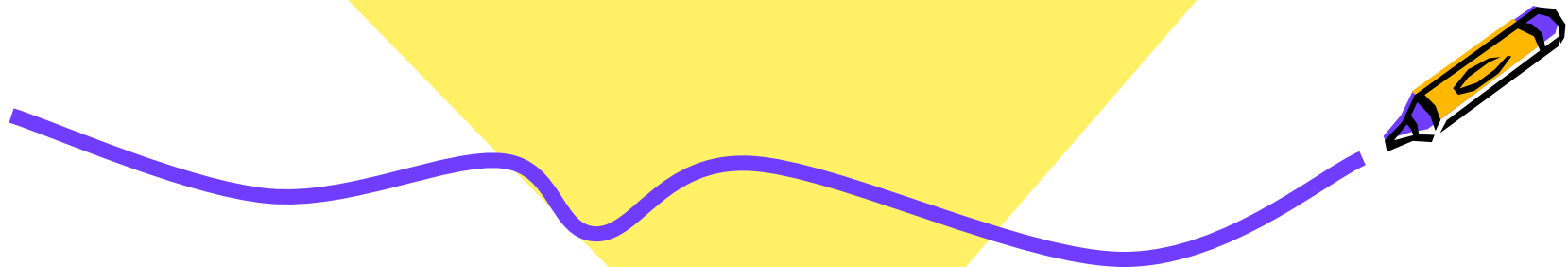




# Reaction cross sections of carbon isotopes Incident on proton and $^{12}\text{C}$ target

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A. Kohama (RIKEN Nishina Center) and Y. Suzuki (Niigata U.)



2007/5/30

**C+C: Phys. Rev. C 75, 044607 (2007).  
C+p: to be submitted.**

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Summary

Motivation:

Measurements of p-22C  
(Next talk by Tanaka-  
san)

Reaction mechanism

# Descript. of $p$ - $A$ reactions

- Glauber approxi.

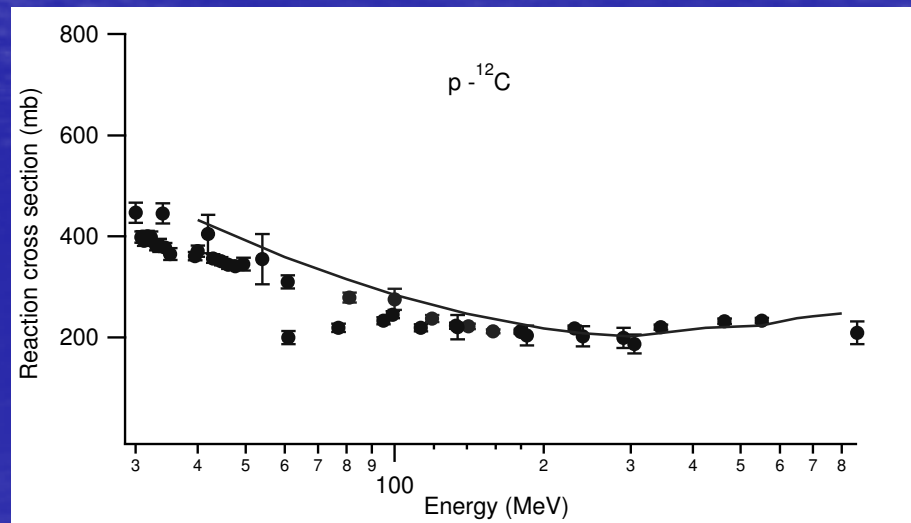
$$\sigma_R = \int db \left( 1 - |e^{i\chi(b)}|^2 \right)$$

$$e^{i\chi(b)} = \left\langle \Psi_0 \left| \prod_{i \in P} (1 - \Gamma_{pi}(b + s_i)) \right| \Psi_0 \right\rangle$$

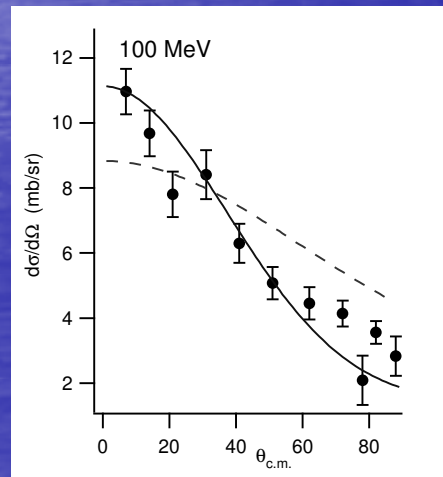
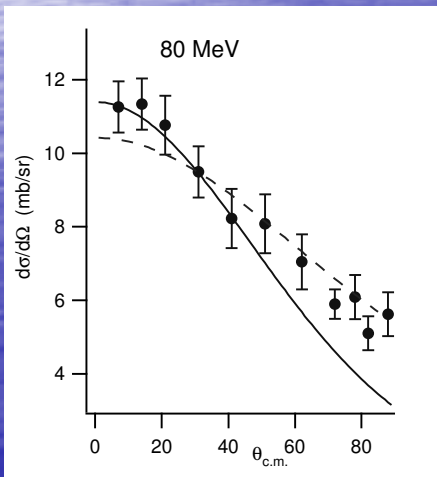
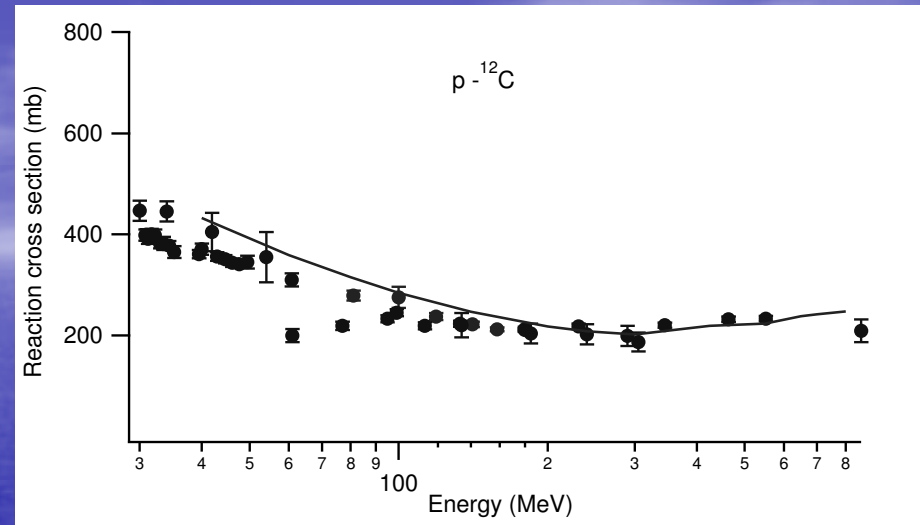
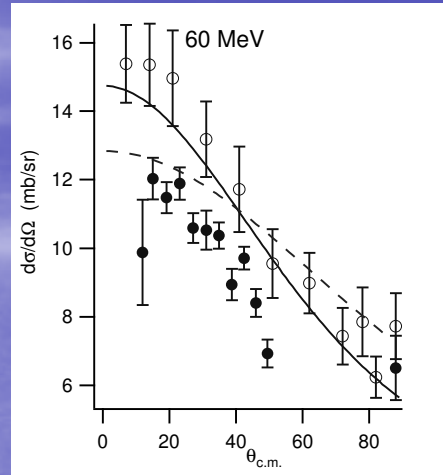
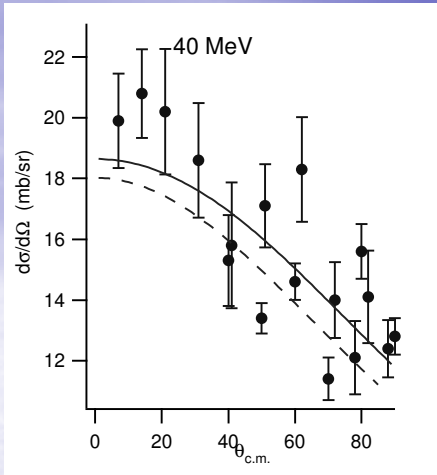
$$\begin{aligned} e^{i\chi_{OLA}(b)} &= e^{i\chi_n(b) + i\chi_p(b)} \\ &= e^{-\int dr [\rho_n(r)\Gamma_{pn}(b+s) + \rho_p(r)\Gamma_{pp}(b+s)]} \end{aligned}$$

$$\Gamma_{pi}(b) = \frac{1 - i\alpha_{pi}}{4\pi\beta_{pi}} \sigma_{pi}^{tot} \exp\left(\frac{b^2}{2\beta_{pi}}\right)$$

- $\sigma_R$  of  $p$ - $^{12}\text{C}$



# pn-scattering

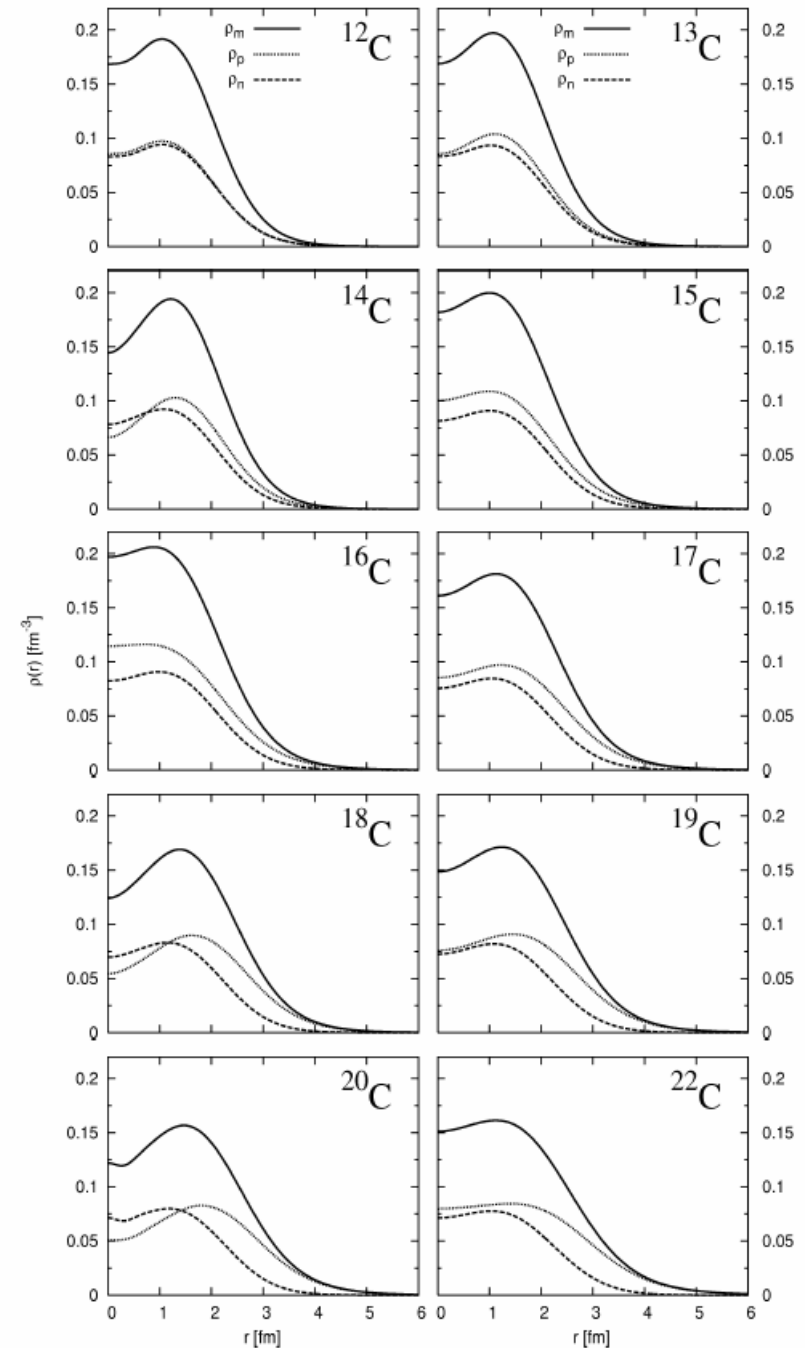


$\sigma^{\text{tot}}(p-^{12}\text{C})$  mb

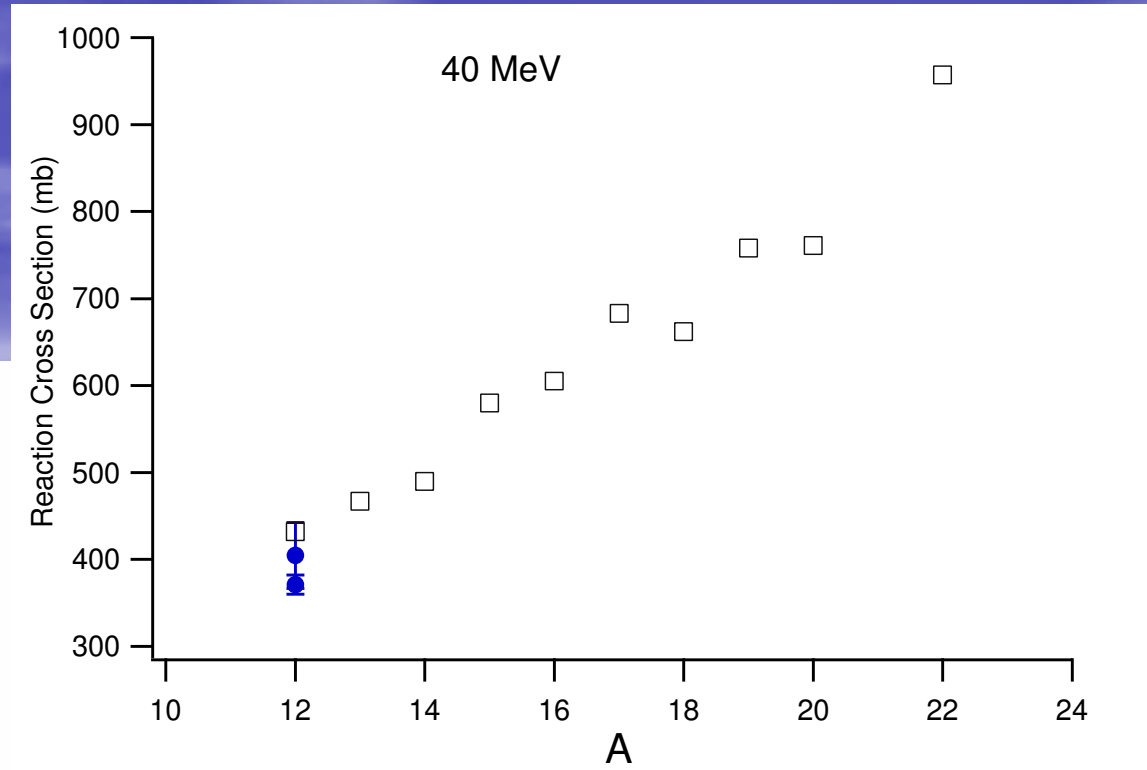
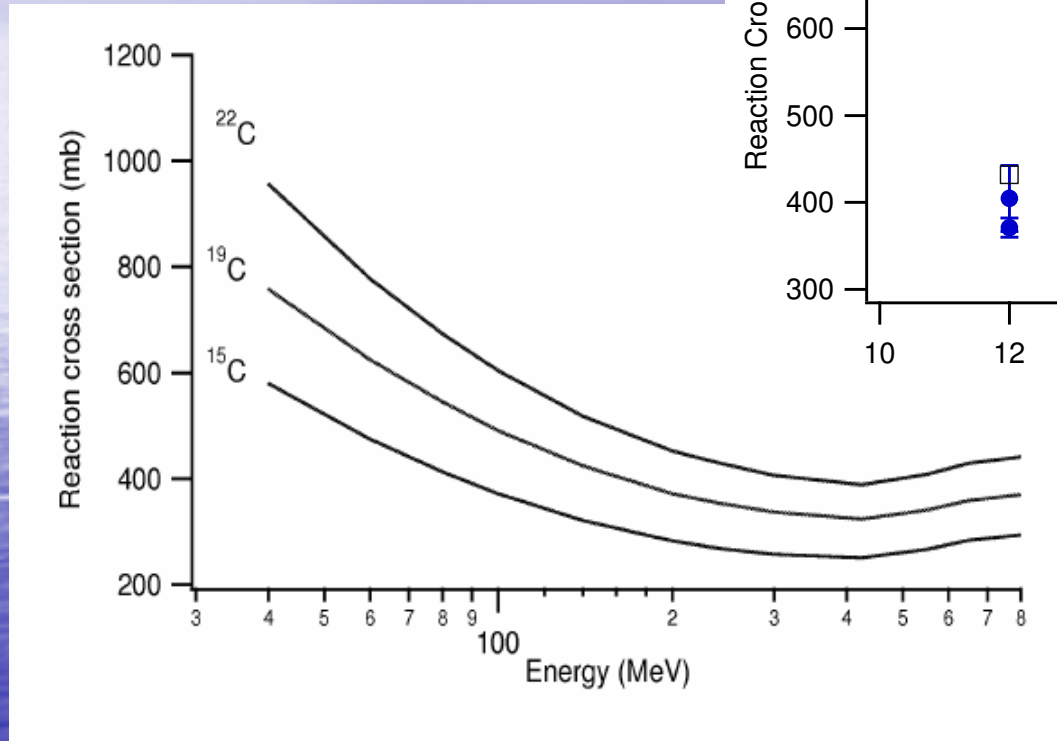
E(MeV)	dashed	solid
40	432	416
60	359	387
80	314	320
100	284	275

# Density distr. of carbon isotopes

- A Slater determinant-type w.f.
- Dynamical model
  - Core+n: odd-A
  - Core+2n: 16C, 22C
- The param. of cen. poten. to reproduce  $1n$  ( $2n$ )-sep. energy.
- c.m. motion is removed.
  - W. Horiuchi et al., PRC75 (2007).



# Numerical Results



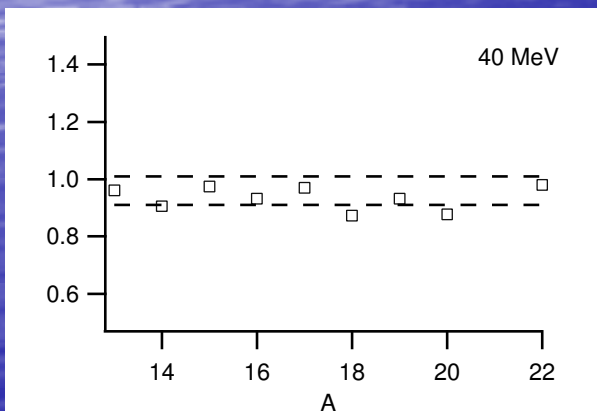
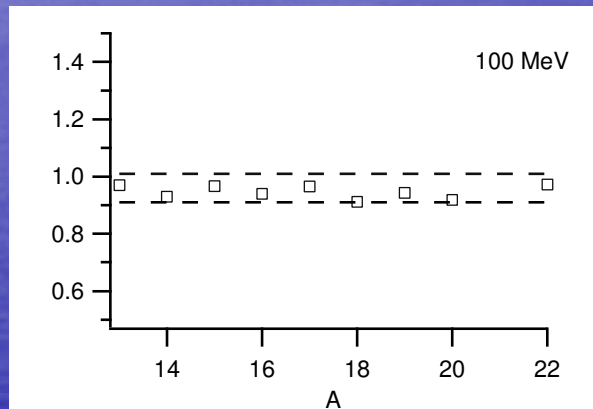
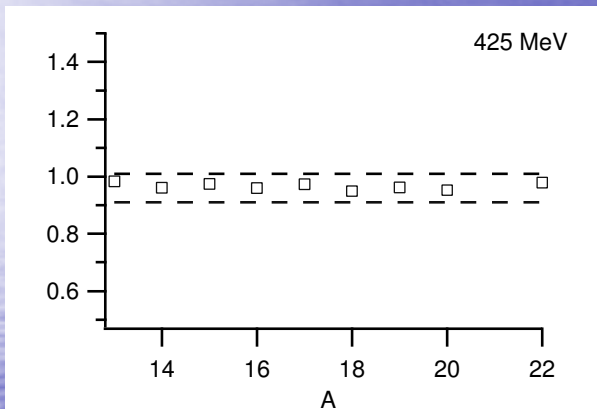
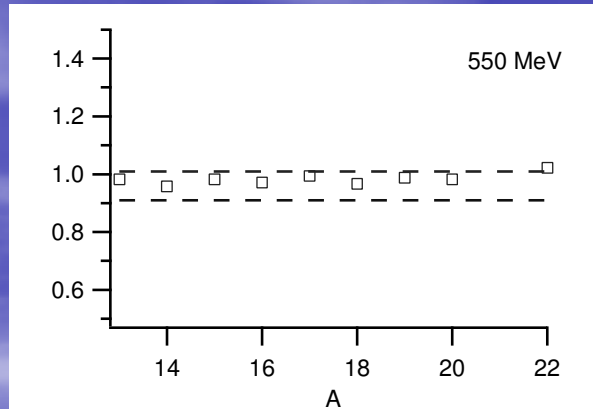
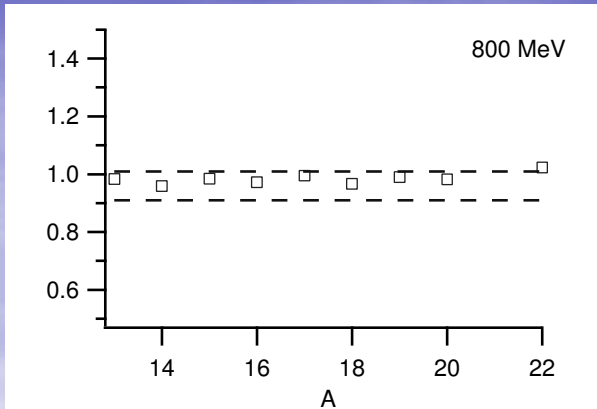
For  $^{22}\text{C}$ , the last two neutrons are in  $s_{1/2}$  orbit.

$$S_{2n} = 0.489 \text{ MeV} \quad \text{rms}=3.6 \text{ fm} \quad \text{rcs}=957 \text{ mb}$$

$$S_{2n} = 0.122 \text{ MeV} \quad \text{rms}=4.1 \text{ fm} \quad \text{rms}=1005 \text{ mb} \quad \leftarrow$$

For this case, the breakup effect is expected to increase the cross section, but we estimated it to be less than one %.

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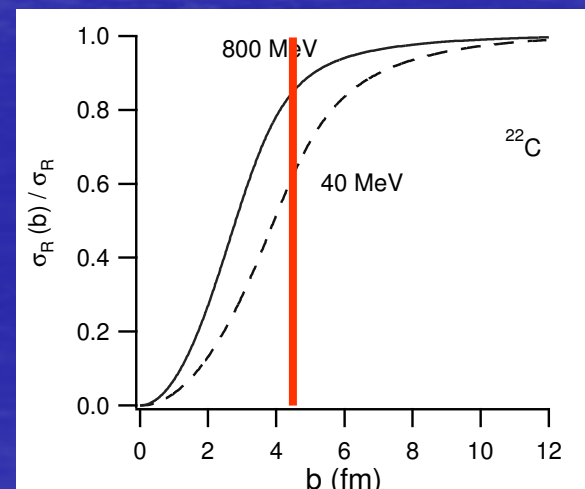
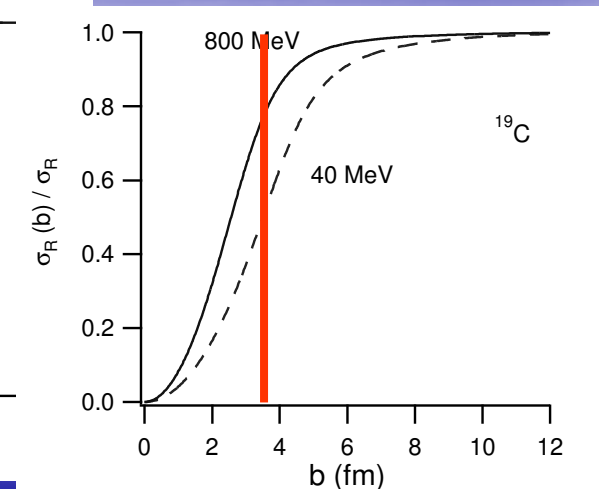
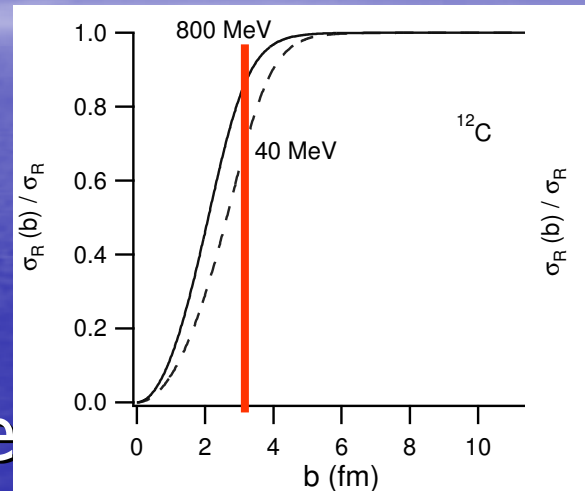
## An empirical formula

$$\frac{\sigma_R(p-{}^N_6\text{C})}{\sigma_R(p-{}^{12}_6\text{C})} = (0.96 \pm 0.05) \frac{6\sigma_{pp} + N\sigma_{pn}}{6\sigma_{pp} + 6\sigma_{pn}}$$

Once we know  $\sigma_R$  of a stable isotope, ...

# The major contribution to $\sigma_R$ ?

- If we determine a scale,  $a$ , from  $\sigma_R = \pi a^2$  at 800 MeV, about 80% of  $\sigma_R$  is filled within this scale for all the cases.
- Surface contributions are more or less the same at high E.



$$\sigma_R(b)/\sigma_R$$

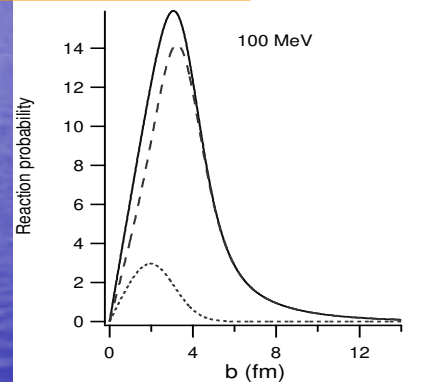
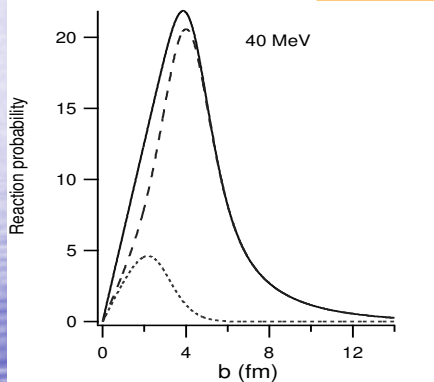
$$\sigma_R = \sigma_R(b=\infty).$$



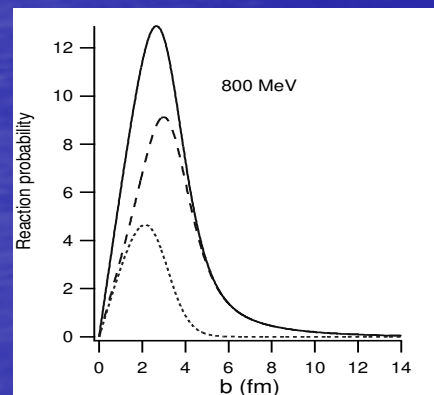
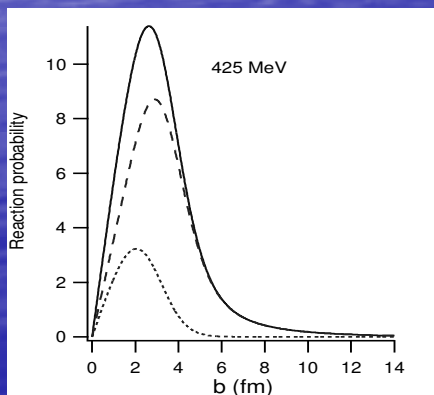
# Neutron contributions to the reaction cross sections

$$\sigma_R = 2\pi \int_0^\infty b db (P_p(b) + P_n(b)).$$

$$2\pi b P(b)$$



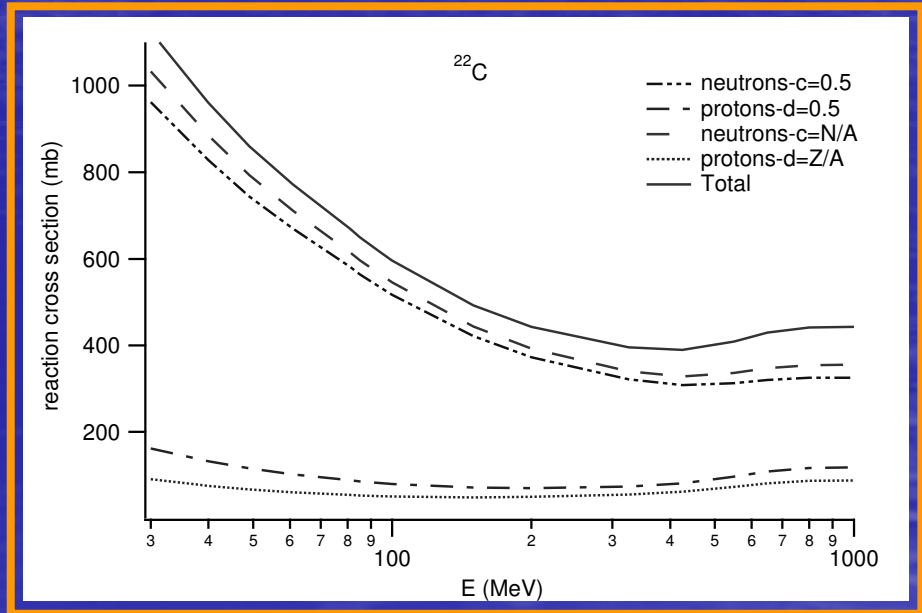
p-22C



$$P_n(b) = |e^{i\chi_p(b)}|^2 \left( 1 - |e^{i\chi_n(b)}|^2 \right) + c \left( 1 - |e^{i\chi_n(b)}|^2 \right) \left( 1 - |e^{i\chi_p(b)}|^2 \right)$$

$$c + d = 1.$$

$$P_p(b) = |e^{i\chi_n(b)}|^2 \left( 1 - |e^{i\chi_p(b)}|^2 \right) + d \left( 1 - |e^{i\chi_n(b)}|^2 \right) \left( 1 - |e^{i\chi_p(b)}|^2 \right)$$

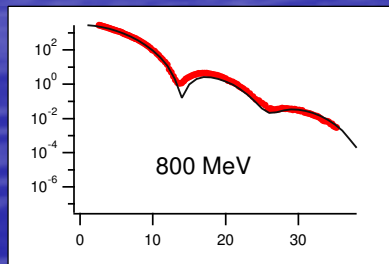
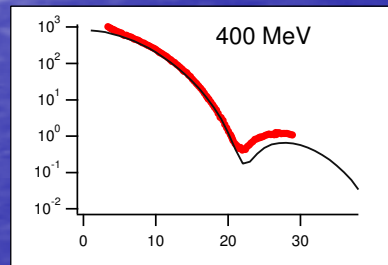
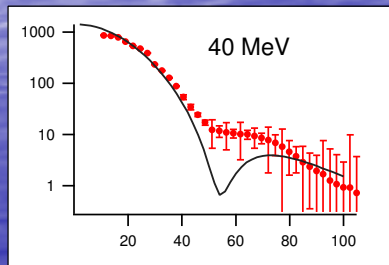
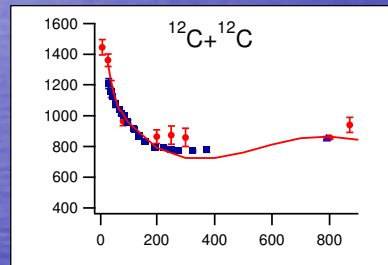
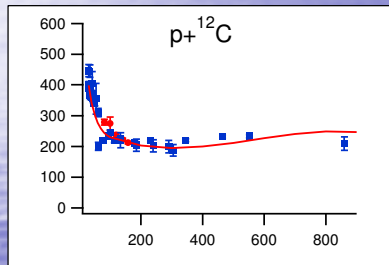
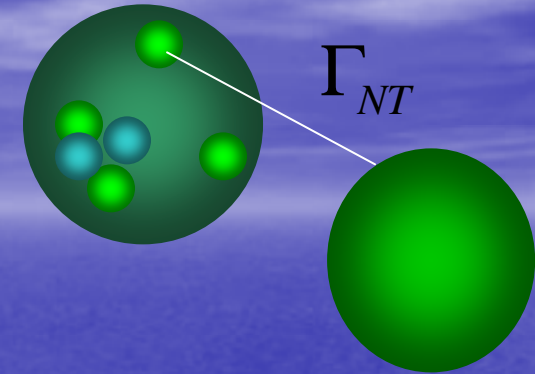


# Nucleus-Nucleus Reaction

$$e^{i\chi(b)} = \left\langle \Psi_0 \left| \prod_{i \in P} (1 - \Gamma_{NT}(r_i + b)) \right| \Psi_0 \right\rangle$$

$$i\chi_{OLA}^{NT}(b) = - \int dr \rho_P(r) \Gamma_{NT}(r + b)$$

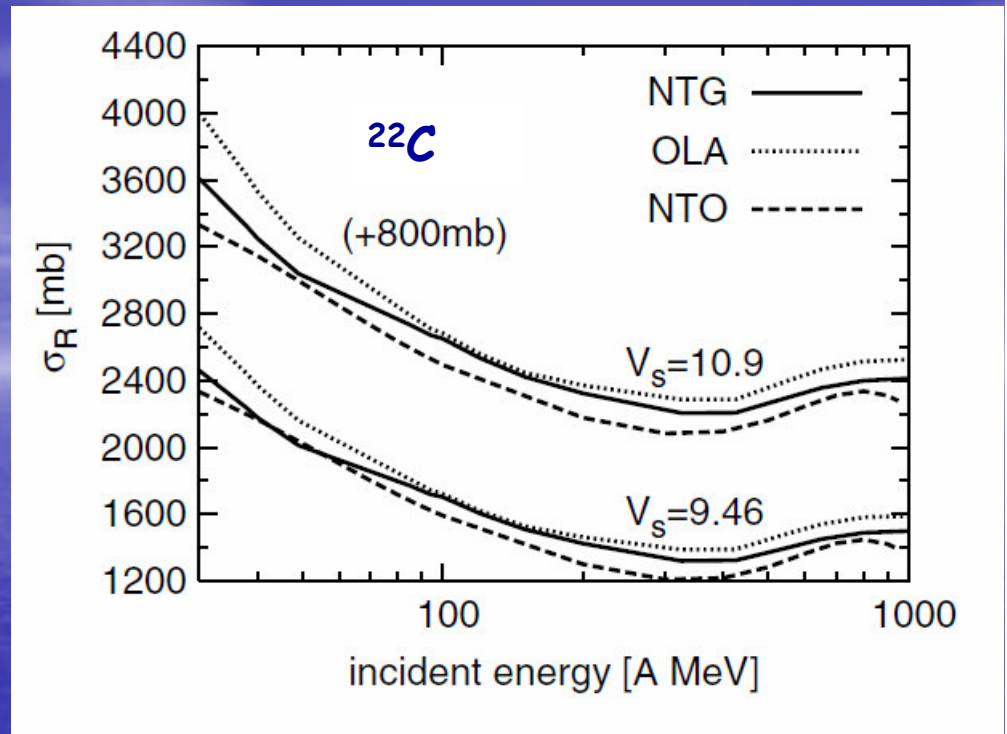
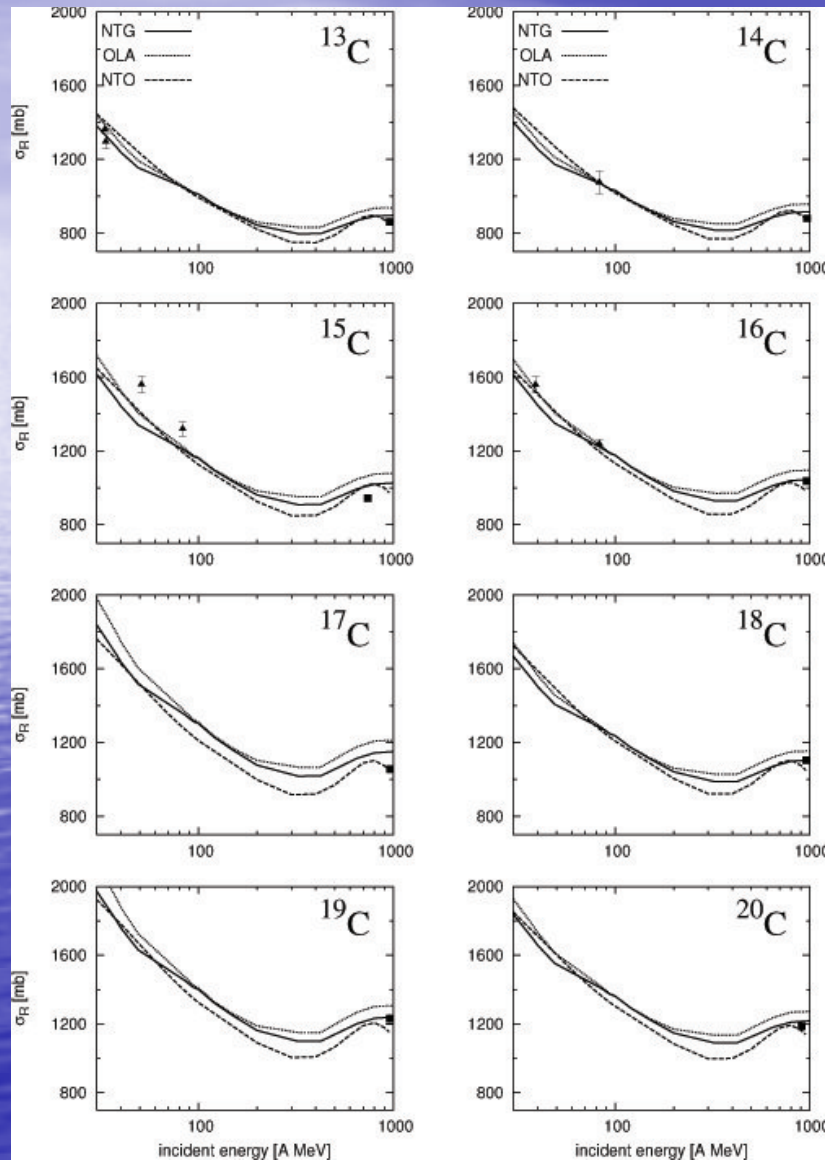
$$\Gamma_{NT}(b) = 1 - \exp\left(-\frac{i}{\hbar v} \int_{-\infty}^{\infty} U_{NT}(b+z) dz\right)$$



Using N-T interaction means various in-medium effects has been taken into account

- 1- L.N. Blumberg et al PR 147(1966)812.
- 2- G.S. Blanpied et al PRL 39(1977)1447.
- 3- K.W. Jones et al PRC 33 (1986)17.
- 4- H.O. Meyer et al PRC 23 (1981) 616.
- 5- M. Takechi et al., Eur. Phys. J. A 25, s01, 217 (2005).
- 6- S. Kox et al., Phys. Rev. C 35, 1678 (1987).

# Numerical Results



$V_s$  for poten. of n- $^{20}\text{C}$ .

16C, 22C: core+2n model.

Exp.data:

NPA 693, 32 (2001).

PRC 69, 034613 (2004).

NPA 709, 103 (2002).

PRC 61, 064311 (2000).

# Summary

- 1. We have predicted the reaction cross sections of carbon isotopes incident on a proton target on the energy range from 40 MeV to 800 MeV.**
- 2. A new set of NN-parameters values has been obtained.**
- 3. We have proposed a relation that separates the neutrons and protons contributions to the reaction cross section. The neutron and proton contributions to the reaction cross section have been studied.**
- 4. The reaction cross sections for carbon isotopes incident on  $^{12}\text{C}$  have been studied. Our calculations reproduced the available experimental data, except for  $^{15}\text{C}$ .**
- 5. The reaction cross section of  $^{22}\text{C}+^{12}\text{C}$  has been predicted at different energies.**