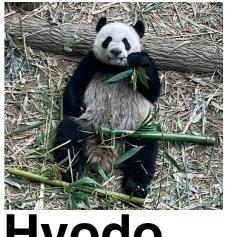
Compositeness of exotic hadrons with decay and coupled-channel effects



arXiv:2303.07038 [hep-ph]

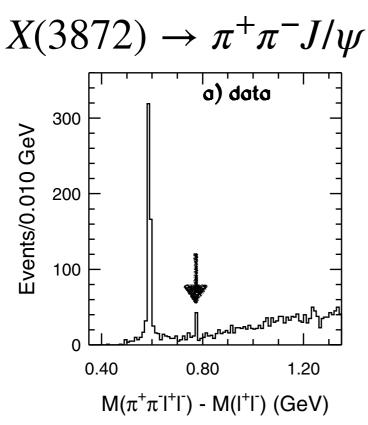


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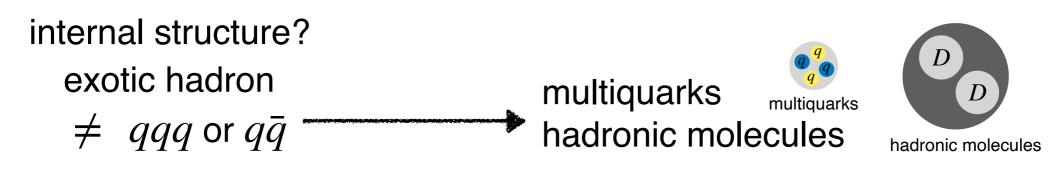
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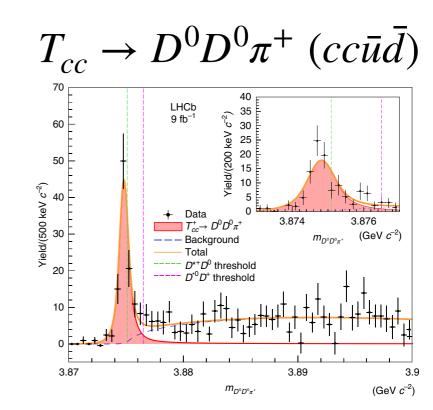
Near-threshold exotic hadrons

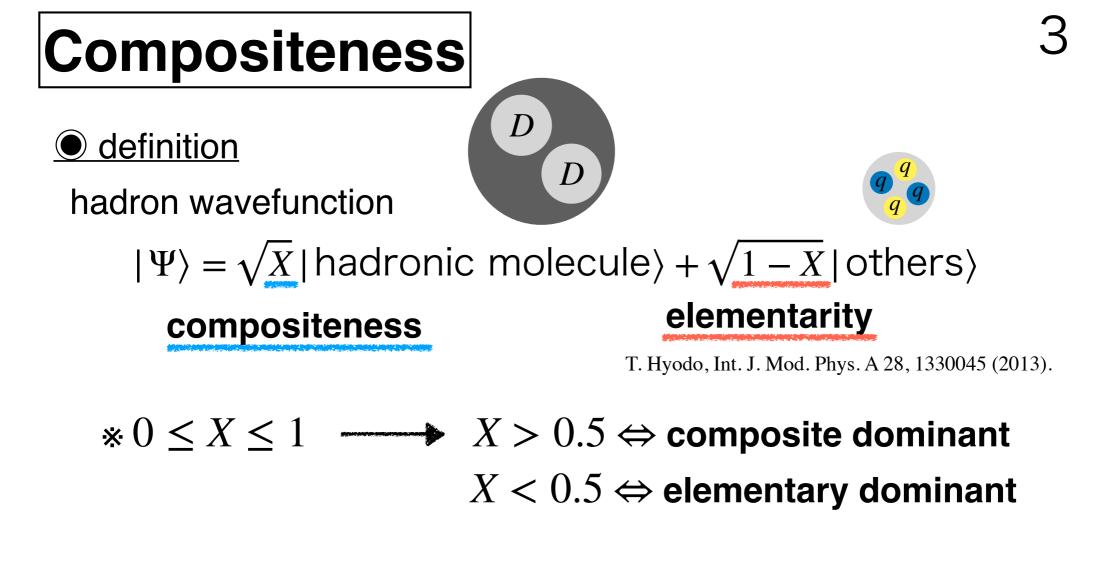




LHCb Collaboration, Nature Phys. **18** (2022) no.7, 751-754; LHCb Collaboration, Nat. Commun. **13** 3351 (2022).







model calculation

T. Hyodo, D. Jido, and A. Hosaka, Phys. Rev. C 85, 015201 (2012);F. Aceti and E. Oset, Phys. Rev. D 86, 014012 (2012).

compositeness X ----- residue of scattering amplitude

Low-energy universality

- scattering length $a_0 \gg$ typical length scale of system $R_{\rm typ}$

low-energy universality

E. Braaten and H.-W. Hammer, Phys. Rept. 428, 259 (2006);F. P. Naidon and S. Endo, Rept. Prog. Phys. 80, 056001 (2017).

 \longrightarrow length scales are written only by $|a_0|(\rightarrow \infty)$

for bound states ?

$$a_0 = R$$
 $R = 1/\sqrt{2\mu B}$ $a_0 \to \infty \longrightarrow B \to 0$

universality holds for weakly-bound states!!

- compositeness X = 1 in $B \rightarrow 0$ limit _{T. Hyodo, Phys. Rev. C 90, 055208 (2014)}.

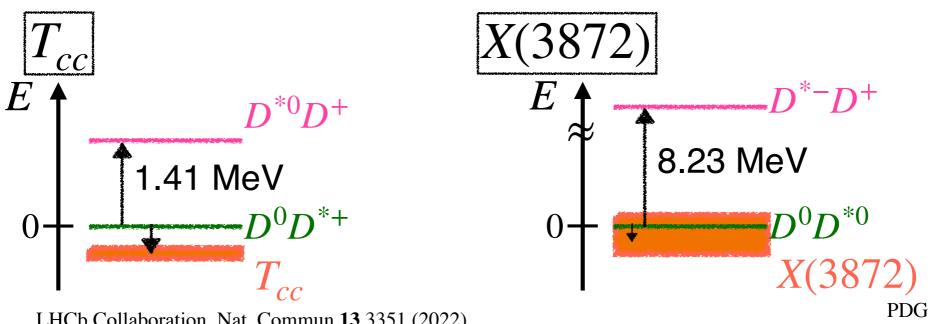
near threshold poles = composite dominant ?

e.g. ⁸Be, ¹²C $\rightarrow \alpha$ cluster? H. Horiuchi, K. Ikeda, and Y. Suzuki, Prog. Theor. Phys. Suppl. 52, 89 (1972).

Decay & coupled ch. effects

However...

actual exotic hadrons ---decay and coupled channel



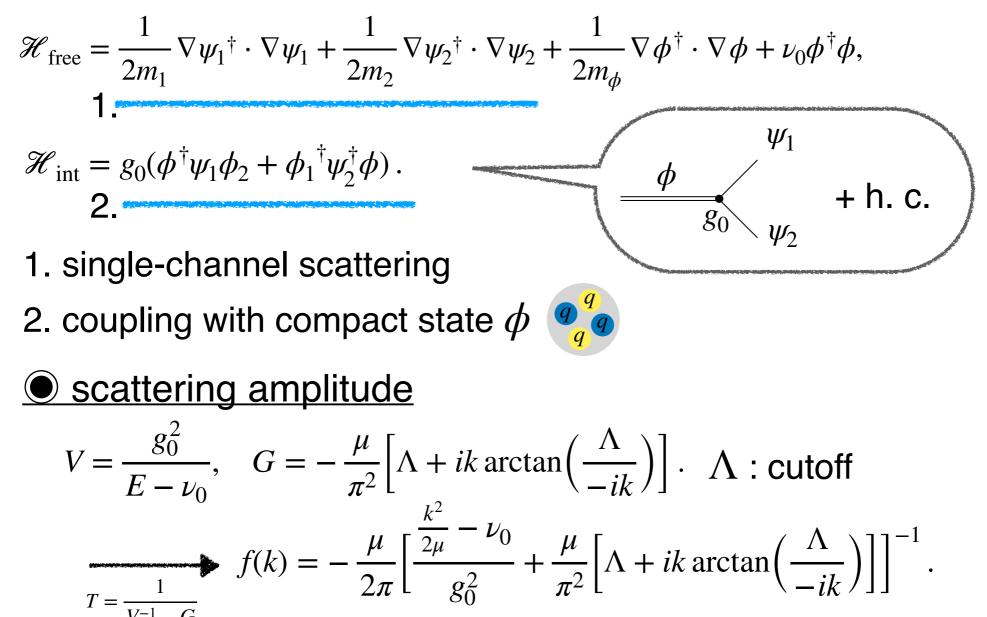
LHCb Collaboration, Nat. Commun 13 3351 (2022).

other ch. than threshold ch. make deviation from X = 1Y. Kamiya and T. Hyodo, PTEP 2017, 023D02 (2017).

This work... study those deviations quantitatively!

Model

Single-channel resonance model



Model scales and parameters

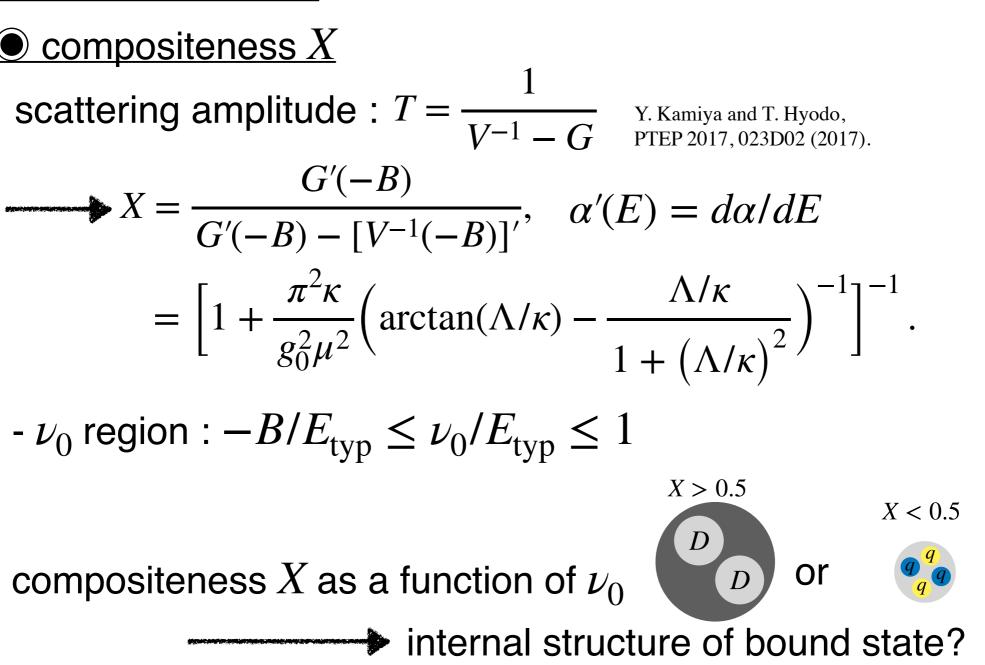
- typical energy scale : $E_{\rm typ} = \Lambda^2/(2\mu)$
- three model parameters g_0,ν_0,Λ
- 1. calculation with given B

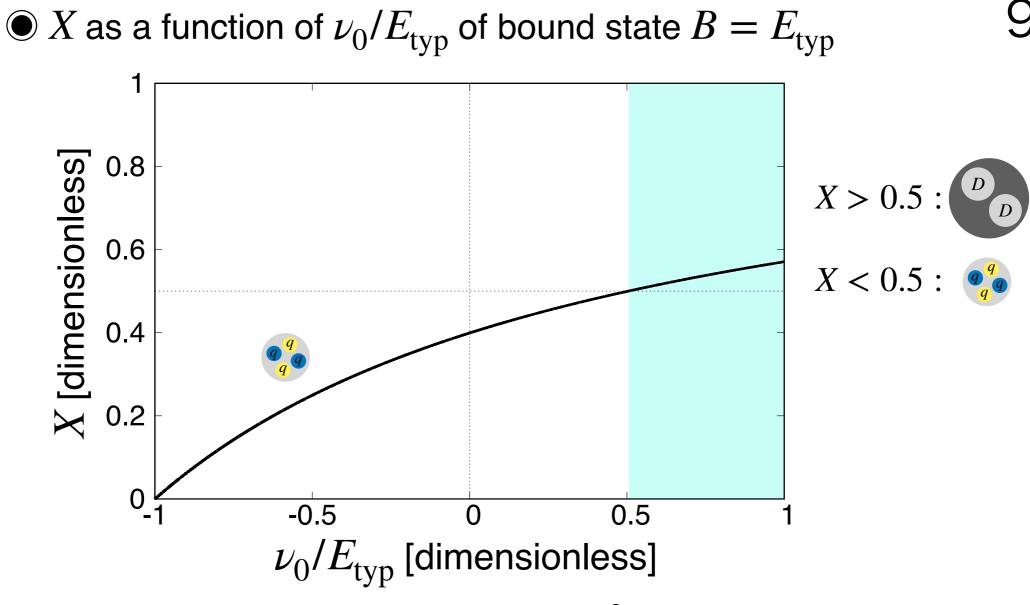
coupling const. g_0 : $g_0^2(B, \nu_0, \Lambda) = \frac{\pi^2}{\mu} (B + \nu_0) \left[\Lambda - \kappa \arctan(\Lambda/\kappa) \right]^{-1}$

- : bound state condition $f^{-1} = 0$ $\kappa = \sqrt{2\mu B}$.
- 2. use dimensionless quantities with Λ

varied in the region : $-B/E_{typ} \le \nu_0/E_{typ} \le 1$ \therefore to have $g_0^2 \ge 0$ & applicable limit of EFT

Calculation

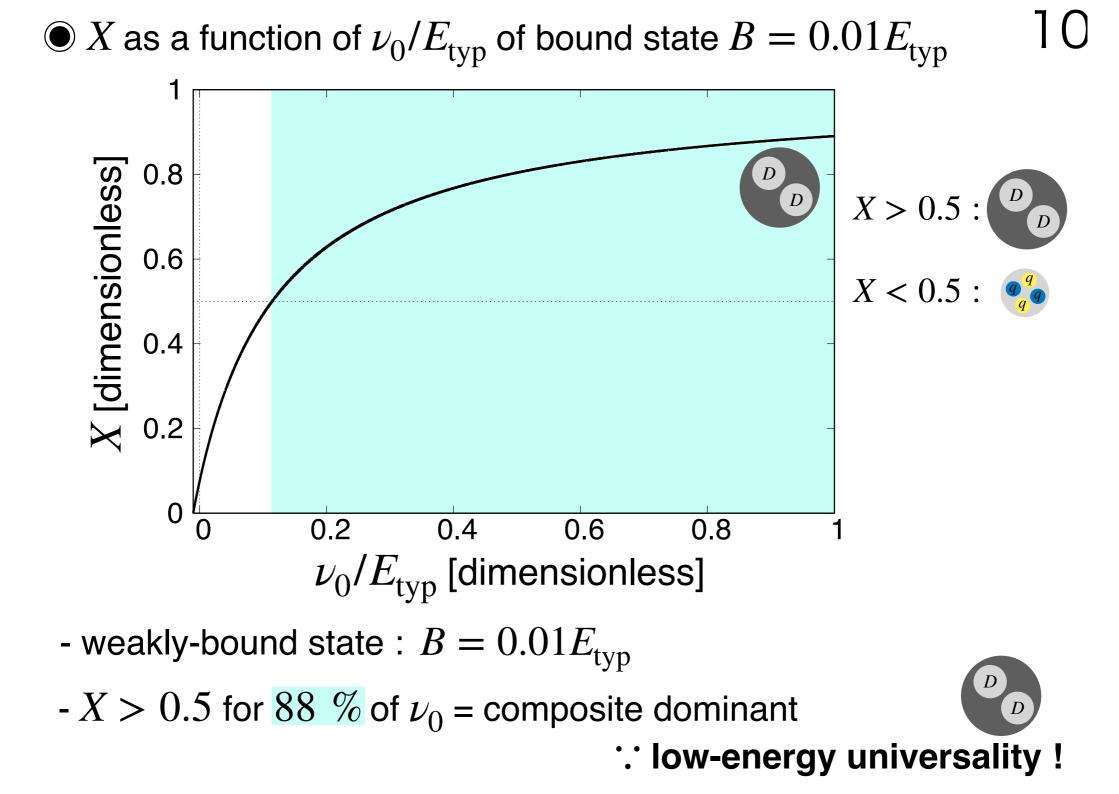




- typical energy scale : $B = E_{typ} = \Lambda^2/(2\mu)$

- X > 0.5 only for 25 % of ν_0 = elementary dominant \P^q

: bare state origin



Effect of decay

Introducing decay effect

- formally : introducing decay channel in lower energy region than binding energy

-----> eigenenergy becomes complex

- effectively : coupling const. $g_0 \in \mathbb{C}$

$$E = -B \longrightarrow E = -B - i\Gamma/2$$

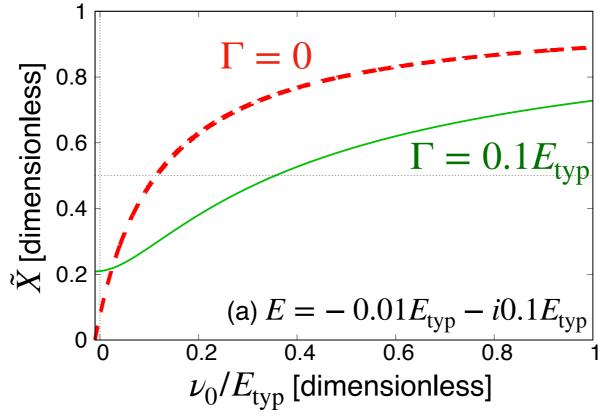
compositeness

$$X \in \mathbb{R} \longrightarrow X \in \mathbb{C}$$

$$\tilde{X} = \frac{|X|}{|X| + |1 - X|}$$
 T. Sekihara, *et. al.*, PRC 93, 035204 (2016).

Effect of decay

O compositeness \tilde{X}



- \tilde{X} is suppressed by $\Gamma \neq 0$

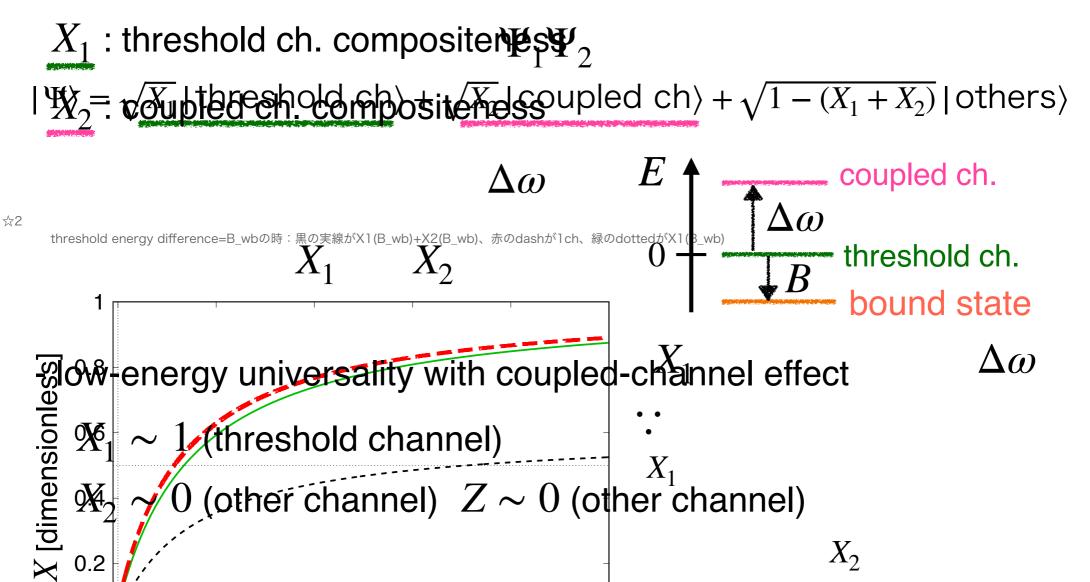
: threshold ch. component (\tilde{X}) decreases with inclusion of decay ch. component $(1 - \tilde{X})$

Effect of coupled channel

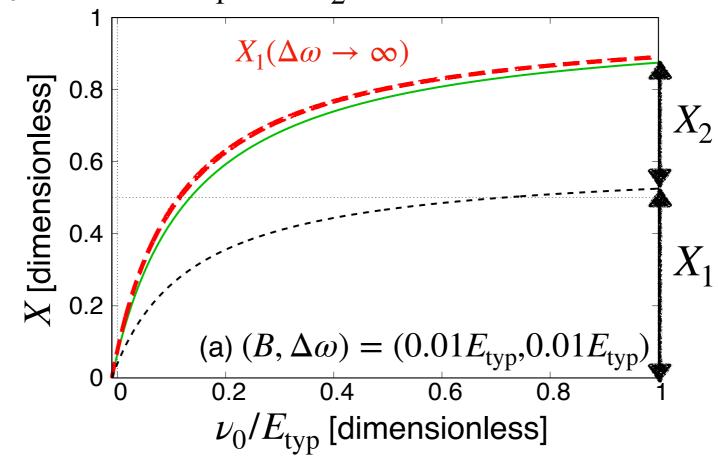
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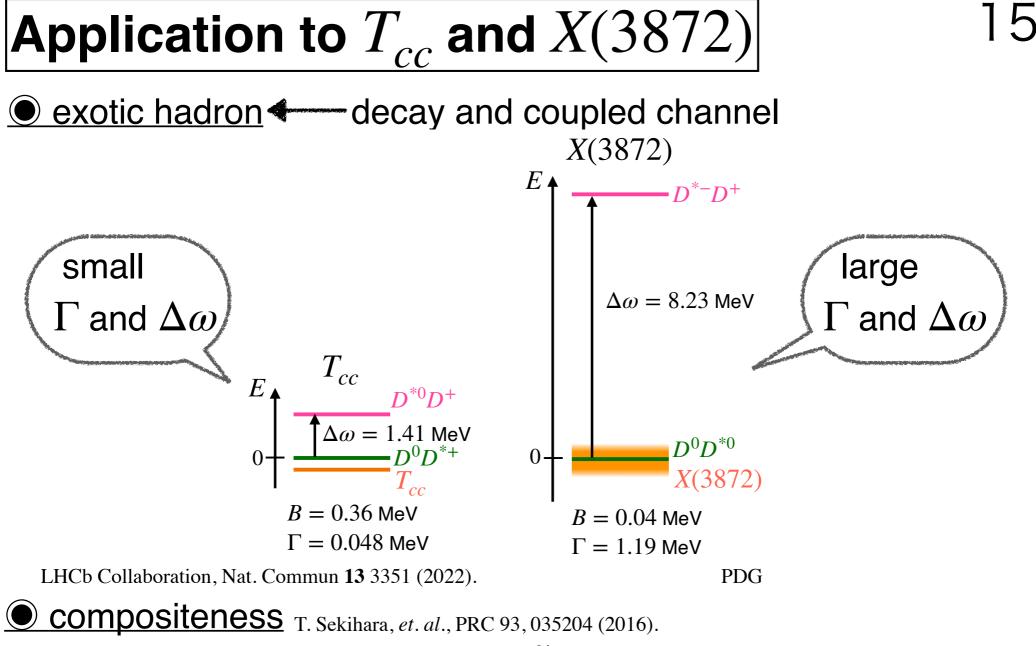
Effect of coupled $\sqrt{champled}$ ch + $\sqrt{1 - (X_1 + X_2)}$ | others)



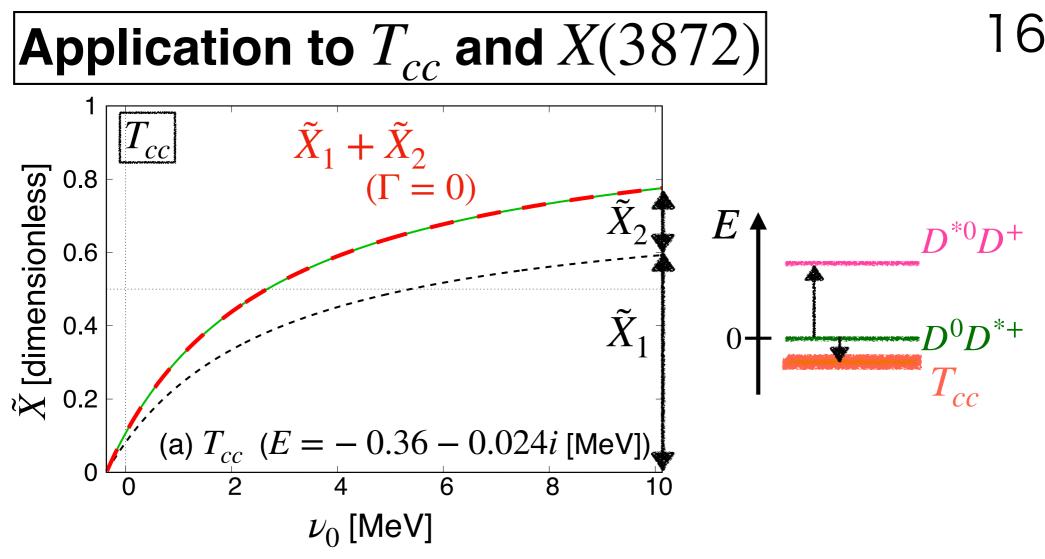
Effect of coupled channel



- X_1 is suppressed by $\Delta \omega$
 - : threshold ch. component (X_1) decreases with inclusion of coupled ch. component (X_2)



$$\tilde{X}_{j} = \frac{|X_{j}|}{\sum_{j} |X_{j}| + |Z|}, \quad (j = 1, 2) \quad \frac{\tilde{X}_{1}}{\tilde{X}_{2}} : \text{threshold ch. compositeness}$$



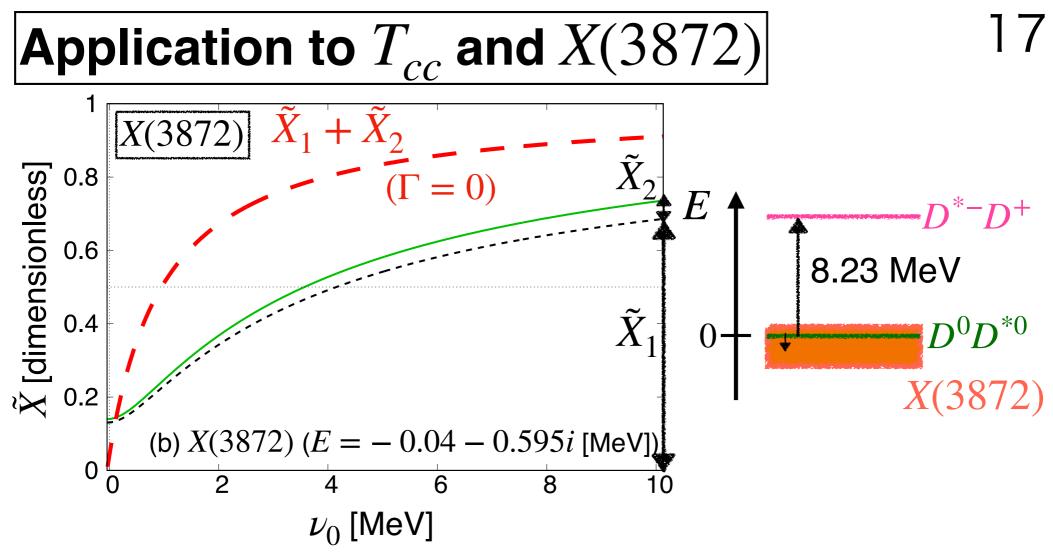
- \tilde{X}_2 is not negligible

 \therefore coupled ch. contribution (small $\Delta \omega$)

- difference of $\tilde{X}_1 + \tilde{X}_2 (\Gamma = 0)$ and $\tilde{X}_1 + \tilde{X}_2$ is too small

----> We can neglect decay contribution

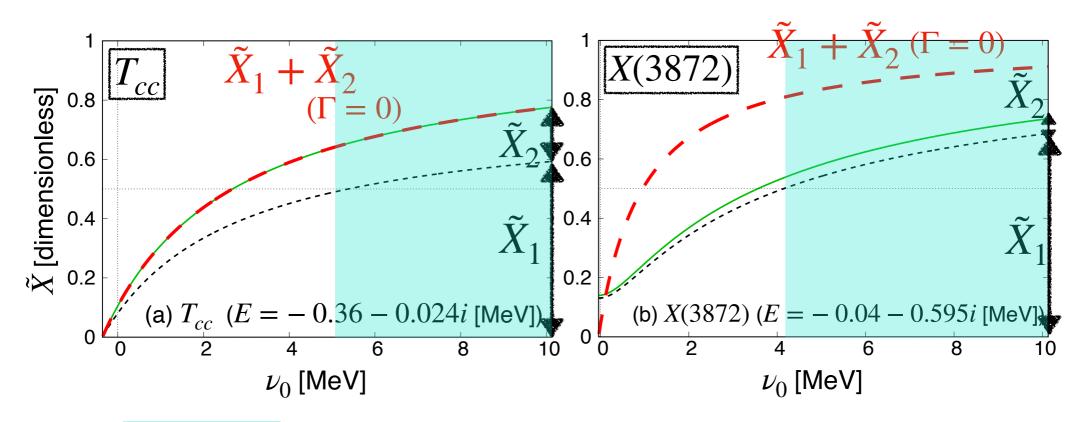
 $\therefore \Gamma \ll B$



- difference of $\tilde{X}_1 + \tilde{X}_2(\Gamma = 0)$ and $\tilde{X}_1 + \tilde{X}_2$ is large

- : large decay width contribution
- \tilde{X}_2 is much smaller than \tilde{X}_1
 - coupled ch. effect is small

Application to T_{cc} and X(3872)



- T_{cc} : $\tilde{X}_1 > 0.5$ for 55 % of ν_0 region

- X(3872) : $\tilde{X}_1 > 0.5$ for 41~% of ν_0 region
- coupled ch. effect is more important for T_{cc} than X(3872)
- decay effect is more important for X(3872) than T_{cc}

- model with bare state coupled to the scattering state
- shallow bound state is composite dominant even from bare state
 - : low-energy universality
- decay and coupled channel effects are introduced
 - both decay and coupled ch. effect suppress compositeness

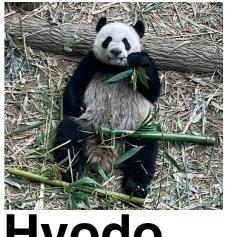
- X of T_{cc} and X(3872) are calculated with decay and coupled ch. effects

 T_{cc} : important coupled ch. effect with negligible decay effect X(3872) : important decay effect with negligible coupled ch. effect

Compositeness of exotic hadrons with decay and coupled-channel effects



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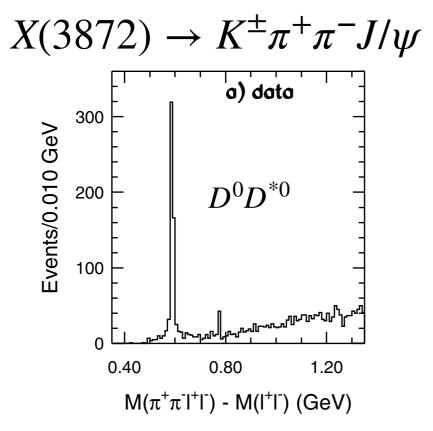


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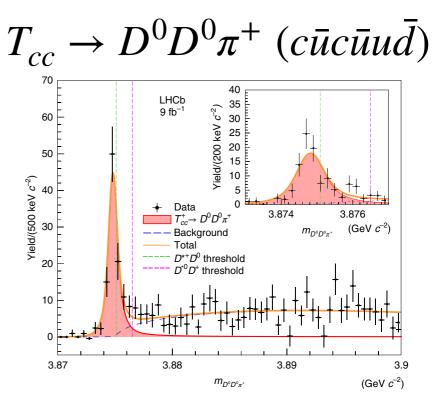
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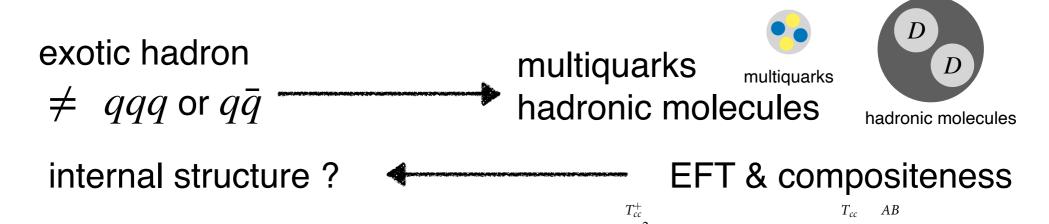
Near-threshold exotic hadrons



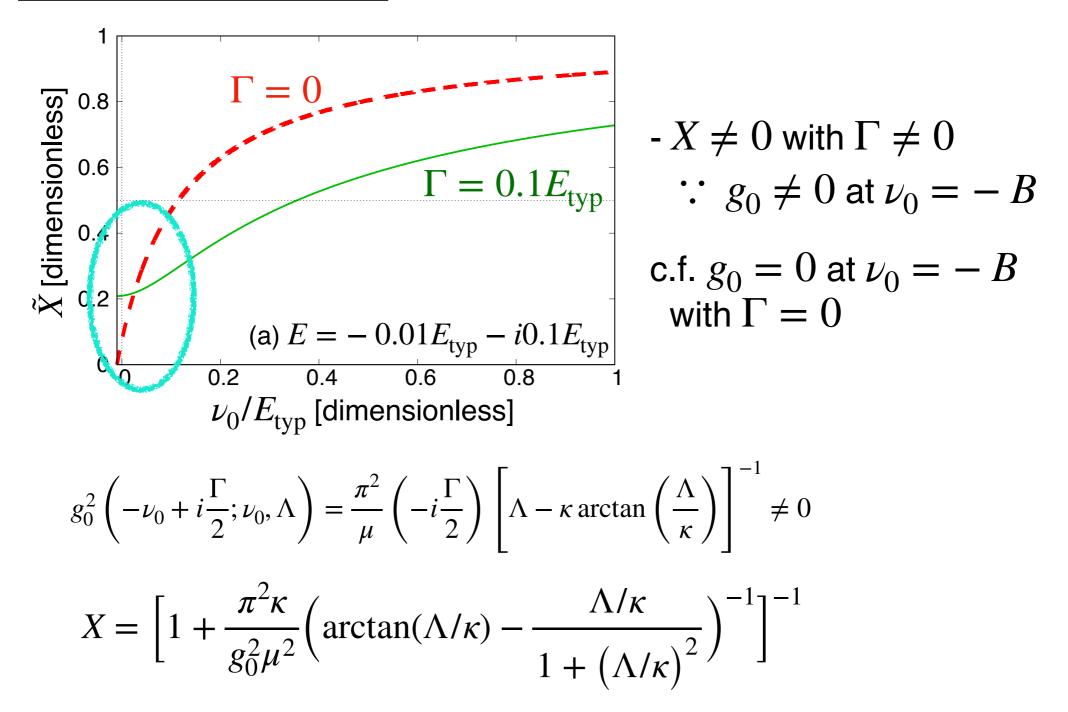
S. K. Choi et al. (Belle), Phys. Rev. Lett. 91, 262001 (2003).



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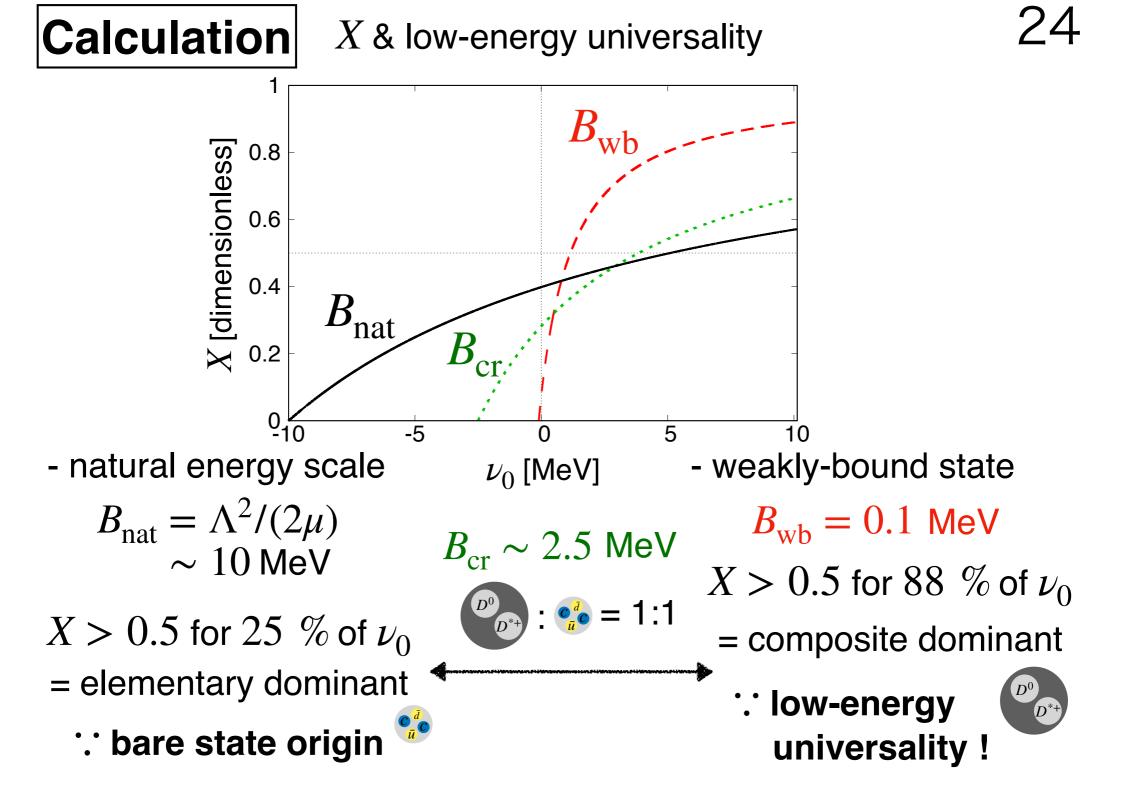


Effect of decay

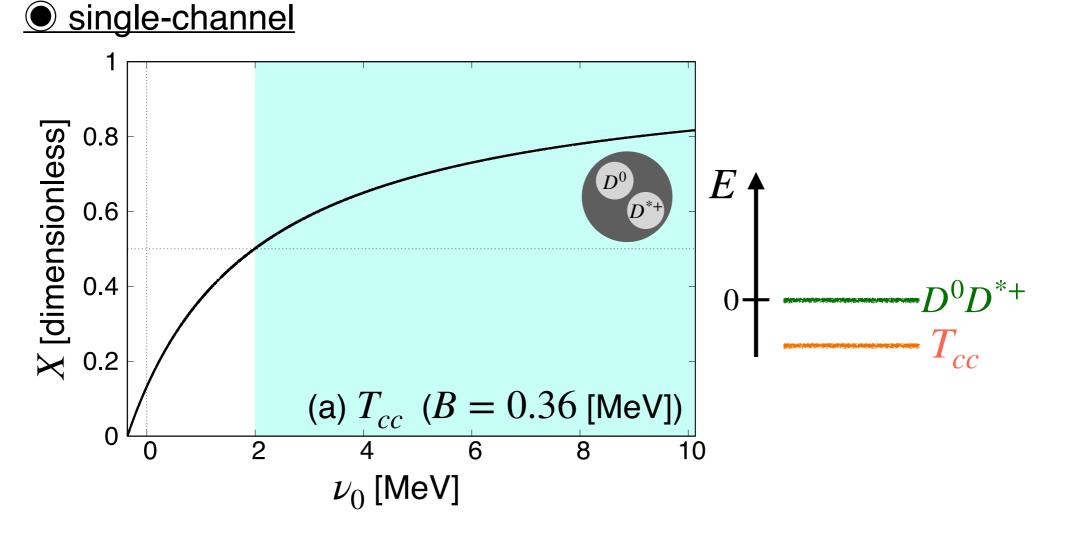


Compositeness for two-channel case

$$\begin{split} X_1 &= \frac{G_1'}{(G_1' + G_2') - [v^{-1}]'}, \\ X_2 &= \frac{G_2'}{(G_1' + G_2') - [v^{-1}]'}. \end{split}$$







- X > 0.5 for 78 % of ν_0 = composite dominant

- fine tuning is necessary to realize X < 0.5