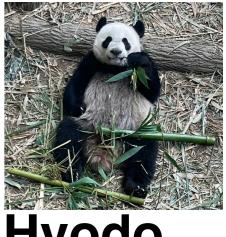
# Compositeness of exotic hadrons with decay and coupled-channel effects



arXiv:2303.07038 [hep-ph]

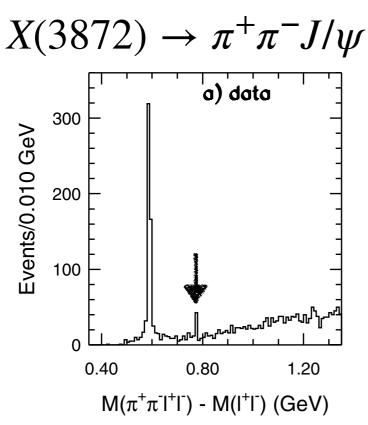


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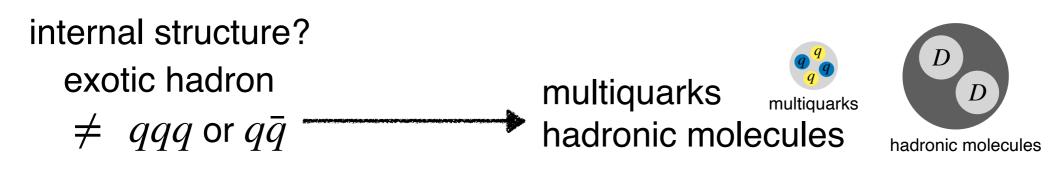
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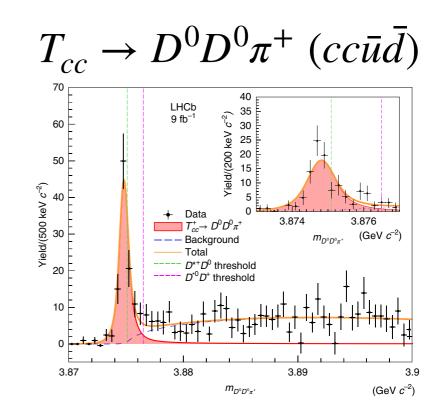
## Near-threshold exotic hadrons

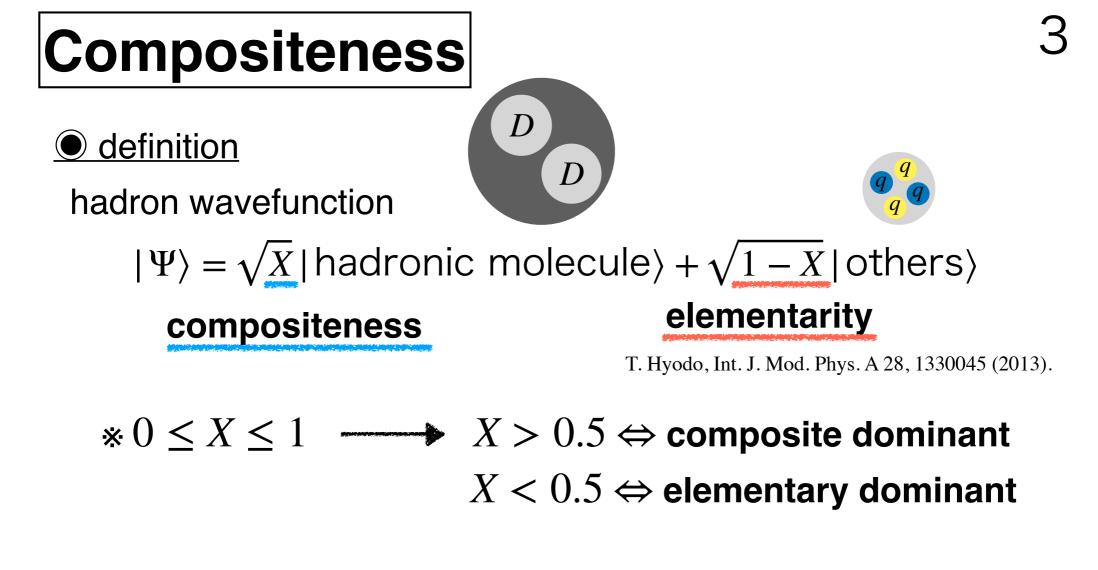




LHCb Collaboration, Nature Phys. **18** (2022) no.7, 751-754; LHCb Collaboration, Nat. Commun. **13** 3351 (2022).







model calculation

T. Hyodo, D. Jido, and A. Hosaka, Phys. Rev. C 85, 015201 (2012);F. Aceti and E. Oset, Phys. Rev. D 86, 014012 (2012).

compositeness X ----- residue of scattering amplitude

## Low-energy universality

- scattering length  $a_0 \gg$  typical length scale of system  $R_{\rm typ}$ 

#### low-energy universality

E. Braaten and H.-W. Hammer, Phys. Rept. 428, 259 (2006);F. P. Naidon and S. Endo, Rept. Prog. Phys. 80, 056001 (2017).

 $\longrightarrow$  length scales are written only by  $|a_0|(\rightarrow \infty)$ 

for bound states ?

$$a_0 = R$$
  $R = 1/\sqrt{2\mu B}$   $a_0 \to \infty \longrightarrow B \to 0$ 

universality holds for weakly-bound states!!

- compositeness X = 1 in  $B \rightarrow 0$  limit <sub>T. Hyodo, Phys. Rev. C 90, 055208 (2014)</sub>.

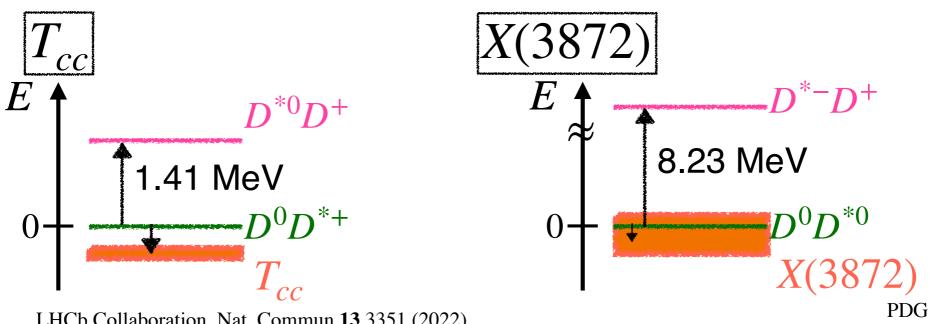
#### near threshold poles = composite dominant ?

e.g. <sup>8</sup>Be, <sup>12</sup>C  $\rightarrow \alpha$  cluster? H. Horiuchi, K. Ikeda, and Y. Suzuki, Prog. Theor. Phys. Suppl. 52, 89 (1972).

# Decay & coupled ch. effects

However...

actual exotic hadrons ---decay and coupled channel



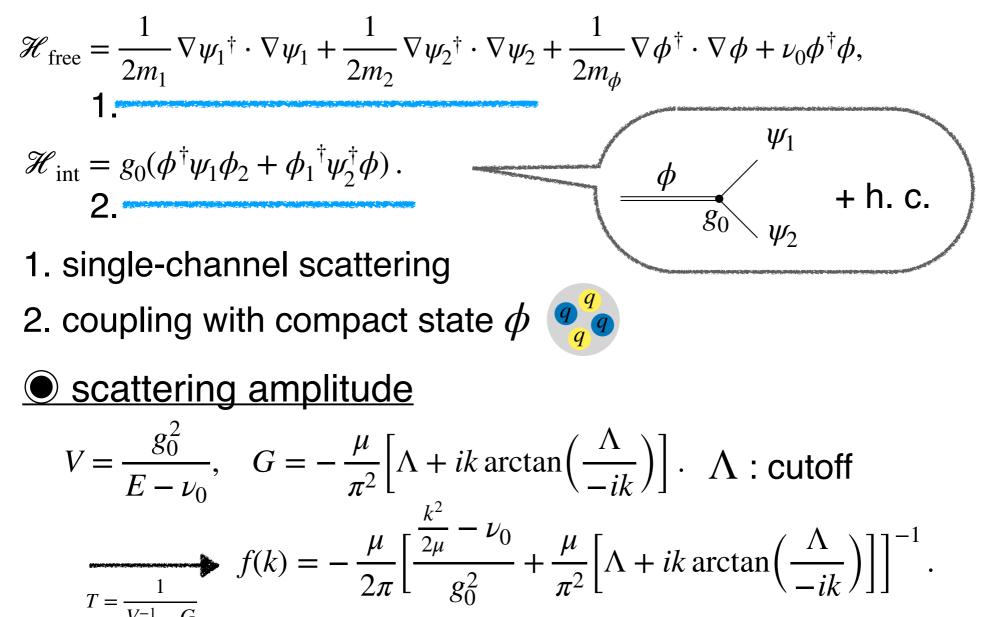
LHCb Collaboration, Nat. Commun 13 3351 (2022).

other ch. than threshold ch. make deviation from X = 1Y. Kamiya and T. Hyodo, PTEP 2017, 023D02 (2017).

This work... study those deviations quantitatively!

# Model

#### Single-channel resonance model



## Model scales and parameters

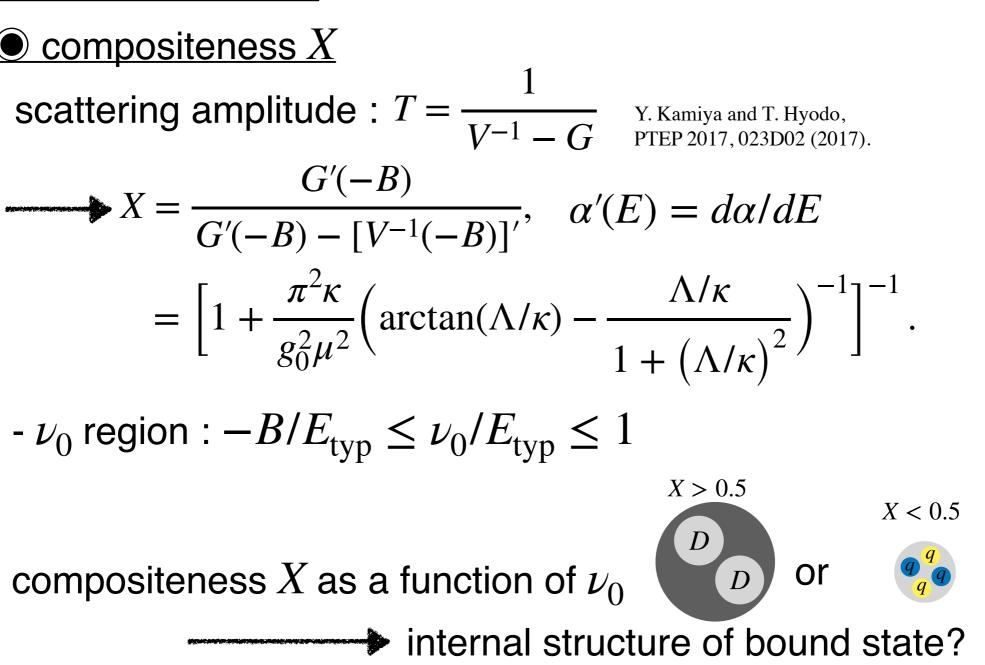
- typical energy scale :  $E_{\rm typ} = \Lambda^2/(2\mu)$
- three model parameters  $g_0,\nu_0,\Lambda$
- 1. calculation with given B

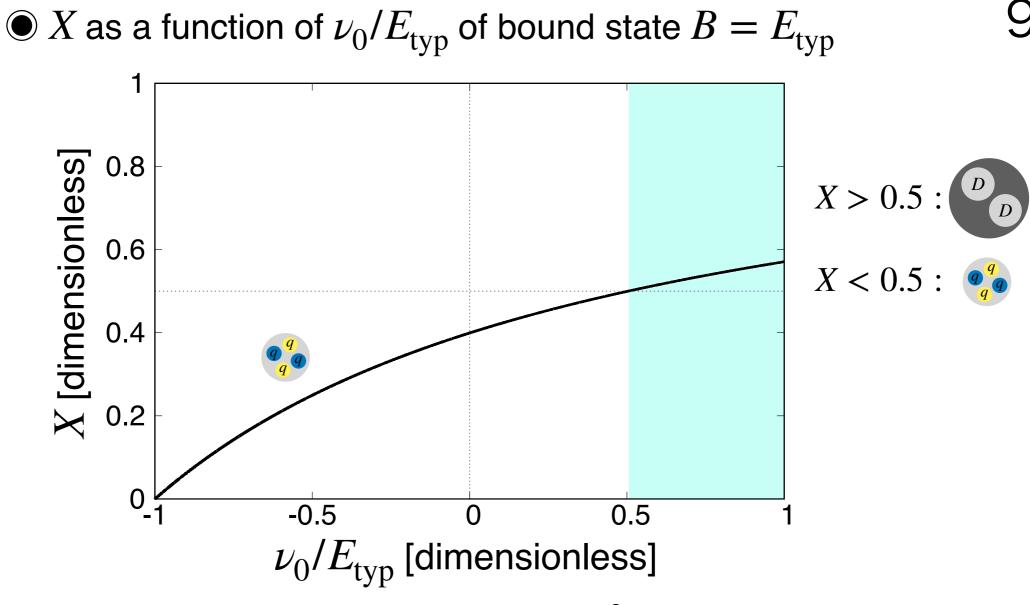
coupling const.  $g_0$ :  $g_0^2(B, \nu_0, \Lambda) = \frac{\pi^2}{\mu} (B + \nu_0) \left[ \Lambda - \kappa \arctan(\Lambda/\kappa) \right]^{-1}$ 

- : bound state condition  $f^{-1} = 0$   $\kappa = \sqrt{2\mu B}$ .
- 2. use dimensionless quantities with  $\Lambda$

varied in the region :  $-B/E_{typ} \le \nu_0/E_{typ} \le 1$  $\therefore$  to have  $g_0^2 \ge 0$  & applicable limit of EFT

## Calculation

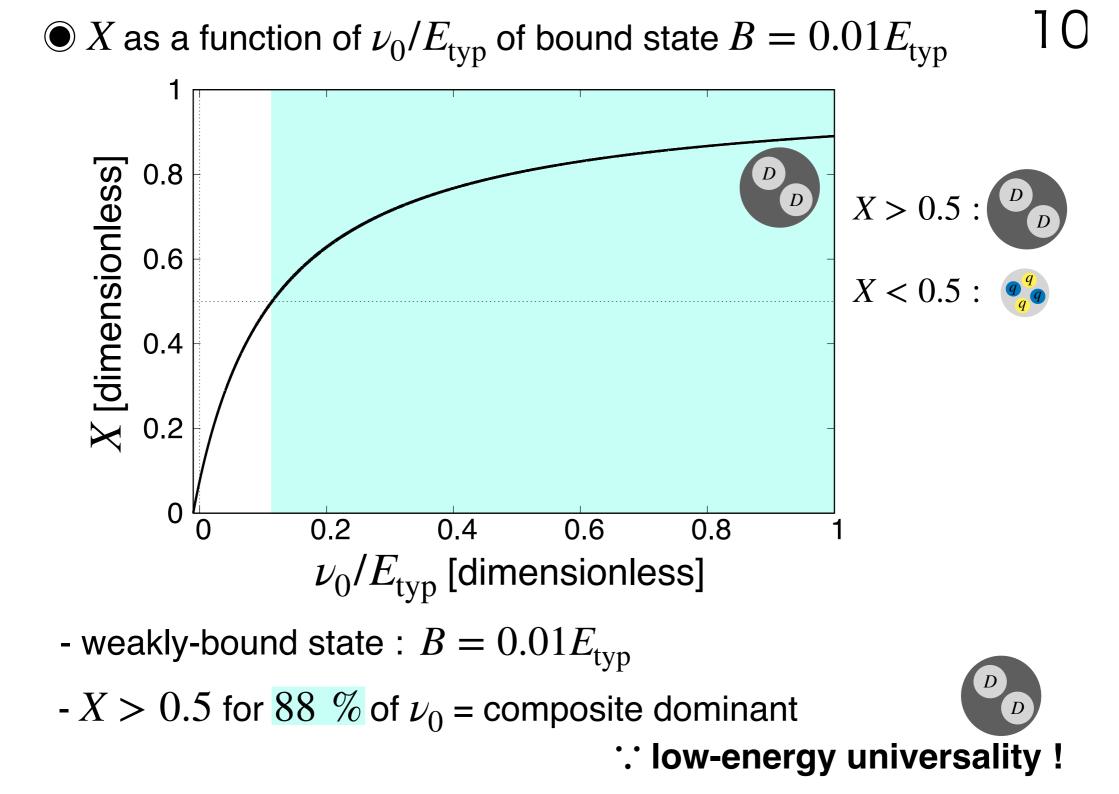




- typical energy scale :  $B = E_{typ} = \Lambda^2/(2\mu)$ 

- X > 0.5 only for 25 % of  $\nu_0$  = elementary dominant  $\P^q$ 

: bare state origin



## Effect of decay

Introducing decay effect

- formally : introducing decay channel in lower energy region than binding energy

-----> eigenenergy becomes complex

- effectively : coupling const.  $g_0 \in \mathbb{C}$ 

$$E = -B \longrightarrow E = -B - i\Gamma/2$$

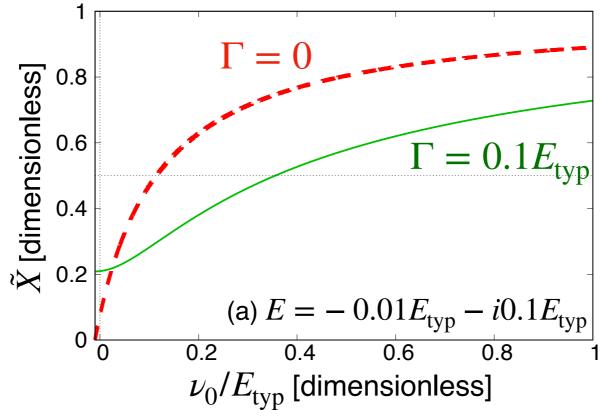
compositeness

$$X \in \mathbb{R} \longrightarrow X \in \mathbb{C}$$

$$\tilde{X} = \frac{|X|}{|X| + |1 - X|}$$
 T. Sekihara, *et. al.*, PRC 93, 035204 (2016).

## Effect of decay

#### O compositeness $\tilde{X}$



-  $\tilde{X}$  is suppressed by  $\Gamma \neq 0$ 

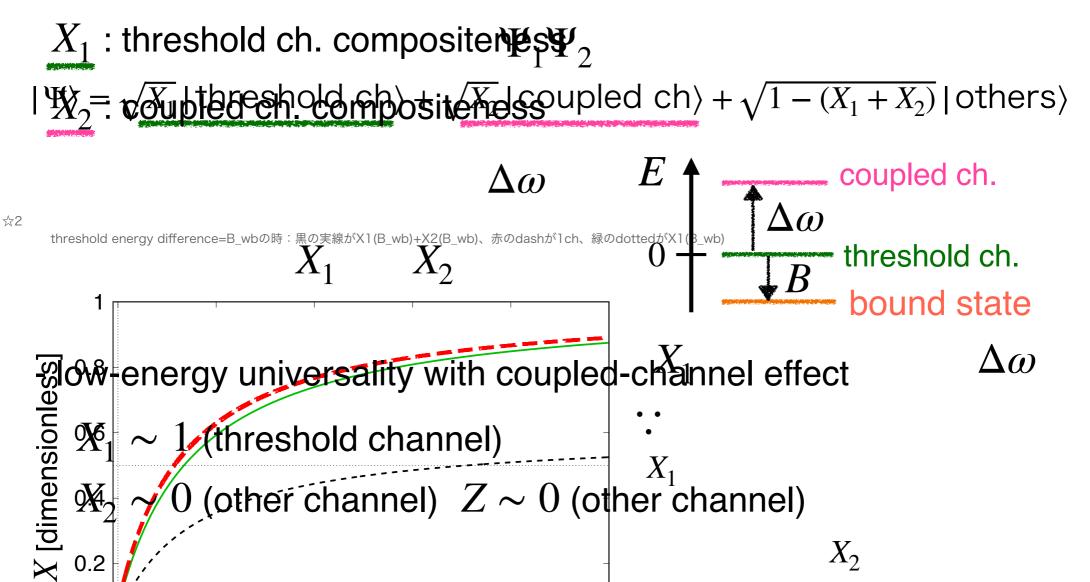
: threshold ch. component  $(\tilde{X})$  decreases with inclusion of decay ch. component  $(1 - \tilde{X})$ 

## Effect of coupled channel

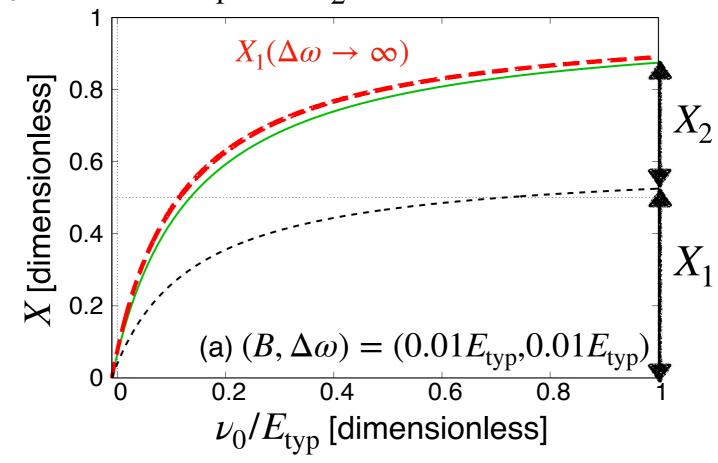
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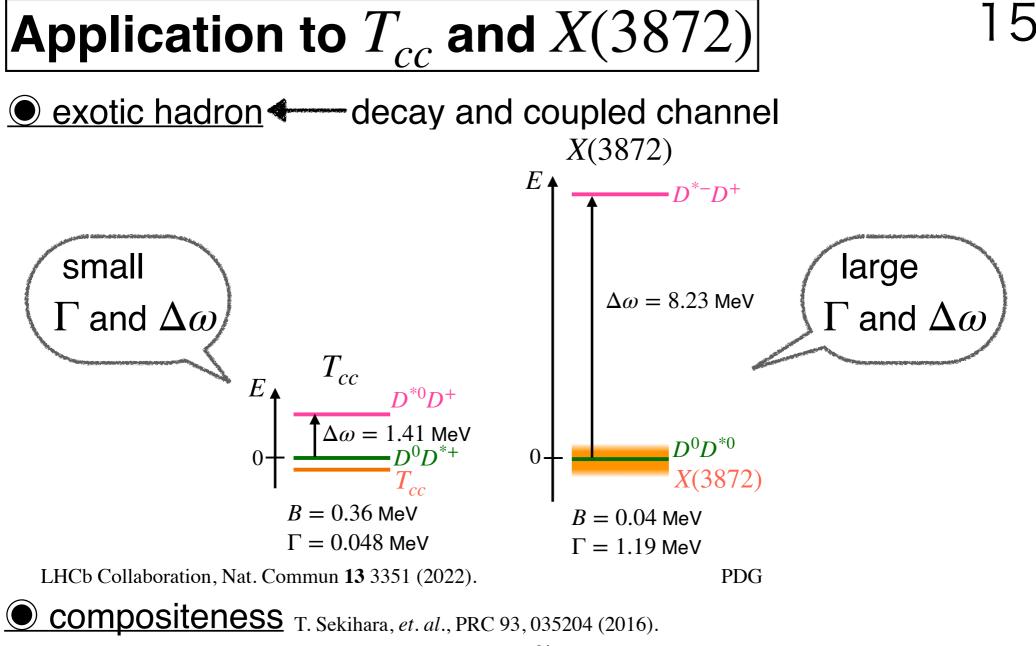
**Effect** of coupled  $\sqrt{champled}$  ch +  $\sqrt{1 - (X_1 + X_2)}$  | others)



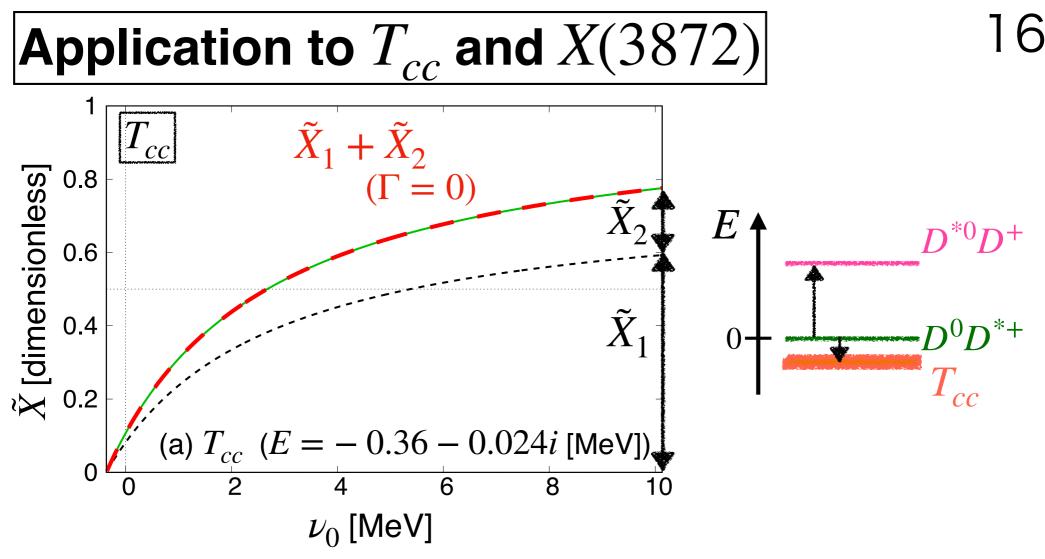
#### Effect of coupled channel



- $X_1$  is suppressed by  $\Delta \omega$ 
  - : threshold ch. component  $(X_1)$  decreases with inclusion of coupled ch. component  $(X_2)$



$$\tilde{X}_{j} = \frac{|X_{j}|}{\sum_{j} |X_{j}| + |Z|}, \quad (j = 1, 2) \quad \frac{\tilde{X}_{1}}{\tilde{X}_{2}} : \text{threshold ch. compositeness}$$



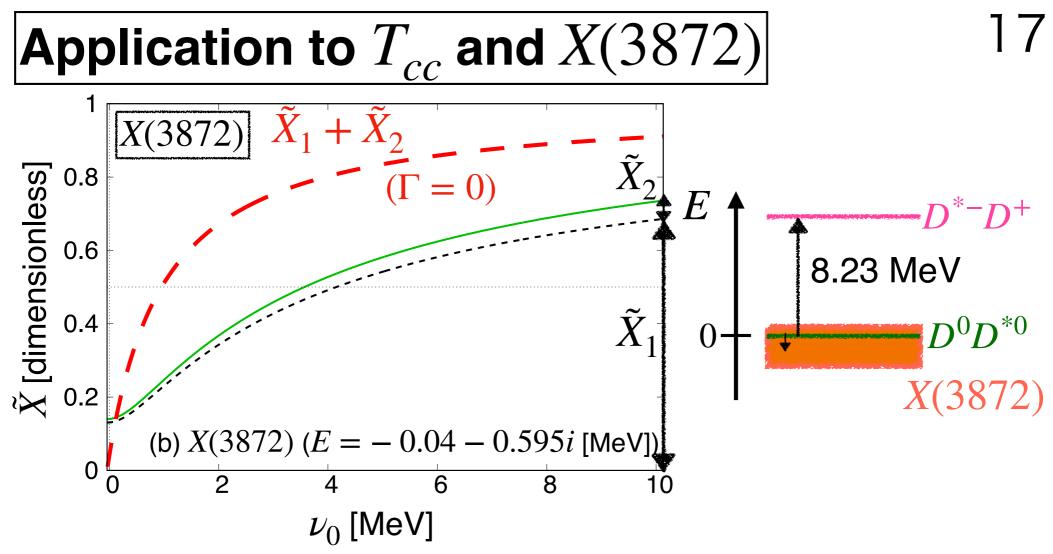
-  $\tilde{X}_2$  is not negligible

 $\therefore$  coupled ch. contribution (small  $\Delta \omega$ )

- difference of  $\tilde{X}_1 + \tilde{X}_2 (\Gamma = 0)$  and  $\tilde{X}_1 + \tilde{X}_2$  is too small

----> We can neglect decay contribution

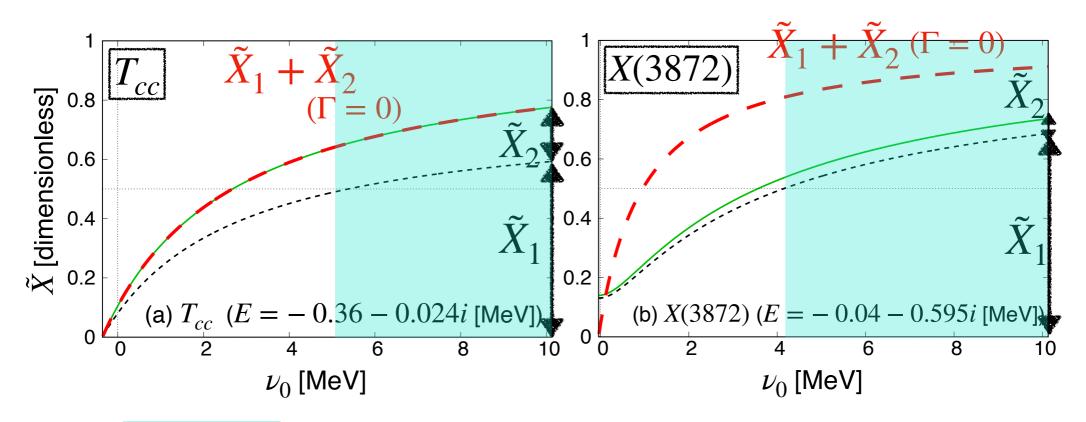
 $\therefore \Gamma \ll B$ 



- difference of  $\tilde{X}_1 + \tilde{X}_2(\Gamma = 0)$  and  $\tilde{X}_1 + \tilde{X}_2$  is large

- : large decay width contribution
- $\tilde{X}_2$  is much smaller than  $\tilde{X}_1$ 
  - coupled ch. effect is small

## **Application to** $T_{cc}$ and X(3872)



-  $T_{cc}$  :  $\tilde{X}_1 > 0.5$  for 55 % of  $\nu_0$  region

- X(3872) :  $\tilde{X}_1 > 0.5$  for 41~% of  $\nu_0$  region
- coupled ch. effect is more important for  $T_{cc}$  than X(3872)
- decay effect is more important for X(3872) than  $T_{cc}$

- model with bare state coupled to the scattering state
- shallow bound state is composite dominant even from bare state
  - : low-energy universality
- decay and coupled channel effects are introduced
  - both decay and coupled ch. effect suppress compositeness

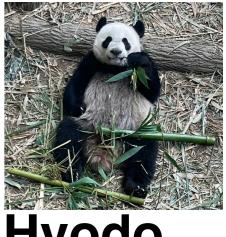
- X of  $T_{cc}$  and X(3872) are calculated with decay and coupled ch. effects

 $T_{cc}$ : important coupled ch. effect with negligible decay effect X(3872) : important decay effect with negligible coupled ch. effect

# Compositeness of exotic hadrons with decay and coupled-channel effects



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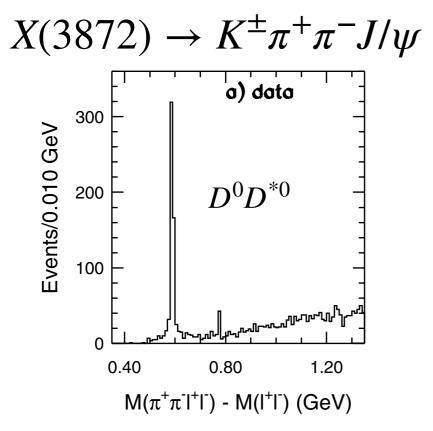


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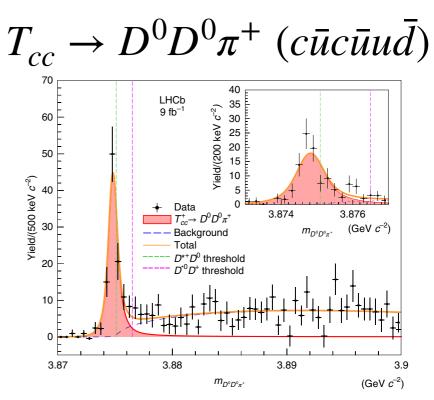
## Tetsuo Hyodo

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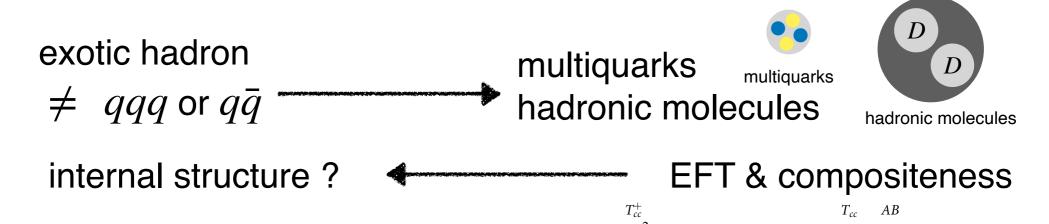
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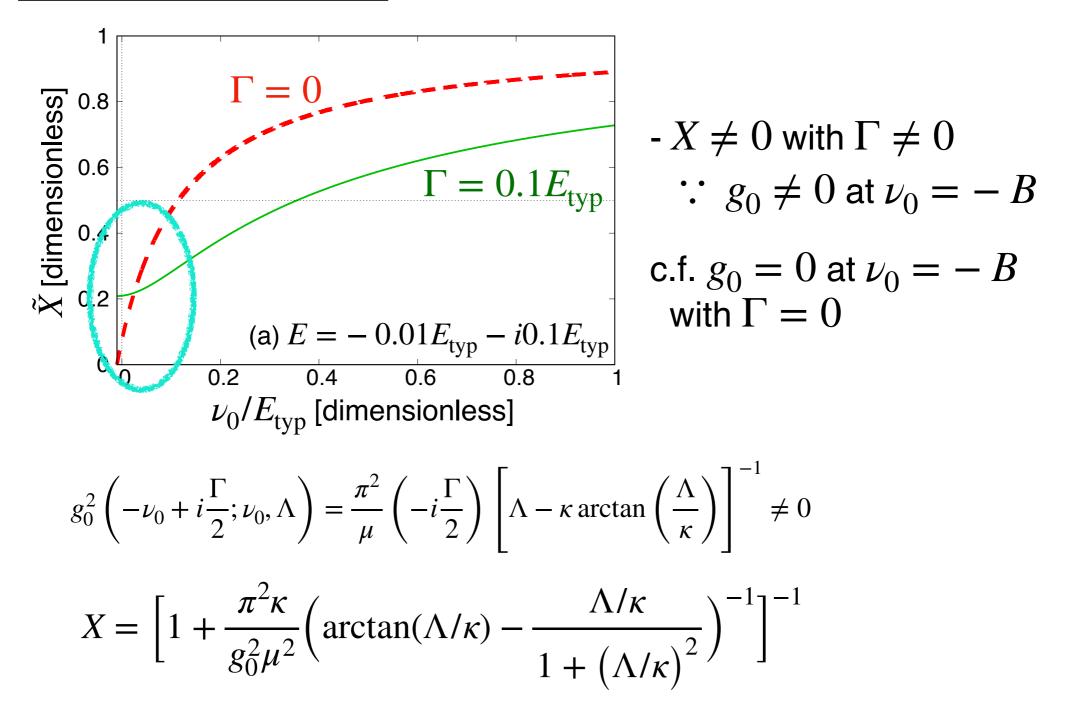
S. K. Choi et al. (Belle), Phys. Rev. Lett. 91, 262001 (2003).



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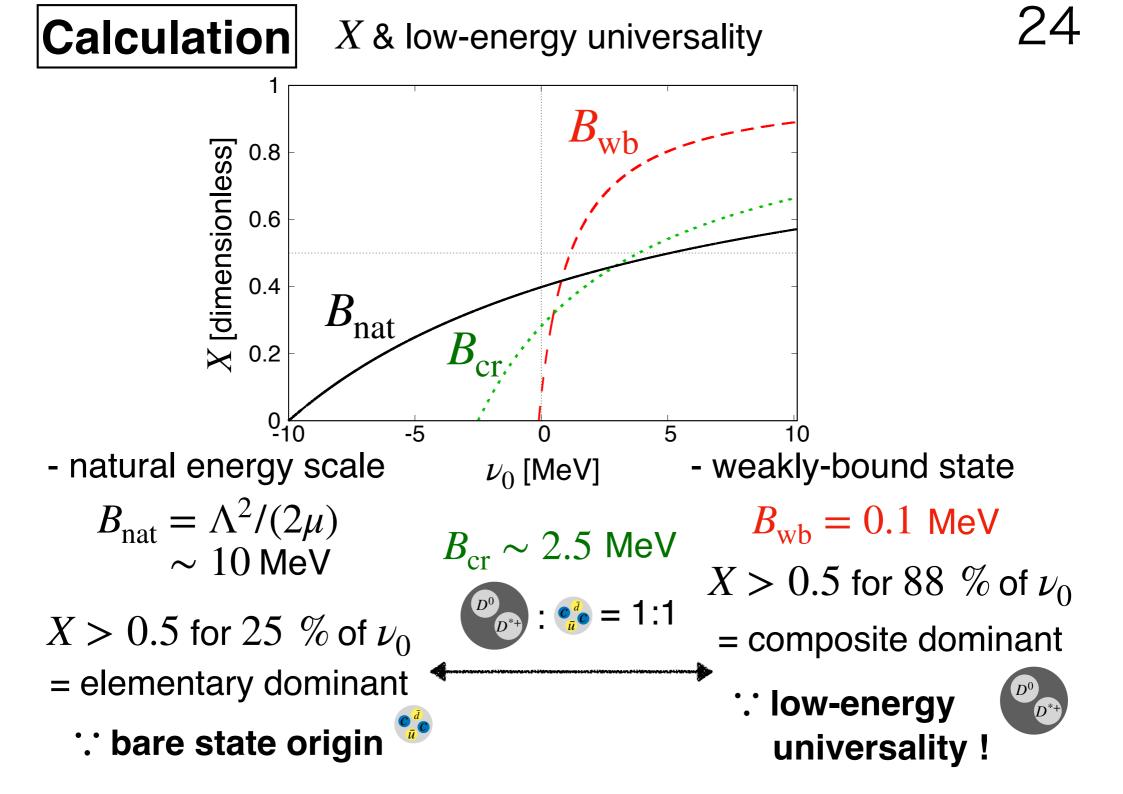


#### Effect of decay

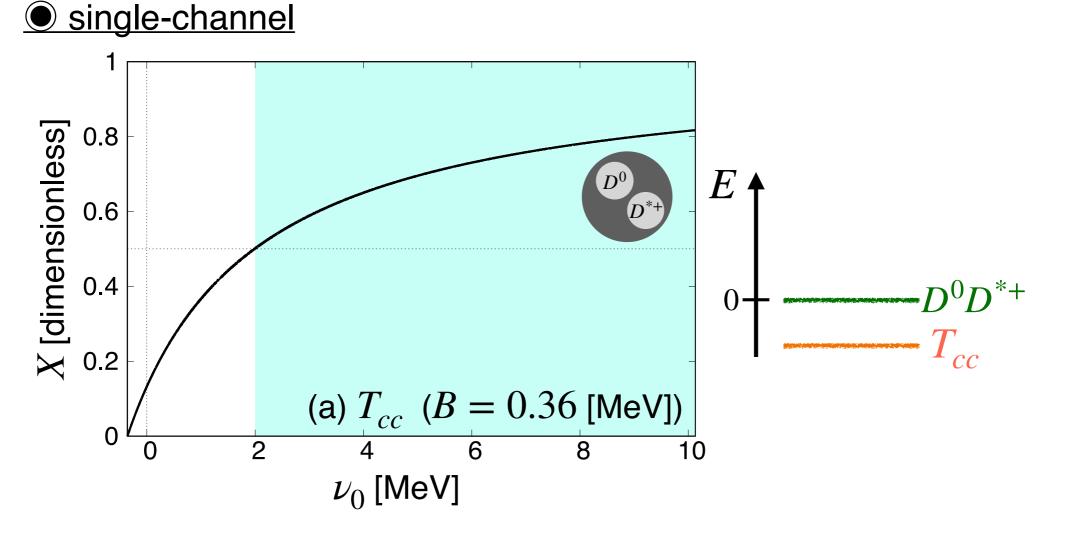


#### **Compositeness for two-channel case**

$$\begin{split} X_1 &= \frac{G_1'}{(G_1' + G_2') - [v^{-1}]'}, \\ X_2 &= \frac{G_2'}{(G_1' + G_2') - [v^{-1}]'}. \end{split}$$







- X > 0.5 for 78 % of  $\nu_0$  = composite dominant

- fine tuning is necessary to realize X < 0.5