

Radioactive Beams for **Nuclear Spectroscopy** and **Nuclear Astrophysics**

**DREB
2007** Direct Reaction
with Exotic Beams

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May 30, 2007

Today's Talk

- **What we measure in transfer reactions**
- **ANCs** for nuclear astrophysics
 - recent results
- **Spectroscopic factors**
 - connections to nuclear astrophysics
- **Future directions**

Extracting spectroscopic factors

Transfer reaction $B+d \rightarrow A+a$

$$\frac{d\sigma}{d\Omega} = \sum S_{Bpl_A j_A} S_{apl_d j_d} \sigma_{l_A j_A l_d j_d}^{DW}$$

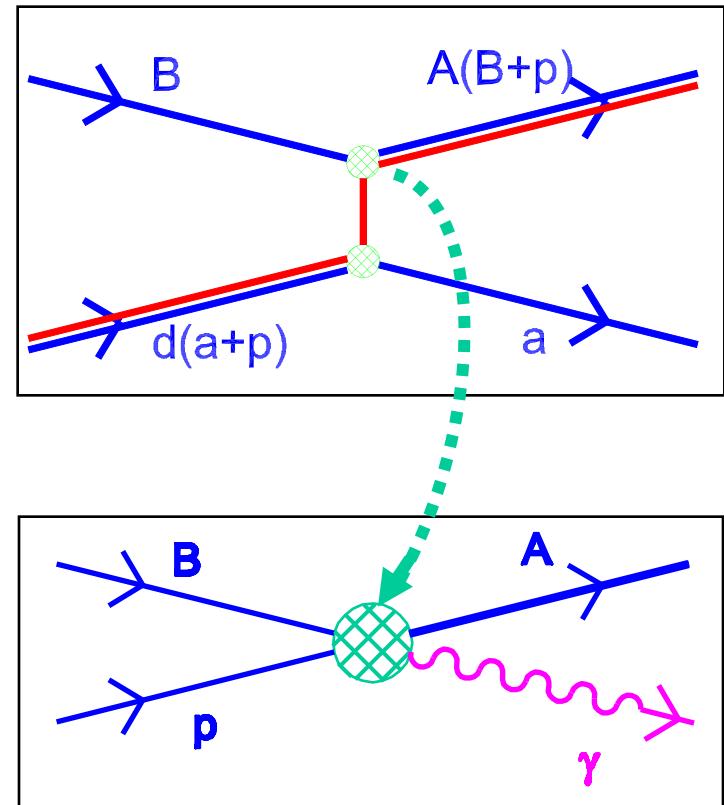
$$\frac{d\sigma}{d\Omega} = (C_{Bpl_A j_A}^A)^2 (C_{apl_d j_d}^d)^2 \frac{\sigma_{l_A j_A l_d j_d}^{DW}}{b_{Bpl_A j_A}^2 b_{apl_d j_d}^2}$$

Direct p capture

$$\sigma_{(p,\gamma)} \propto (C_{Bp}^A)^2$$

Direct n capture

$\sigma_{(n,\gamma)} =$ more complicated!



$$I_{Bp}^A \stackrel{r_{Bp} > R_N}{\approx} C_{Bp}^A \frac{W_{-\mathbf{n}_A, l+\frac{1}{2}}(2\kappa_{Bp} r_{Bp})}{r_{Bp}}$$

ANCs for (p,γ) rates

- **Proton transfer reactions**
 - stable and radioactive beams
- **Neutron transfer reactions + charge symmetry**
 - stable beams
- **Breakup reactions**
 - radioactive beams
- **Ancillary measurements**
 - elastic scattering for O.M. parameters
 - folding model O.M. parameters in the p shell

H burning, CNO & HCNO Cycles

Reactions studied relevant to:

p-p chain

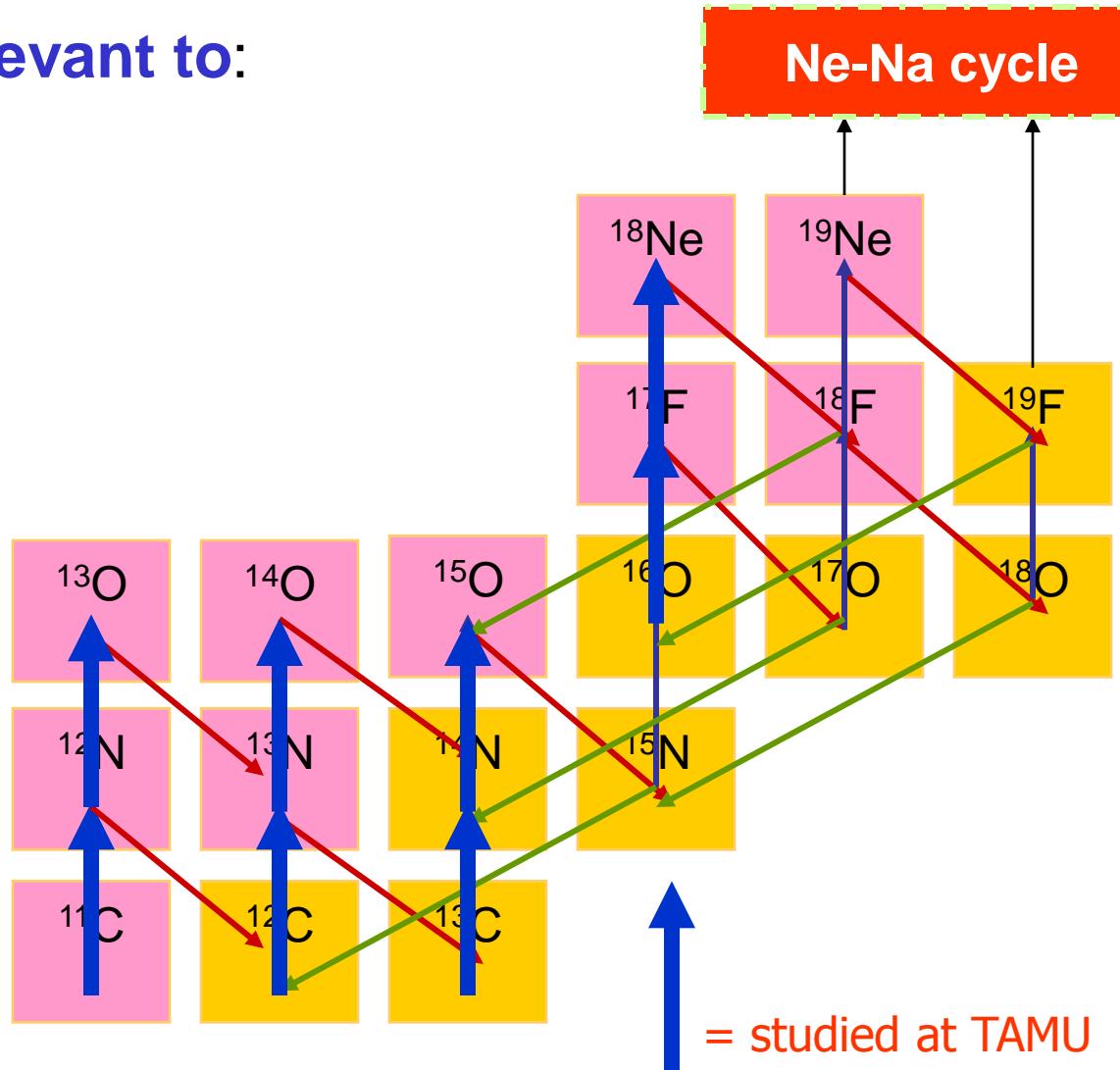
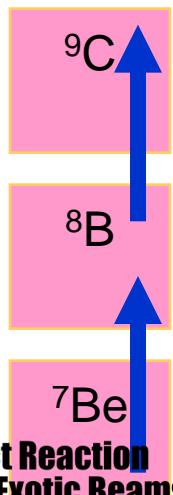
rapid α -*p* reactions

CNO cycle

HCNO cycle

Breakout from CNO cycle

Ne-Na cycle



ANCs (p) measured using stable beams

- ${}^9\text{Be} + \text{p} \leftrightarrow {}^{10}\text{B}^*$ [${}^9\text{Be}({}^3\text{He}, d){}^{10}\text{B}$; ${}^9\text{Be}({}^{10}\text{B}, {}^9\text{Be}){}^{10}\text{B}$] ${}^9\text{Be}(\text{p}, \gamma){}^{10}\text{B}$
 - ${}^{12}\text{C} + \text{p} \leftrightarrow {}^{13}\text{N}$ [${}^{12}\text{C}({}^3\text{He}, d){}^{13}\text{N}$] ${}^{12}\text{C}(\text{p}, \gamma){}^{13}\text{N}$
 - ${}^{13}\text{C} + \text{p} \leftrightarrow {}^{14}\text{N}$ [${}^{13}\text{C}({}^3\text{He}, d){}^{14}\text{N}$; ${}^{13}\text{C}({}^{14}\text{N}, {}^{13}\text{C}){}^{14}\text{N}$] ${}^{13}\text{C}(\text{p}, \gamma){}^{14}\text{N}$
 - ${}^{14}\text{N} + \text{p} \leftrightarrow {}^{15}\text{O}$ [${}^{14}\text{N}({}^3\text{He}, d){}^{15}\text{O}$] ${}^{14}\text{N}(\text{p}, \gamma){}^{15}\text{O}$
 - ${}^{16}\text{O} + \text{p} \leftrightarrow {}^{17}\text{F}^*$ [${}^{16}\text{O}({}^3\text{He}, d){}^{17}\text{F}$] ${}^{16}\text{O}(\text{p}, \gamma){}^{17}\text{F}$
 - ${}^{20}\text{Ne} + \text{p} \leftrightarrow {}^{21}\text{Na}^*$ [${}^{20}\text{Ne}({}^3\text{He}, d){}^{21}\text{Na}$] ${}^{20}\text{Ne}(\text{p}, \gamma){}^{21}\text{Na}$
- beams ≈ 10 MeV/u

* Test cases

ANCs measured by our group with **radioactive** (rare isotope) **beams**

- ${}^7\text{Be} + \text{p} \leftrightarrow {}^8\text{B}$ $[{}^{10}\text{B}({}^7\text{Be}, {}^8\text{B}) {}^9\text{Be}]$ ${}^7\text{Be}(\text{p}, \gamma) {}^8\text{B}$
 $[{}^{14}\text{N}({}^7\text{Be}, {}^8\text{B}) {}^{13}\text{C}]$
 - ${}^{11}\text{C} + \text{p} \leftrightarrow {}^{12}\text{N}$ $[{}^{14}\text{N}({}^{11}\text{C}, {}^{12}\text{N}) {}^{13}\text{C}]$ ${}^{11}\text{C}(\text{p}, \gamma) {}^{12}\text{N}$
 - ${}^{12}\text{N} + \text{p} \leftrightarrow {}^{13}\text{O}$ $[{}^{14}\text{N}({}^{12}\text{N}, {}^{13}\text{O}) {}^{13}\text{C}]$ ${}^{12}\text{N}(\text{p}, \gamma) {}^{13}\text{O}$
 - ${}^{13}\text{N} + \text{p} \leftrightarrow {}^{14}\text{O}$ $[{}^{14}\text{N}({}^{13}\text{N}, {}^{14}\text{O}) {}^{13}\text{C}]$ ${}^{13}\text{N}(\text{p}, \gamma) {}^{14}\text{O}$
 - ${}^{17}\text{F} + \text{p} \leftrightarrow {}^{18}\text{Ne}$ $[{}^{14}\text{N}({}^{17}\text{F}, {}^{18}\text{Ne}) {}^{13}\text{C}]$ ${}^{17}\text{F}(\text{p}, \gamma) {}^{18}\text{Ne}$
{ORNL (TAMU collaborator)}

beams \approx 10 - 12 MeV/u

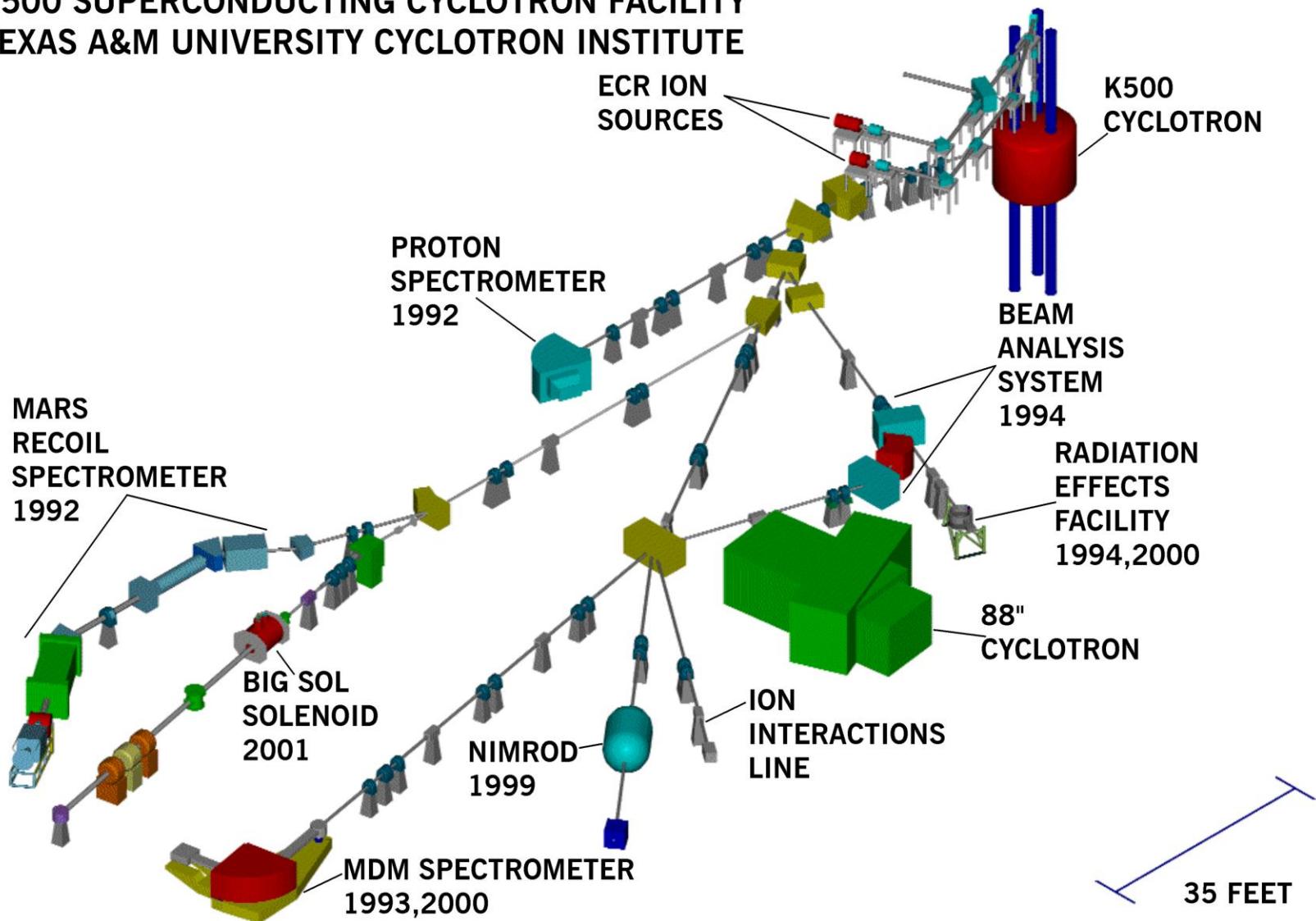
ANCs (n) measured using stable beams

[Charge Symmetry]

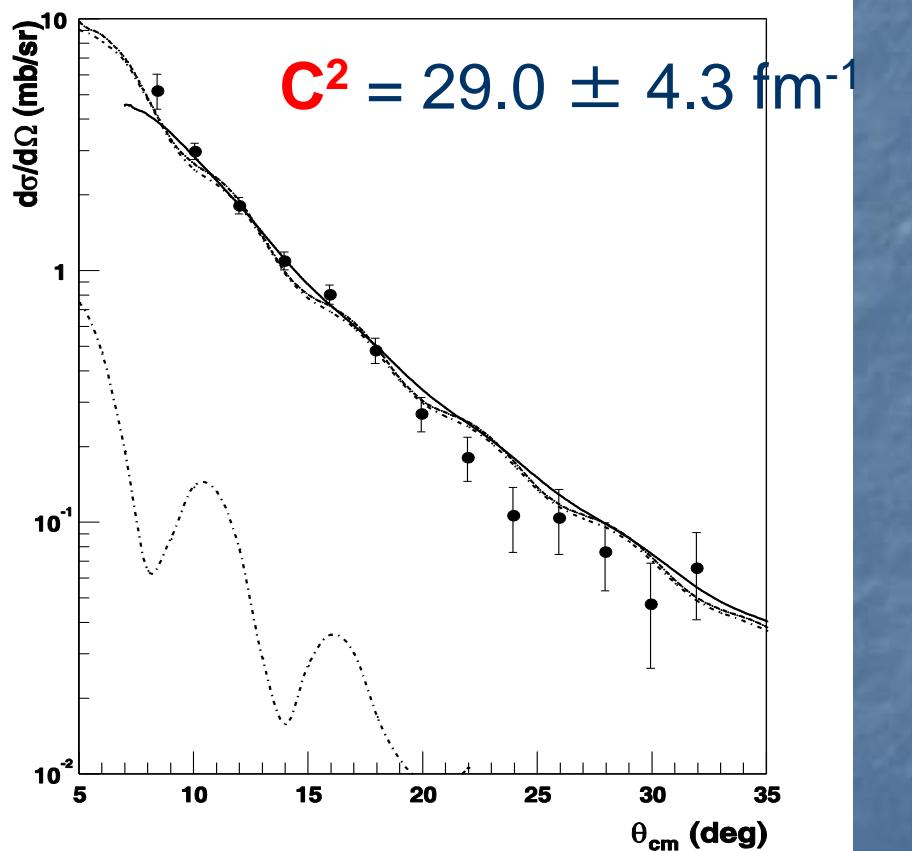
- ${}^7\text{Li} + \text{n} \leftrightarrow {}^8\text{Li}$ $[{}^{13}\text{C}({}^7\text{Li}, {}^8\text{Li}){}^{12}\text{C}]$ ${}^7\text{Be}(\text{p}, \gamma){}^8\text{B}$
- ${}^{12}\text{C} + \text{n} \leftrightarrow {}^{13}\text{C}$ $[{}^{12}\text{C}({}^{13}\text{C}, {}^{12}\text{C}){}^{13}\text{C}]$
- ${}^{22}\text{Ne} + \text{n} \leftrightarrow {}^{23}\text{Ne}$ $[{}^{13}\text{C}({}^{22}\text{Ne}, {}^{23}\text{Ne}){}^{12}\text{C}]$ ${}^{22}\text{Mg}(\text{p}, \gamma){}^{23}\text{Al}$
- ${}^{16}\text{O} + \text{n} \leftrightarrow {}^{17}\text{O}$ $[{}^{13}\text{C}({}^{16}\text{O}, {}^{17}\text{O}){}^{12}\text{C}]$ ${}^{16}\text{O}(\text{p}, \gamma){}^{17}\text{F}$
- ${}^{17}\text{O} + \text{n} \leftrightarrow {}^{18}\text{O}$ $[{}^{13}\text{C}({}^{17}\text{O}, {}^{18}\text{O}){}^{12}\text{C}]$ ${}^{17}\text{F}(\text{p}, \gamma){}^{18}\text{Ne}$

beams ≈ 10 MeV/u

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S Factor(^1H , ^1H , ^{14}N (p , ρ) ^{14}O)

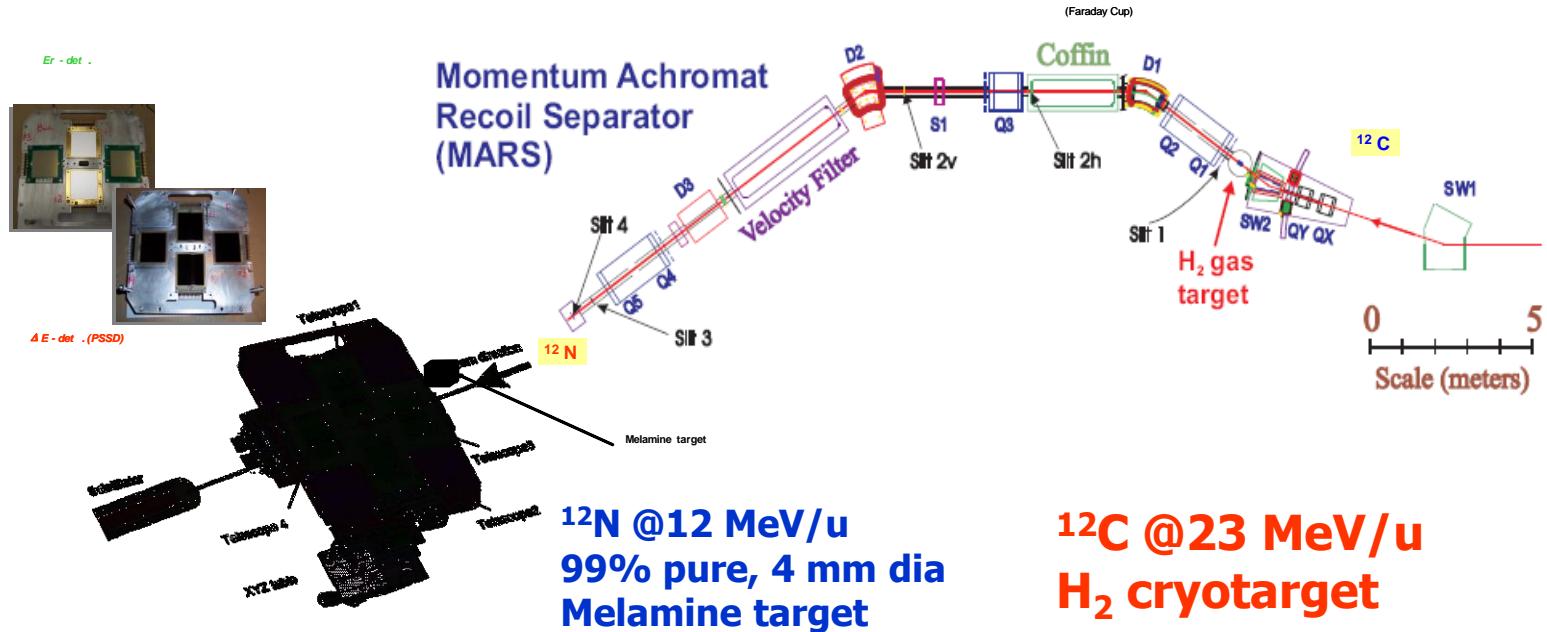


Use R-matrix with resonant and DC pieces to get S factor

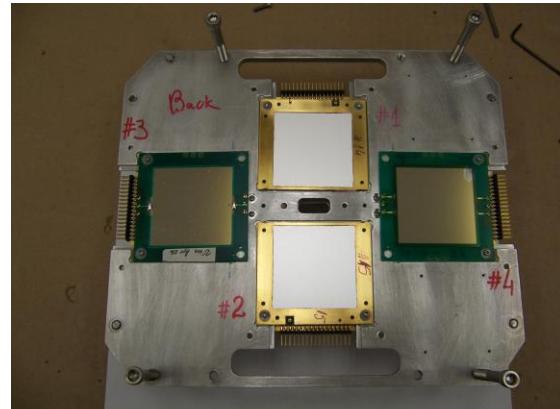
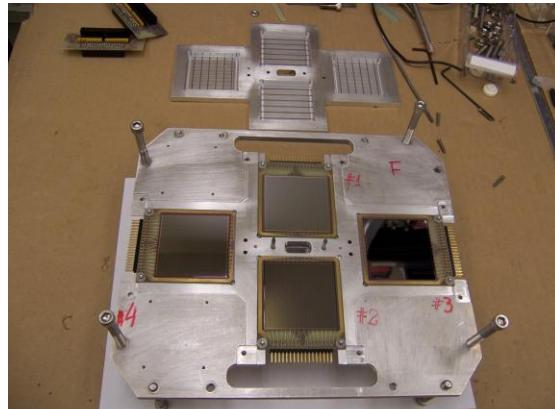
Find S(0) about 7 keVb with constructive int.

DWBA by FRESCO

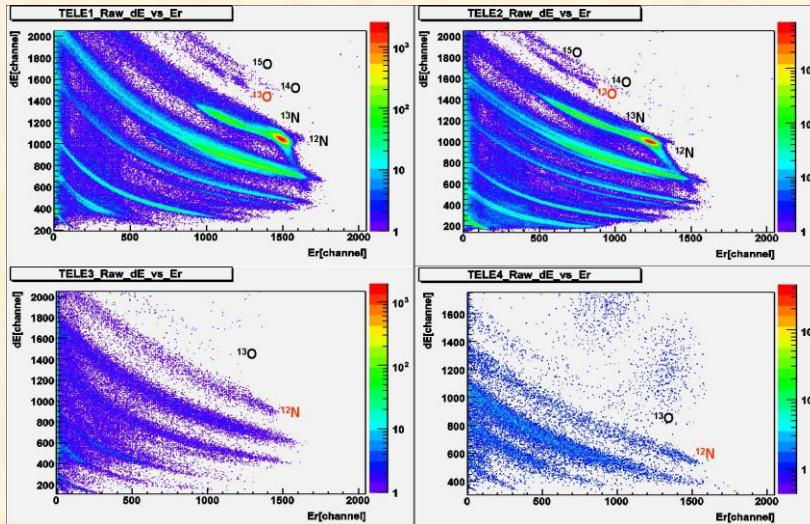
Cross sections for (p,γ) from p -transfer reactions with RNB from MARS



Extended telescope system:
 $\Delta E - \text{PSD } 65, 110 \mu\text{m}$
 $E - 500 \mu\text{m}$



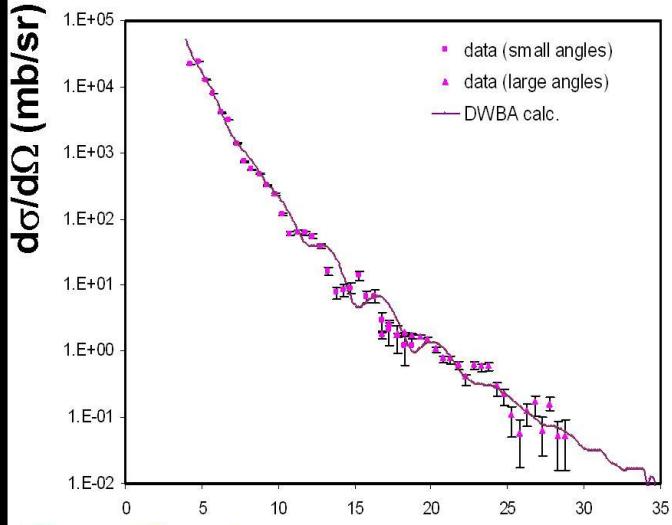
^{12}N @12 MeV on $\text{N}_6\text{C}_3\text{H}_6$ – May 2006



- ^{12}C @ 23 MeV/A - 150 pNA
- ^{12}N @ 12 MeV/A - 10^5 pps

Elastic angular distribution:

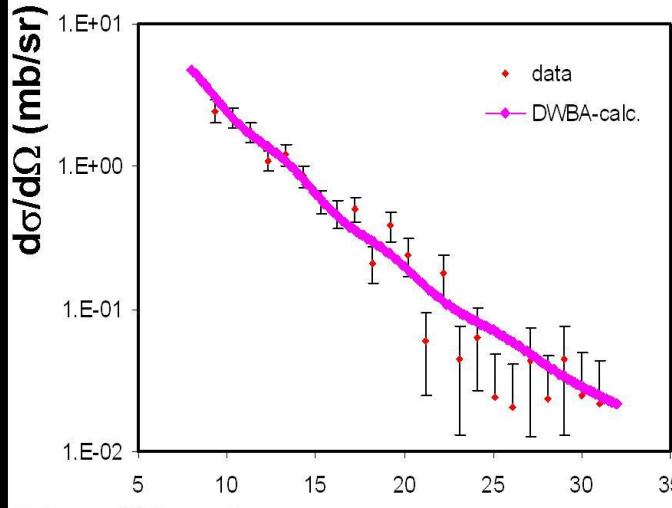
^{12}N on melamine



Preliminary

Transfer angular distribution:

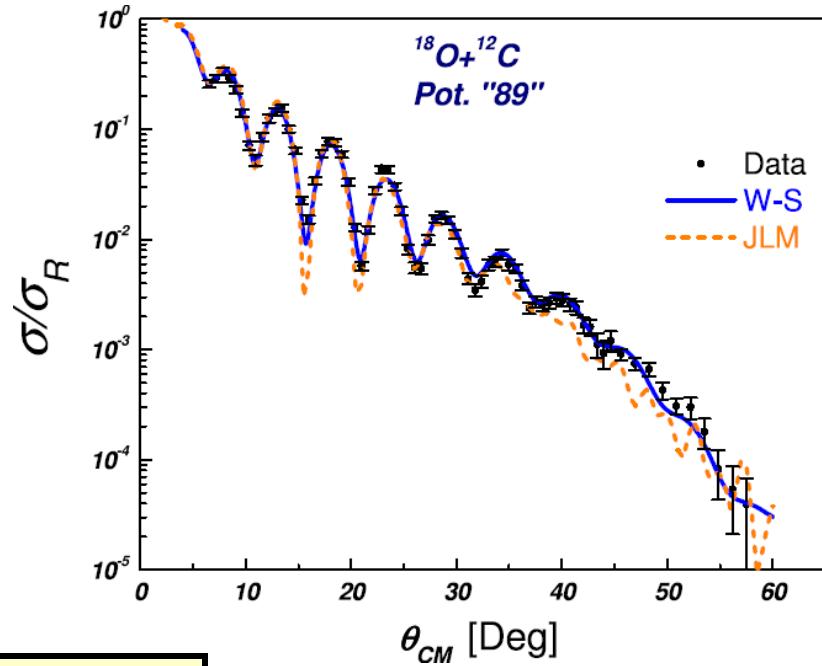
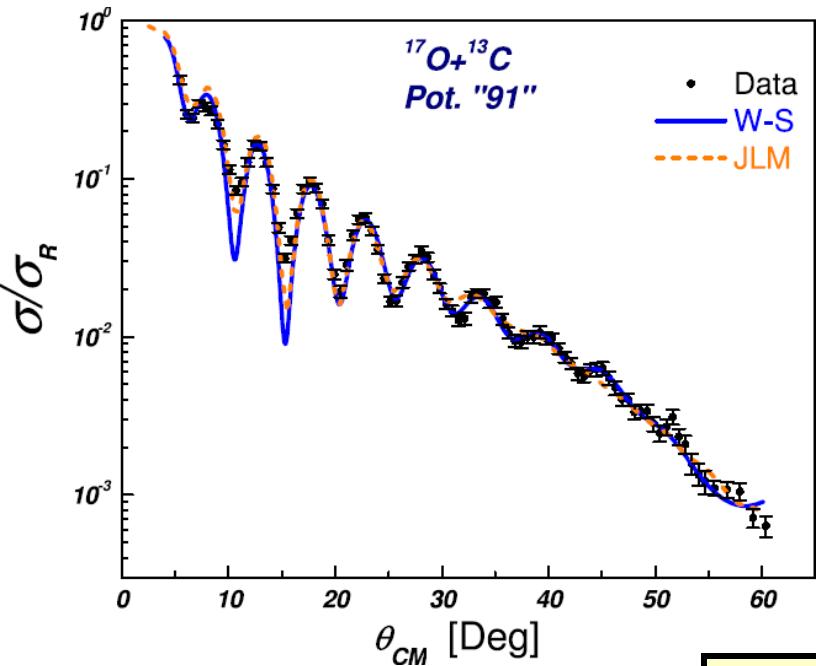
$^{14}\text{N}(^{12}\text{N}, ^{13}\text{O})^{13}\text{C}$ @ 12 MeV/u



Preliminary

$$C^2 \sim 3.3 \text{ fm}^{-1}$$

ATM



Wood-Saxon & double
folding both work!

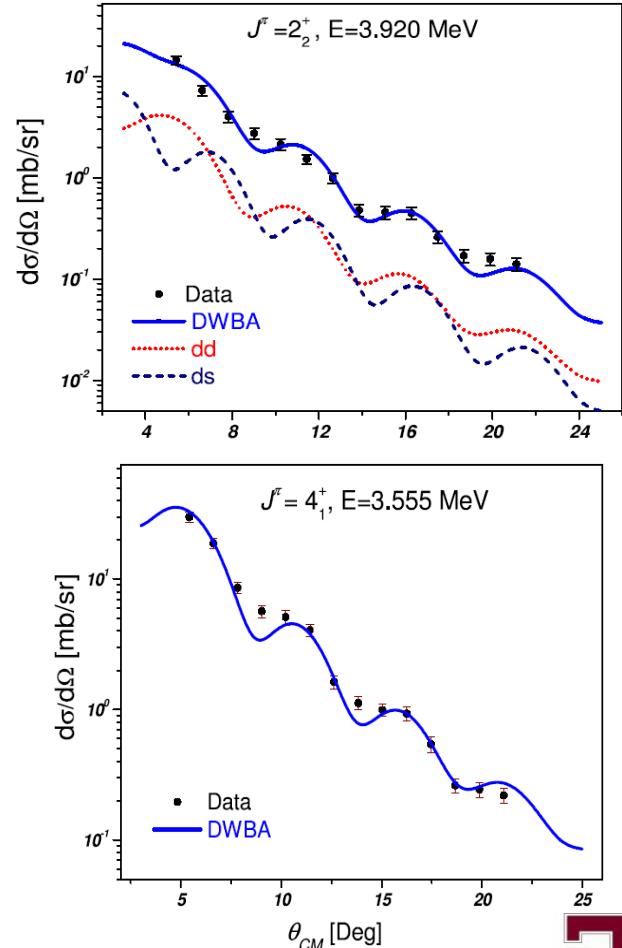
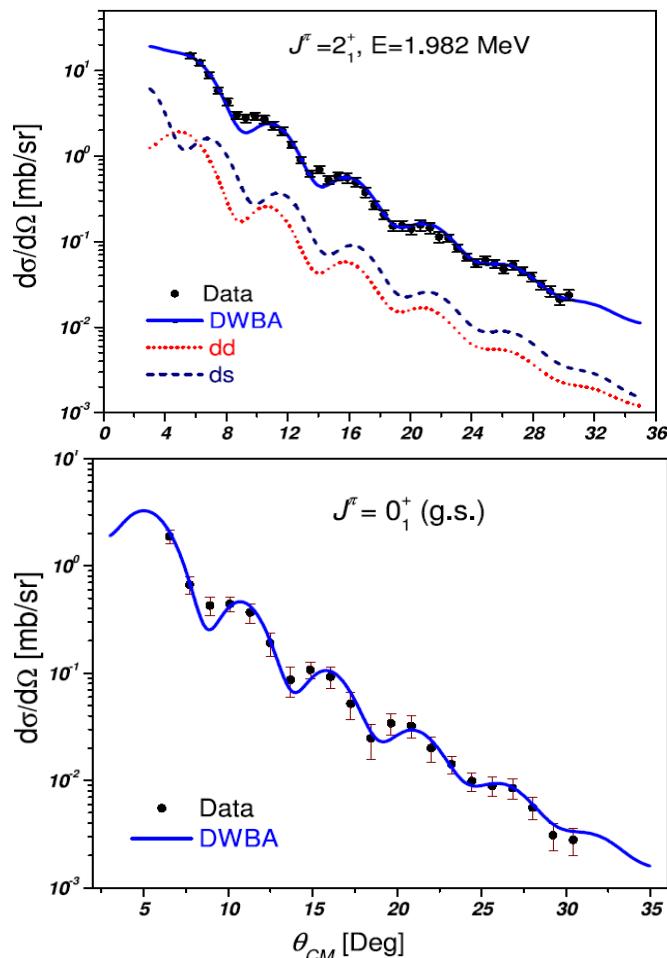
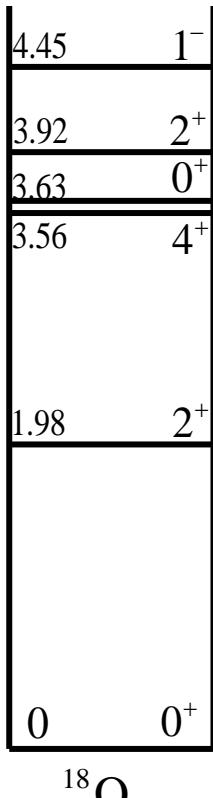
V [MeV]	r _V [fm]	a _V [fm]	W [MeV]	r _W [fm]	a _W [fm]	χ^2
91.8	0.90	0.86	26.9	1.10	0.71	4.4
200	0.70	0.95	22.0	1.16	0.65	4.9
396.3	0.57	0.95	25.2	1..18	0.62	4.9

V [MeV]	r _V [fm]	a _V [fm]	W [MeV]	r _W [fm]	a _W [fm]	χ^2
89.1	0.88	0.90	26.2	1.16	0.70	5.0
189.8	0.69	0.96	27.2	1.16	0.69	8.6
218.0	0.86	1.42	22.0	1.36	0..97	14.0

$^{13}\text{C}(^{17}\text{O}, ^{18}\text{O})^{12}\text{C}$

- ANC's for first 4 states in ^{18}O
- 2_2^+ state dominates (p, γ) rate

$$\frac{d\sigma}{d\Omega} = \frac{\left(C_{^{12}\text{C}, \frac{1}{2}} \right)^2}{b_{^{12}\text{C}, \frac{1}{2}}^2} \left[\left(C_{^{17}\text{O}, \frac{5}{2}} \right)^2 \frac{\sigma_{\frac{5}{2}, \frac{5}{2}}^{DW}}{b_{^{17}\text{O}, \frac{5}{2}}^2} + \left(C_{^{17}\text{O}, \frac{1}{2}} \right)^2 \frac{\sigma_{\frac{5}{2}, \frac{1}{2}}^{DW}}{b_{^{17}\text{O}, \frac{1}{2}}^2} \right]$$



$^{17}\text{F}(\text{p},\gamma)^{18}\text{Ne}$

Charge symmetry:

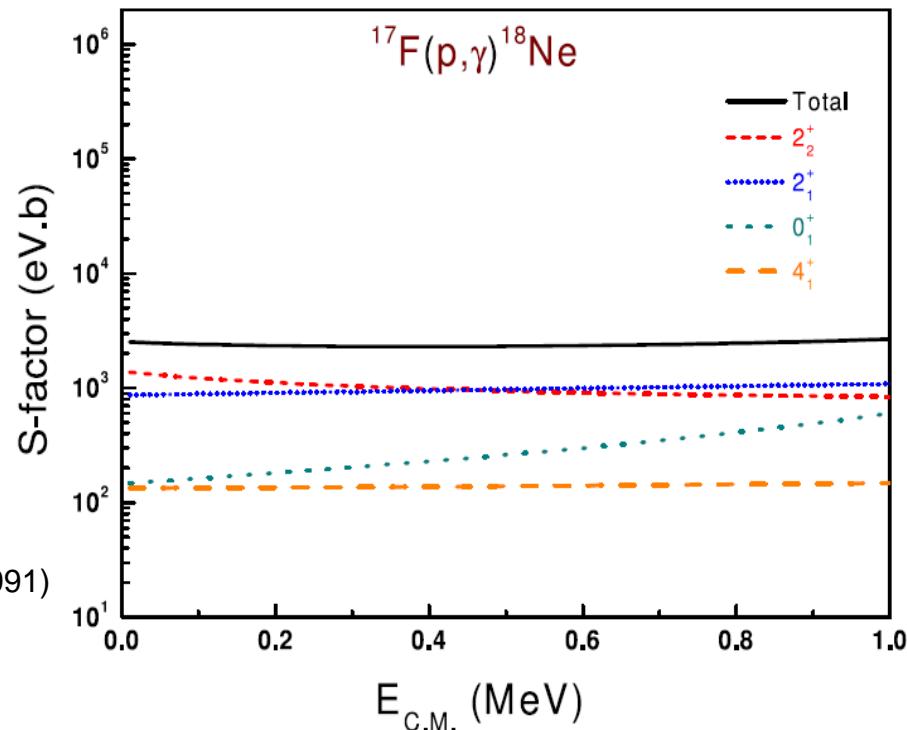
$$\frac{C_{\ell j}^2}{b_{\ell j}^2} \left(^{18}\text{O} \right) = \frac{C_{\ell j}^2}{b_{\ell j}^2} \left(^{18}\text{Ne} \right)$$

$$S_{1-17}(0) = 2.5 \pm 0.4 \text{ keV b}$$

Predictions:

≈ $S_{1-17}(0) = 2.9 \pm 0.4 \text{ keV b}$ * PRC 43, 2012(1991)

< $S_{1-17}(0) = 3.5 \text{ keV b}$ * NPA 730 (2004) 316



J^π	Proton Orbital	^{18}O		^{18}Ne	
		B.E. [MeV]	$C_{\ell j}^2 \text{ [fm}^{-1}]$	B.E. [MeV]	$C_{\ell j}^2 \text{ [fm}^{-1}]$
0^+_1	$d_{5/2}$	8.04	7.33 ± 0.73	3.92	10.76 ± 0.97
2^+_1	$d_{5/2}$	6.06	2.06 ± 0.21	2.04	2.17 ± 0.24
	$s_{1/2}$		6.55 ± 0.69		14.29 ± 1.71
4^+_1	$d_{5/2}$	4.48	1.05 ± 0.11	0.54	2.17 ± 0.22
2^+_2	$d_{5/2}$	4.12	0.49 ± 0.06	0.31	2.69 ± 0.32
	$s_{1/2}$		4.47 ± 0.54		127 ± 17

Future direction:
extension to
(n, γ) direct capture

Test case: $^{14}\text{C}(\text{n},\gamma)^{15}\text{C}$

- ANC from breakup of $^{15}\text{C} \rightarrow ^{14}\text{C} + \text{n}$
- Compare to $^{13}\text{C}(^{14}\text{C},^{15}\text{C})^{12}\text{C}$ at TAMU
- Determine **spectroscopic factor**
 - $d(^{14}\text{C},p)^{15}\text{C}$ in inverse kinematics – 12 MeV/A
 - compare to $^{14}\text{C}(d,p)^{15}\text{C}$ from Rez – 24 MeV
 - higher energy $^{14}\text{C}(d,p)^{15}\text{C}$ with K150 beam
- Use ANC to fix exterior part of cross section
- With ANC, determine $^{14}\text{C}(\text{n},\gamma)^{15}\text{C}$ direct capture
- Compare **spectroscopic factor** to expectations
- Use **spectroscopic factors** for s-wave d.c.

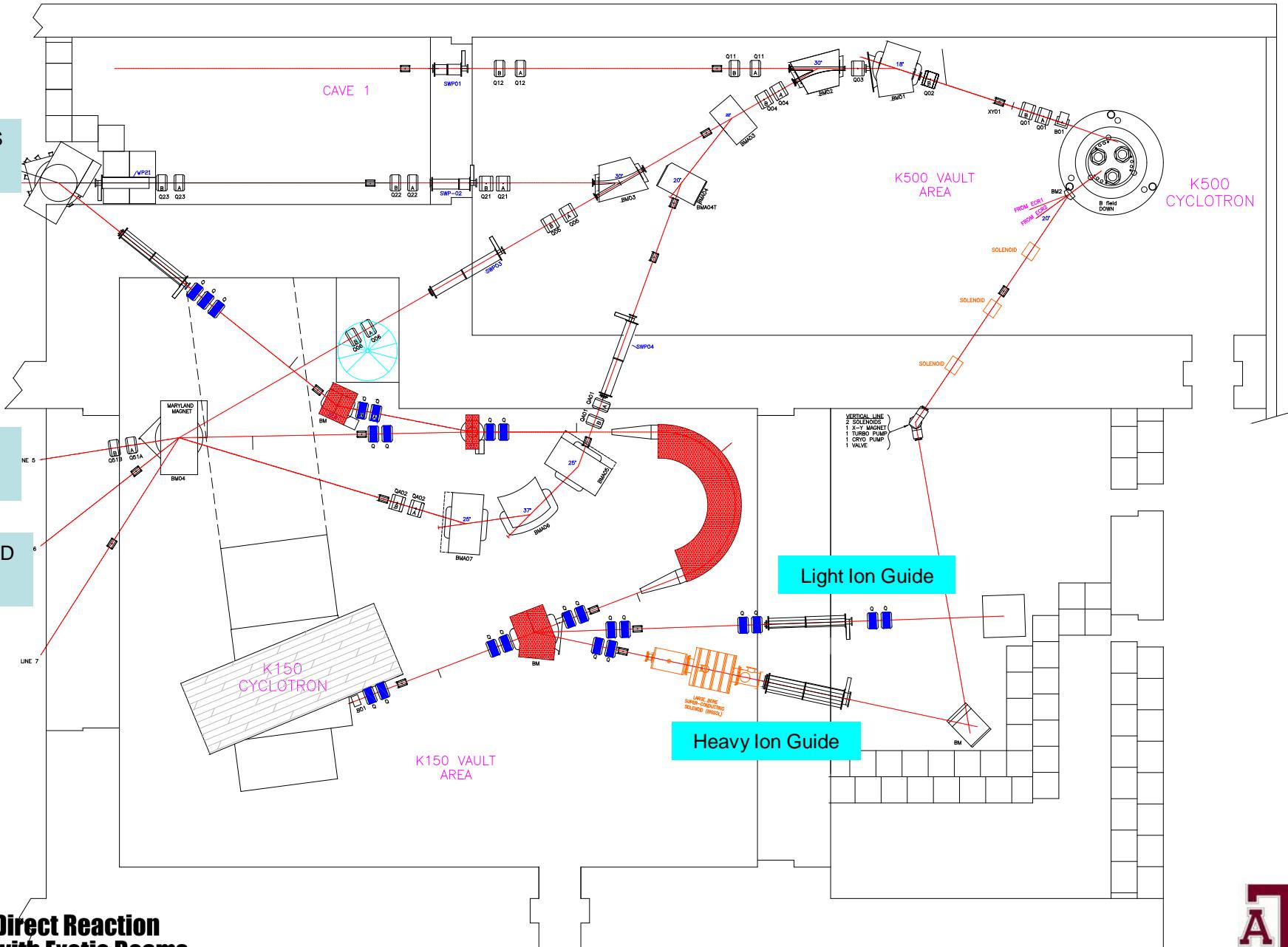
TAMU Upgrade Project

- Further develop **RIB** capability
- Produce **accelerated RIB's** at intermediate energies

TAMU Upgrade Project

- **Stage I**
 - commission K150(88") cyclotron
 - ECR source injection
 - commission beam lines to existing apparatus
- **Stage II**
 - isotope production stations completed
 - production of rare isotopes
- **Stage III**
 - K500 acceleration of rare isotope beams

Facility with K150 Beam Lines



Collaborators

- **TAMU**: T. Al-Abdullah, A. Azhari, H. Clark, C. Gagliardi, C. Fu, Y.-W. Lui, G. Tabacaru, X. Tang, L. Trache, A. Zhanov (Mukhamedzhanov)
- **INP** (Czech Republic): P. Bem, V. Burjan, V. Kroha, E. Simeckova, J. Vincour
- **IAP** (Romania): F. Carstoiu