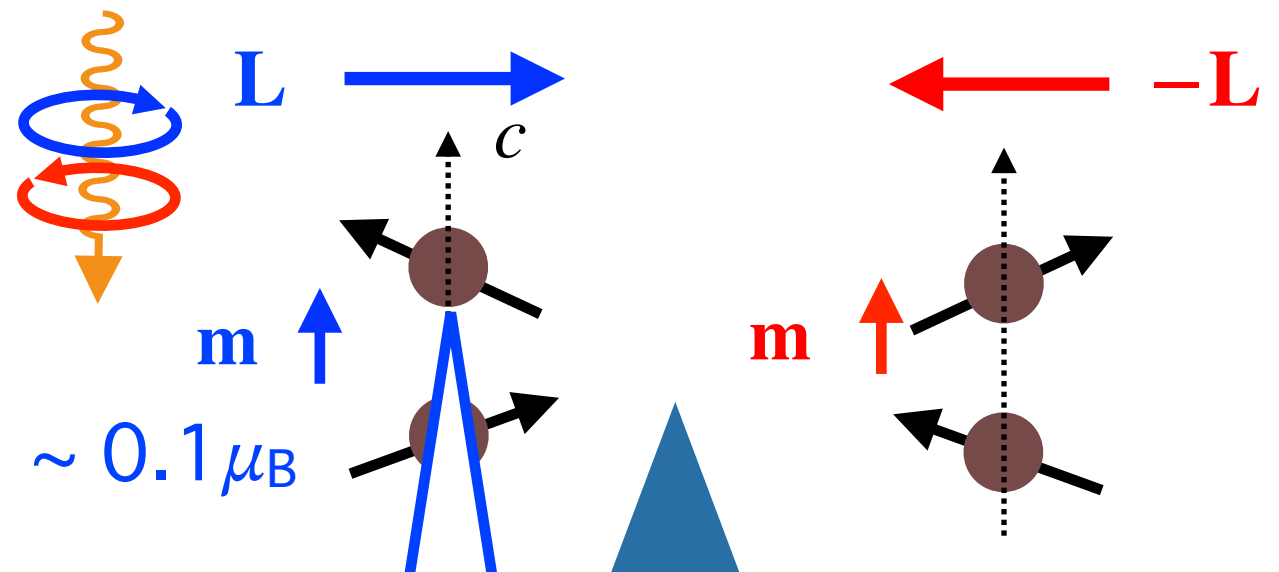
Experiment and Theory

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Experiment $\mathbf{k} \parallel \mathbf{c}$

- Cooled below T_c in field $B(6T) \parallel C$
- Measured in the field B



Recent XMCD experiment

arXiv > cond-mat > arXiv:2502.18597

Search...

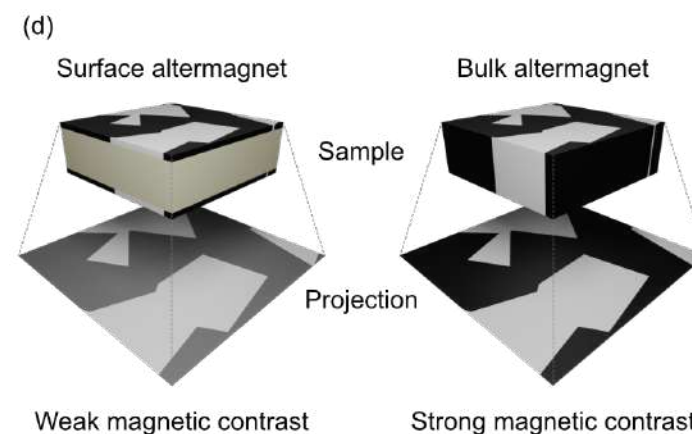
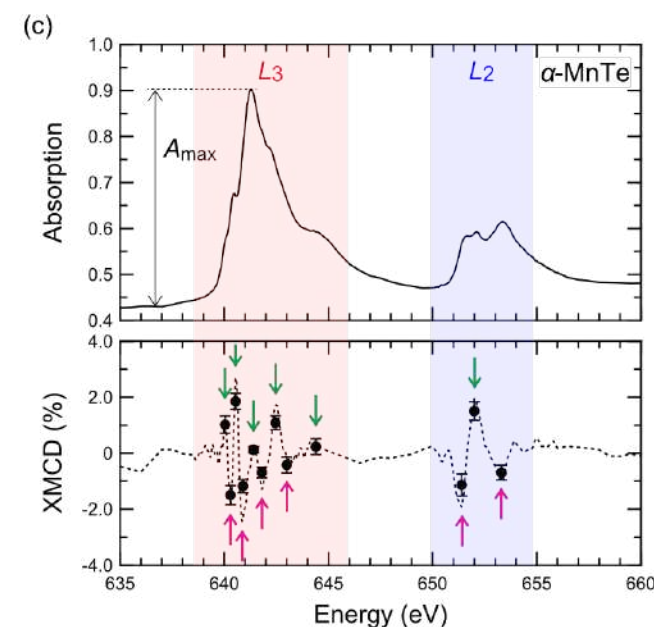
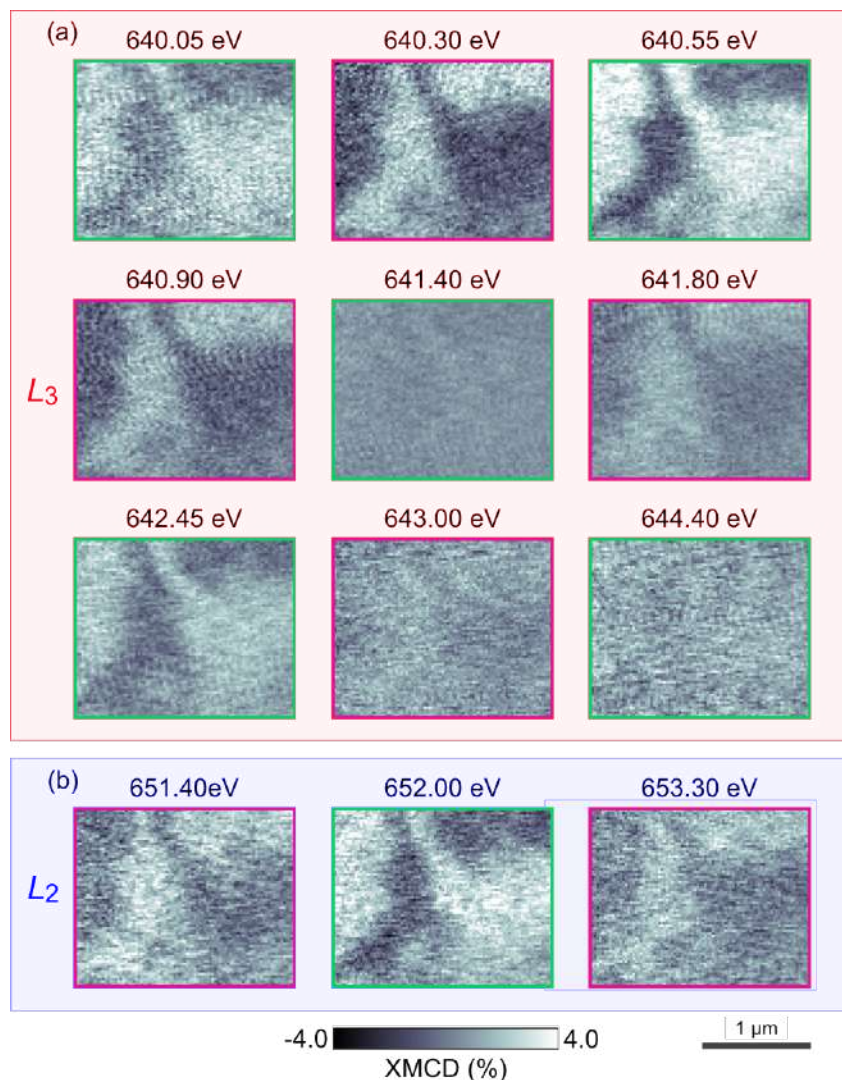
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Condensed Matter > Materials Science

[Submitted on 25 Feb 2025]

Altermagnetic nanotextures revealed in bulk MnTe

Rikako Yamamoto, Luke Alexander Turnbull, Marcus Schmidt, José Claudio Corsaletti Filho, Hayden Jeffrey Binger, Marisel Di Pietro Martínez, Markus Weigand, Simone Finizio, Yurii Prots, George Matthew Ferguson, Uri Vool, Sebastian Wintz, Claire Donnelly



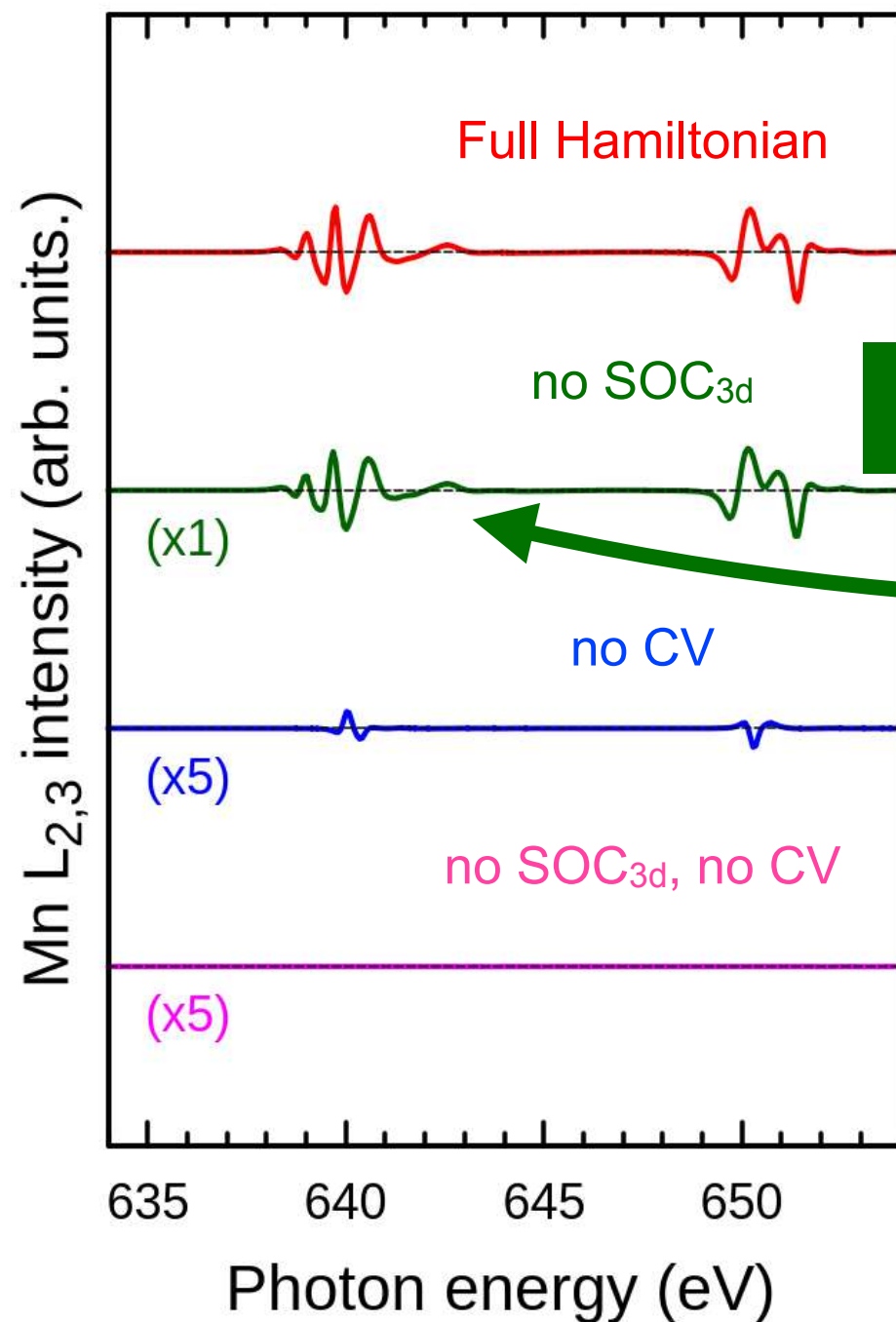
signal as well. Indeed, previous spectroscopic measurements reported an order of magnitude difference between the magnitude of the predicted, and measured altermagnetic XMCD signal [27]. Here, we observe a maximum XMCD contrast of $1.8 \pm 0.3\%$ of A_{max} , the maximum absorption, which agrees well with the predicted XMCD contrast of 1.8% of A_{max} [27].

Our DFT+DMFT calculation

Origin of XMCD in altermagnetic MnTe

Calc. Mn single-site XMCD

$\mathbf{k} \perp \mathbf{L} \ (\sim \sigma_{xy})$

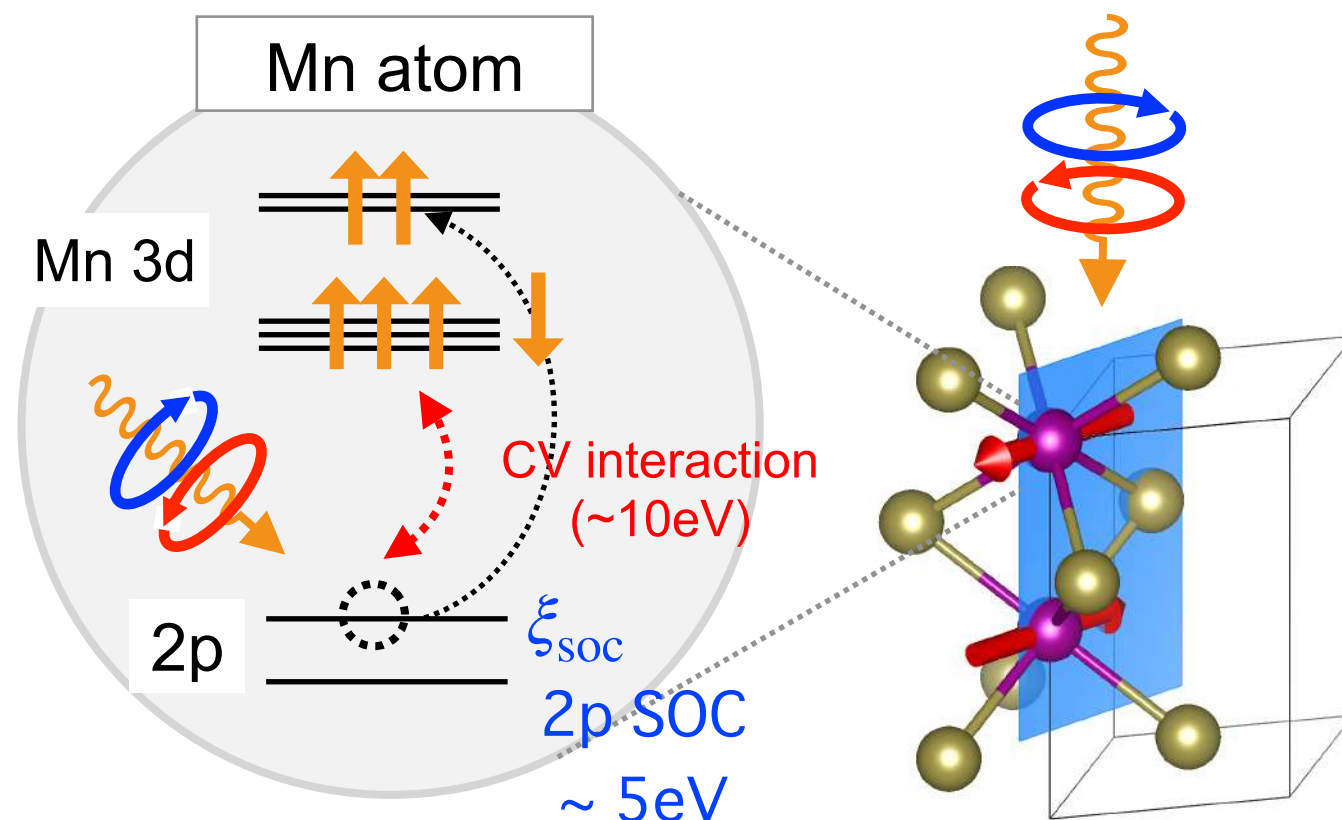


$$\hat{H}_{\text{at}}^0 = \epsilon_c \sum_{m,\sigma} \hat{p}_{m\sigma}^\dagger \hat{p}_{m\sigma} + \sum_{m,m',\sigma,\sigma'} h_{m\sigma,m'\sigma'}^{(2p)} \hat{p}_{m\sigma}^\dagger \hat{p}_{m'\sigma'} + \sum_{m,m',\sigma} h_{mm'}^{(\text{CF})} \hat{d}_{m\sigma}^\dagger \hat{d}_{m'\sigma} + b \sum_{m,\sigma} \hat{d}_{m\sigma}^\dagger \hat{d}_{m-\sigma} + U_{pd} \hat{n}_p \hat{n}_d + \sum_{i,j,k,l} u_{ijkl}^{\sigma\sigma'} \hat{d}_{i\sigma}^\dagger \hat{d}_{j\sigma'} \hat{d}_{k\sigma'}^\dagger \hat{d}_{l\sigma}.$$

3d SOC : negligible role

$$\sum_{m,m',\sigma,\sigma'} h_{m\sigma,m'\sigma'}^{(3d)} \hat{d}_{m\sigma}^\dagger \hat{d}_{m'\sigma'}$$

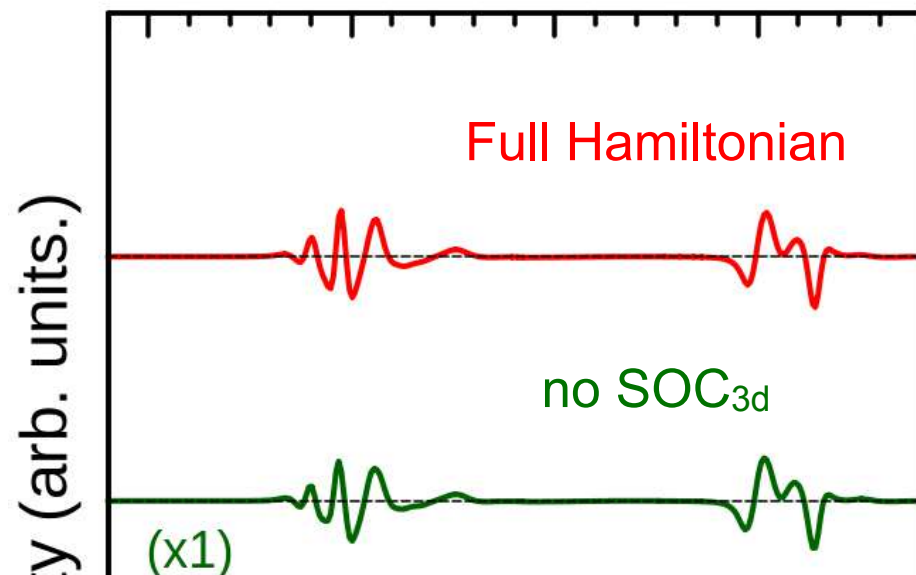
3d SOC



Origin of XMCD in altermagnetic MnTe

Calc. Mn single-site XMCD

$\mathbf{k} \perp \mathbf{L} \ (\sim \sigma_{xy})$



$$\begin{aligned} \hat{H}_{\text{at}}^0 = & \epsilon_c \sum_{m,\sigma} \hat{p}_{m\sigma}^\dagger \hat{p}_{m\sigma} + \sum_{m,m',\sigma,\sigma'} h_{m\sigma,m'\sigma'}^{(2p)} \hat{p}_{m\sigma}^\dagger \hat{p}_{m'\sigma'} \\ & + \sum_{m,m',\sigma} h_{mm'}^{(\text{CF})} \hat{d}_{m\sigma}^\dagger \hat{d}_{m'\sigma} + b \sum_{m,\sigma} \hat{d}_{m\sigma}^\dagger \hat{d}_{m-\sigma} \\ & + U_{pd} \hat{n}_p \hat{n}_d + \sum_{i,j,k,l} u_{ijkl}^{\sigma\sigma'} \hat{d}_{i\sigma}^\dagger \hat{d}_{j\sigma'} \hat{d}_{k\sigma}^\dagger \hat{d}_{l\sigma}. \end{aligned}$$

$$\hat{H}_{\text{at}}^1 = \underbrace{\sum_{i,j,k,l} w_{ijkl}^{\sigma\sigma'} \hat{d}_{i\sigma}^\dagger \hat{d}_{j\sigma'} \hat{p}_{k\sigma}^\dagger \hat{p}_{l\sigma}}_{\text{CV}} + \underbrace{\sum_{m,m',\sigma,\sigma'} h_{m\sigma,m'\sigma'}^{(3d)} \hat{d}_{m\sigma}^\dagger \hat{d}_{m'\sigma'}}_{\text{3d SOC}}$$

Altermagnetism is a non-relativistic concept

dual role of SOC in altermagnetism :

- Necessary to observe AHE and magneto-optical effects (XMCD) etc ..
- May cause weak ferromagnetic, non-collinear magnetism

→ How to distinguish altermagnetic signal from ferromagnetic one?

Core-level XMCD :

Mn 2p SOC : necessary to observe XMCD

Mn 3d SOC : negligible effect on the spectra

XMCD + XMLD = domain imaging

Article | [Open access](#) | Published: 11 December 2024

Nanoscale imaging and control of altermagnetism in MnTe

[O. J. Amin](#) , [A. Dal Din](#) , [E. Golias](#), [Y. Niu](#), [A. Zakharov](#), [S. C. Fromage](#), [C. J. B. Fields](#), [S. L. Heywood](#), [R. B. Cousins](#), [F. Maccherozzi](#), [J. Krempaský](#), [J. H. Dil](#), [D. Kriegner](#), [B. Kiraly](#), [R. P. Campion](#), [A. W. Rushforth](#), [K. W. Edmonds](#), [S. S. Dhesi](#), [L. Šmejkal](#), [T. Jungwirth](#) & [P. Wadley](#) 

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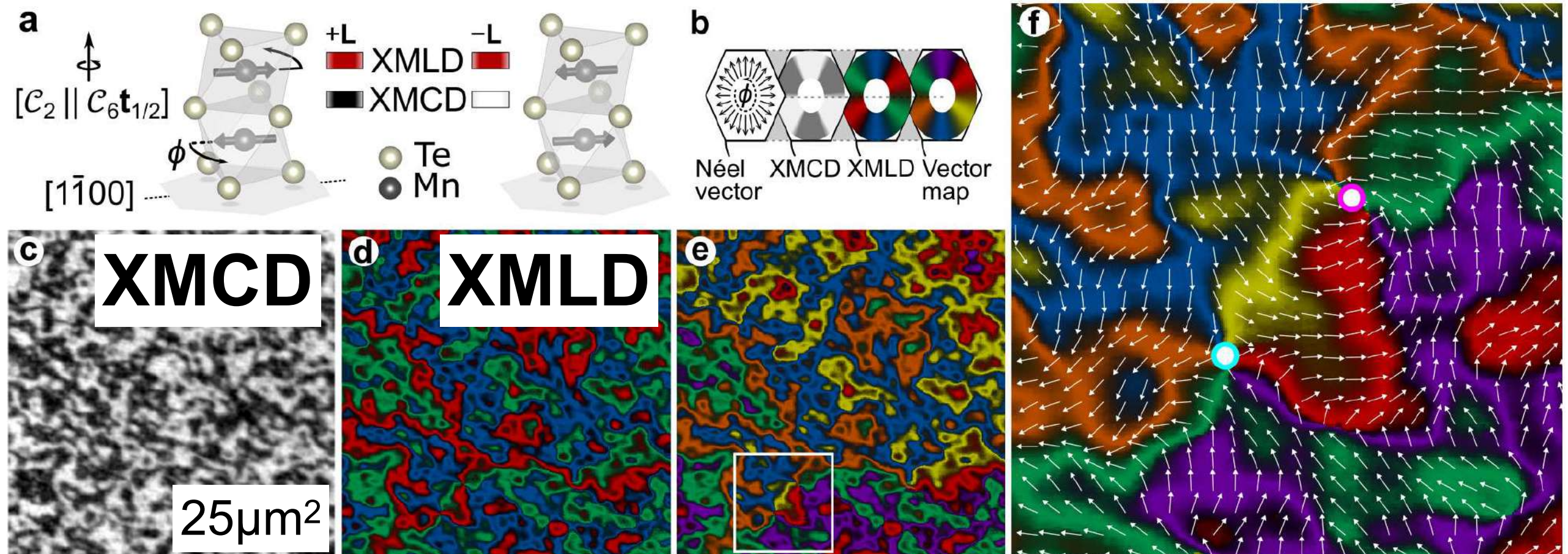


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1. Core-level X-ray spectroscopy and DFT-based embedding approach

★ **Method.** DFT+ dynamical mean-field theory (DMFT)

A. Hariki, T. Uozumi, and J. Kuneš, Phys. Rev. B **96**, 045111 (2017)

A. Hariki, M. Winder, and J. Kuneš, Phys. Rev. Lett. **121**, 126403 (2018)

A. Hariki, M. Winder, T. Uozumi, and J. Kuneš, Phys. Rev. B **101**, 115130 (2020)

2. Application to various optical processes and compounds

★ **Excitations.** XPS, XAS, RIXS ★ **Materials.** *d*, *f* electron systems

★ **Physics.** Magnetism, valence structure, elementary excitations

K. Higashi, M. Winder, J. Kuneš, and A. Hariki, Phys. Rev. X **11**, 041009 (2021)

D. Takegami, A. Hariki et al., Phys. Rev. X **12**, 011017 (2022)

M. C. Rahn, K. Kummer, A. Hariki, et al., Nat. Commun. **13**, 6129 (2022)

J. Li, A. Hariki et al., Phys. Rev. X **13**, 011012 (2023)

A. Hariki et al., Phys. Rev. Lett. **132**, 176701 (2024)

Thank you for your attention

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Jan Kunes
(マサリク大学)



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