

REACTION CROSS SECTIONS AND
NUCLEON DENSITY DISTRIBUTIONS
OF
LIGHT NUCLEI

MAYA TAKECHI

Collaborators

- Osaka Univ. M. Fukuda, M. Mihara, R. Matsumiya,
J. Komurasaki, D. Nishimura,
D. Ishikawa, K. Matsuta
- Fukui UT T. Minamisono
- Saitama Univ. S. Nakajima, K. Kobayashi, T. Kuboki,
T. Yoshitake, T. Yamaguchi, T. Suzuki
- Niigata Univ. T. Izumikawa, T. Ohtsubo, T. Matsuyama
- Kochi UT S. Momota
- Tsukuba Univ. Y. Yasuda, Y. Hashidume, T. Hoya, T. Moriguchi,
A. Ozawa
- NIRS M. Sasaki, S. Sato, M. Kanazawa, A. Kitagawa
- RIKEN K. Tanaka, T. Suda

INTRODUCTION

Sizes of Unstable Nuclei ?

~ Measurements of σ_R ~ $\sigma_R \equiv \sigma_{tot} - \sigma_{el}$

Proton Density
Neutron Density

High Energy Region ~ 1 GeV

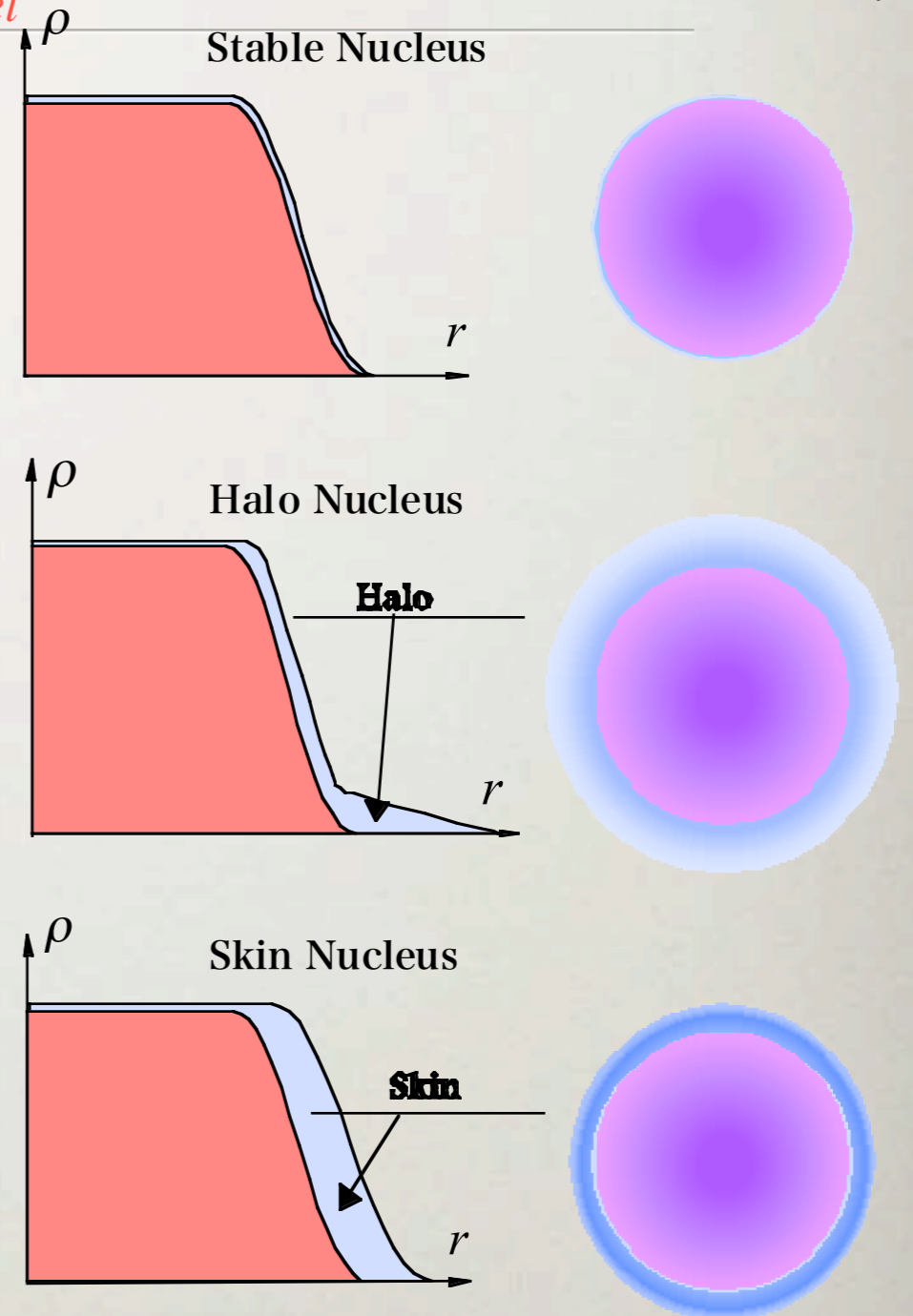
σ_R \longleftrightarrow Nuclear Radii

Glauber Calculation (OLA)

At Intermediate Energies



Nucleon Density Distribution !



Study of Density Distribution through Glauber Calculation

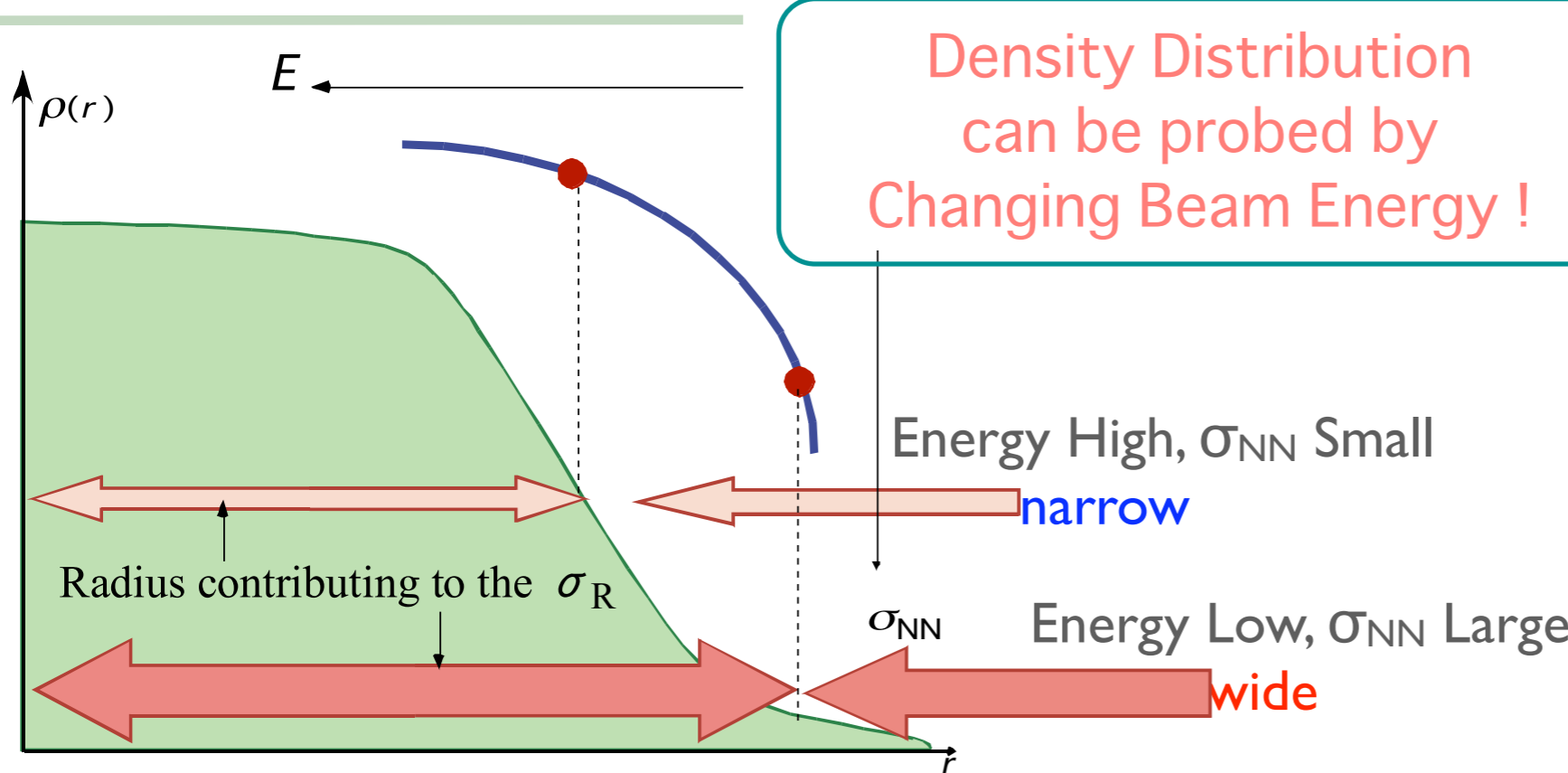
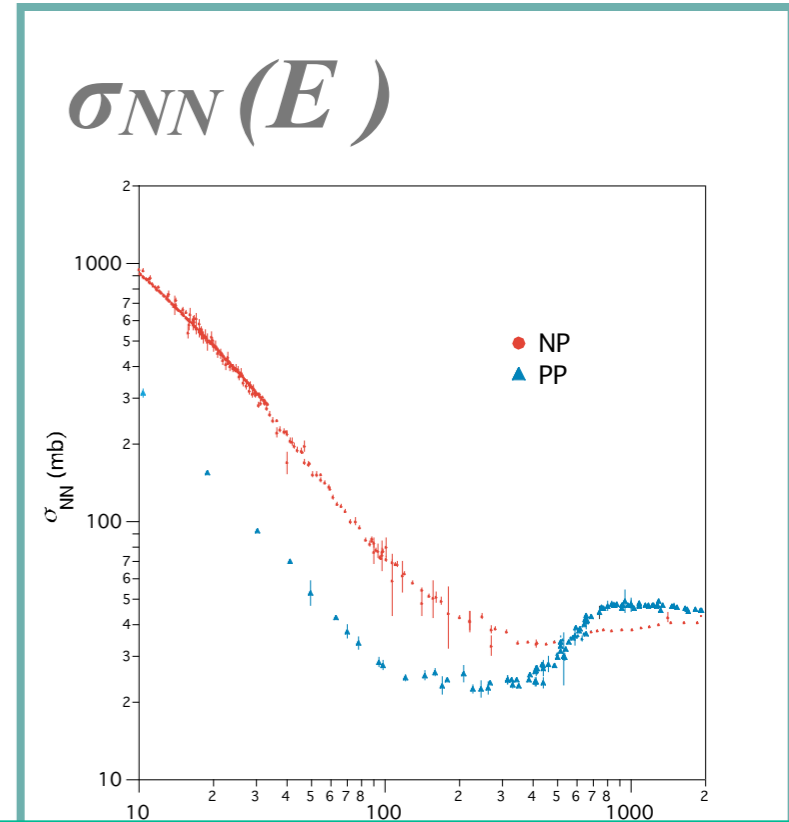
$$\sigma_R \longleftrightarrow \rho(r)$$

Glauber Calculation
(Optical Limit and Zero-Range Approximations of Glauber Theory)

$$\sigma_R = \int db \left[1 - \exp \left(- \int d^2r \sum_{i,j} \sigma_{NN}(E) \rho_z^{P_i}(r) \rho_z^{T_j}(r-b) \right) \right]$$

σ_R can be uniquely calculated by **3** quantities

- ρ^P Projectile Density
- ρ^T Target Density
- σ_{NN} NN total cross section



Problem

$\sigma_R(\text{Exp}) > \sigma_R(\text{Glauber Calc.})$

Glauber Calculation underestimates σ_R at Intermediate Energies

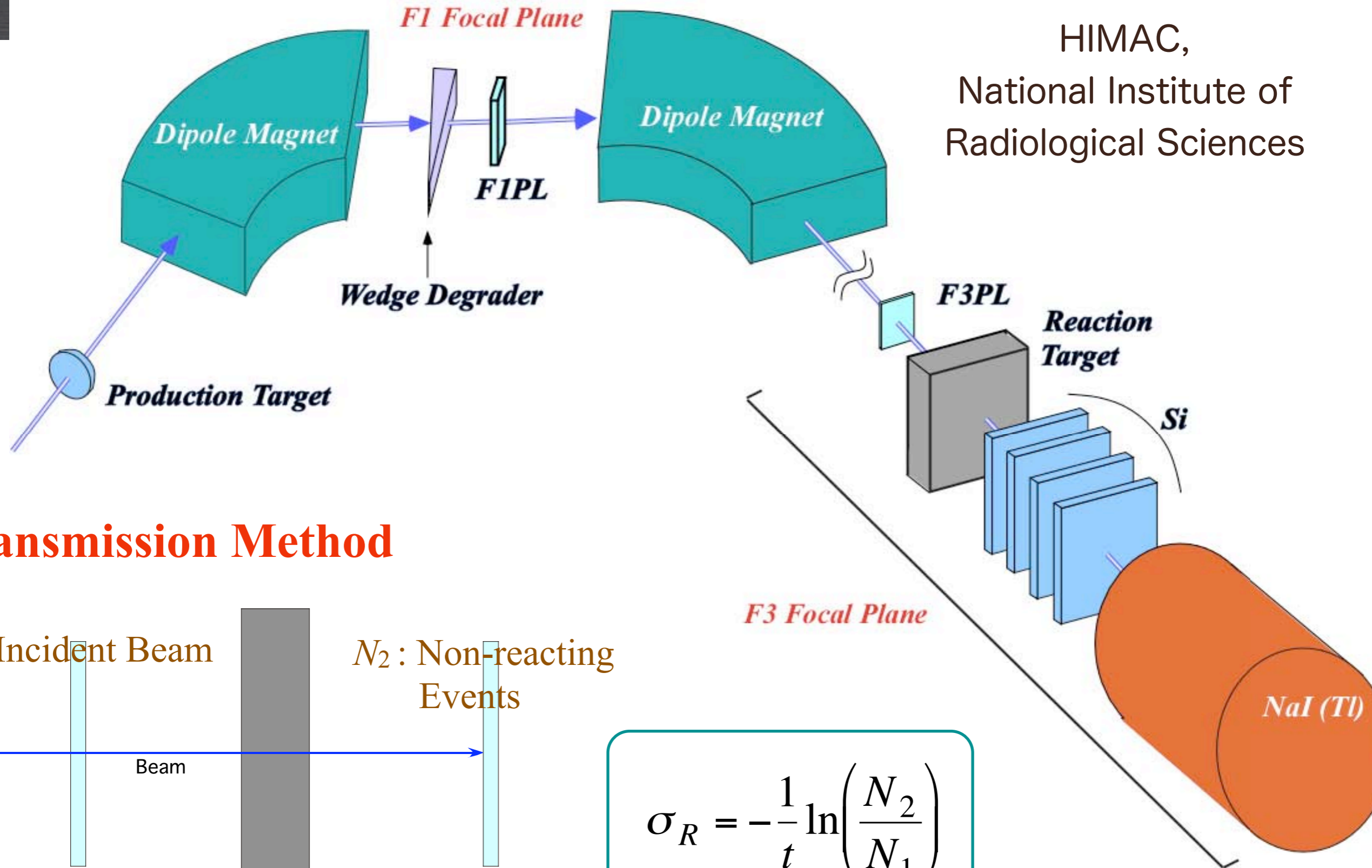
Investigation

Measurements of σ_R for ^{12}C , ^{11}Be

Experiment

^{12}C on Be, C, Al and ^{11}Be on Be

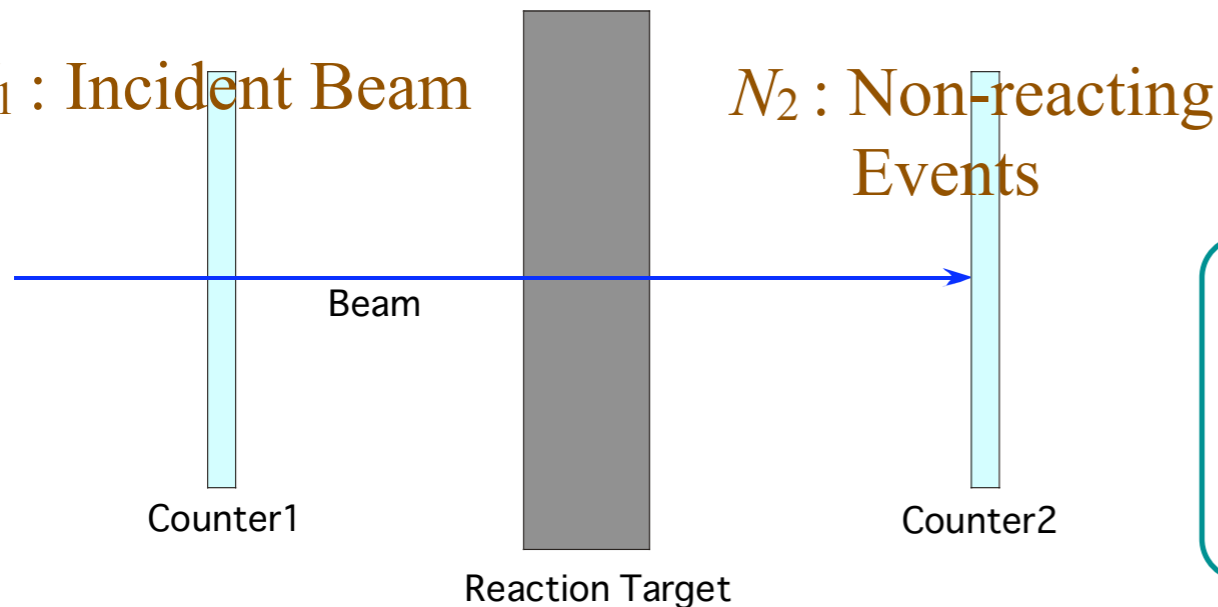
HIMAC,
National Institute of
Radiological Sciences



Transmission Method

N_1 : Incident Beam

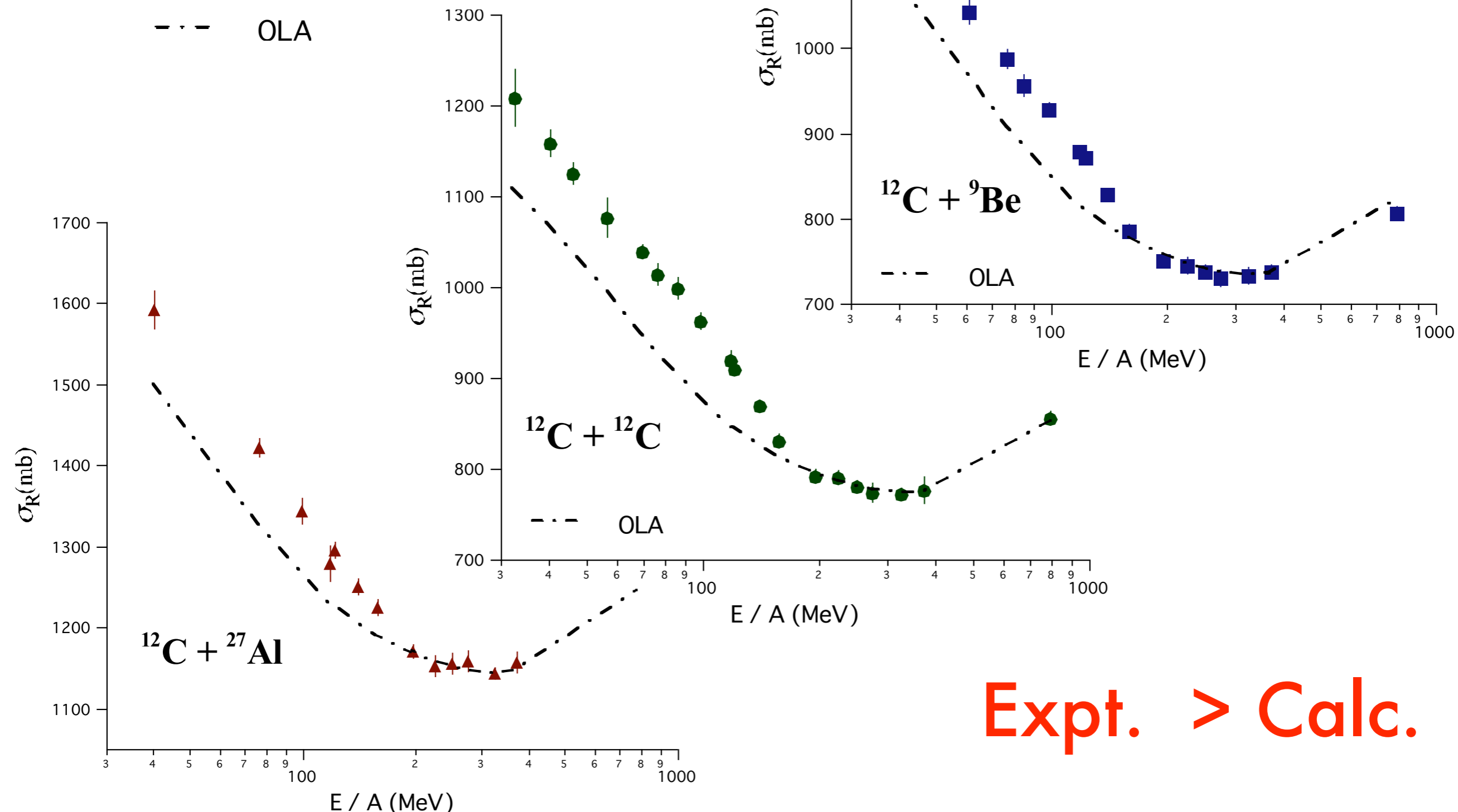
N_2 : Non-reacting Events



$$\sigma_R = -\frac{1}{t} \ln\left(\frac{N_2}{N_1}\right)$$

Result of σ_R for ^{12}C

Comparison with
Glauber Calculation
(OLA, Zero-Range)



Improvement of Galuber Calculation ~ 3 Points ~

● *Neglect of Internal Motion of Nucleons*

$$E_{\text{nucleon}} = E_{\text{proj}}$$



Take into Account Fermi Motion Effect

● *Optical Limit Approximation*

Not Appropriate for Halo Nucleus



Take into Account Multiple Scattering Effect
(Important for Halo Nucleus.)

B. Abu-Ibrahim and Y. Suzuki PRC **62** (2000) 034608.

● *Zero - Range Approximation*

Zero Nucleon - Nucleon Range



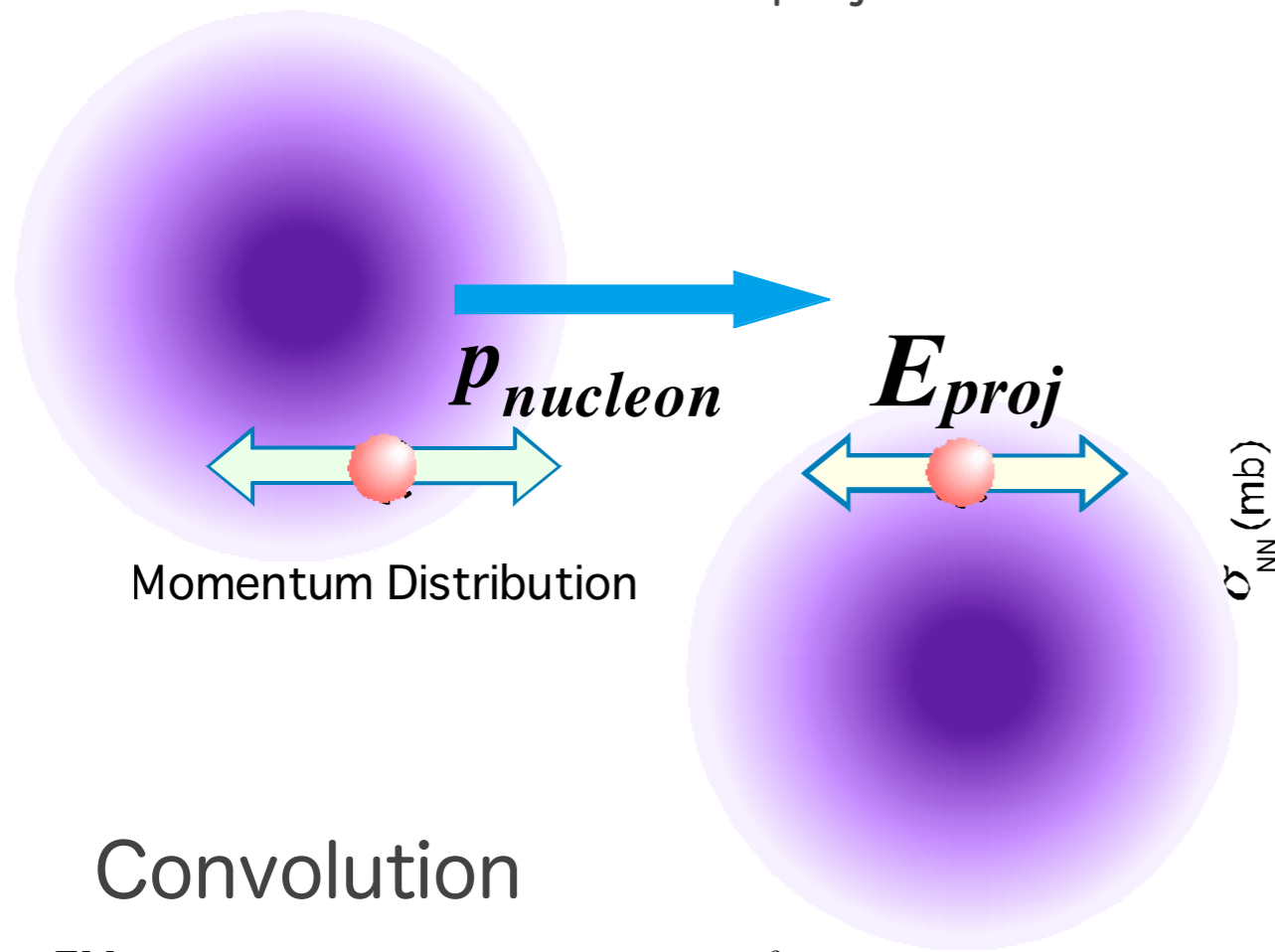
Finite Range Calculation

Modifications for Galuber Calculation ~ 3 Points ~

~~Neglect of Internal Motion of Nucleons~~

$$E_{\text{nucleon}} = E_{\text{proj}}$$

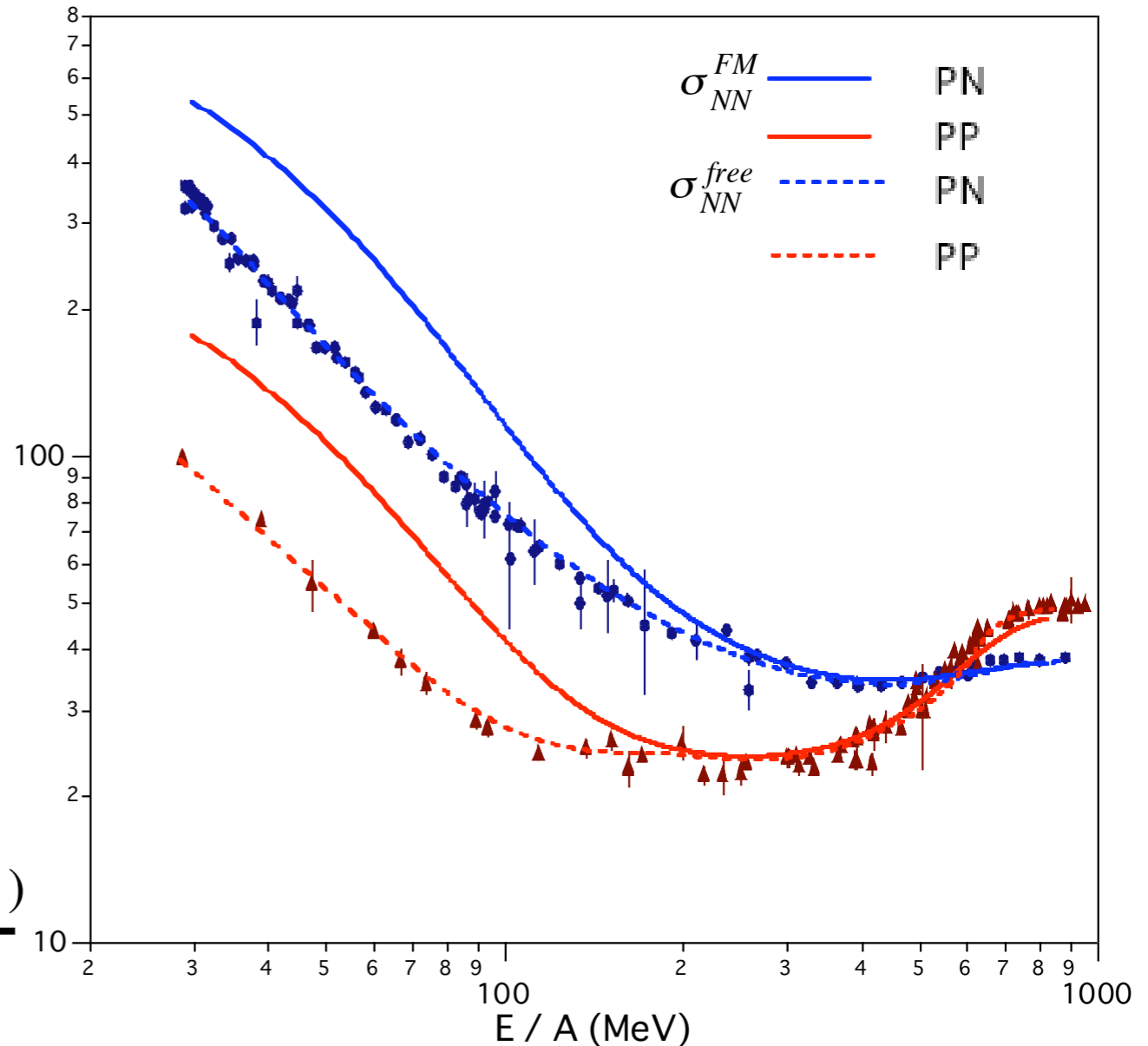
Take into Account Fermi Motion Effect



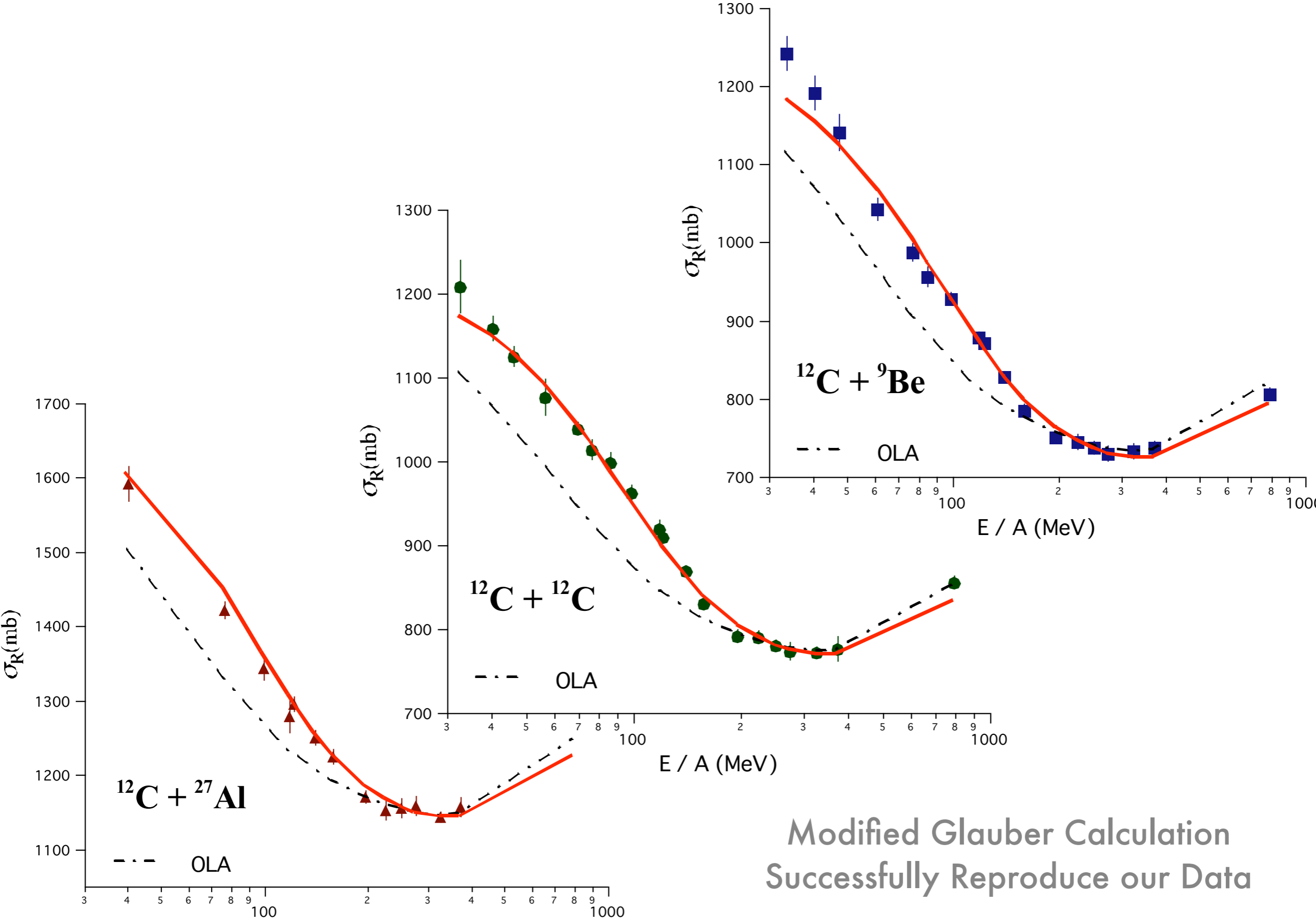
Convolution

$$\sigma_{NN}^{FM}(E_{\text{nucleon}}) = \int_{-\infty}^{+\infty} dp_{\text{nucleon}} \sigma_{NN}^{\text{free}}(p_{\text{nucleon}}) \underbrace{P(p_{\text{nucleon}})}_{\text{Momentum Distribution}}$$

Momentum Distribution



Modified Glauber Calculation and Data of ^{12}C

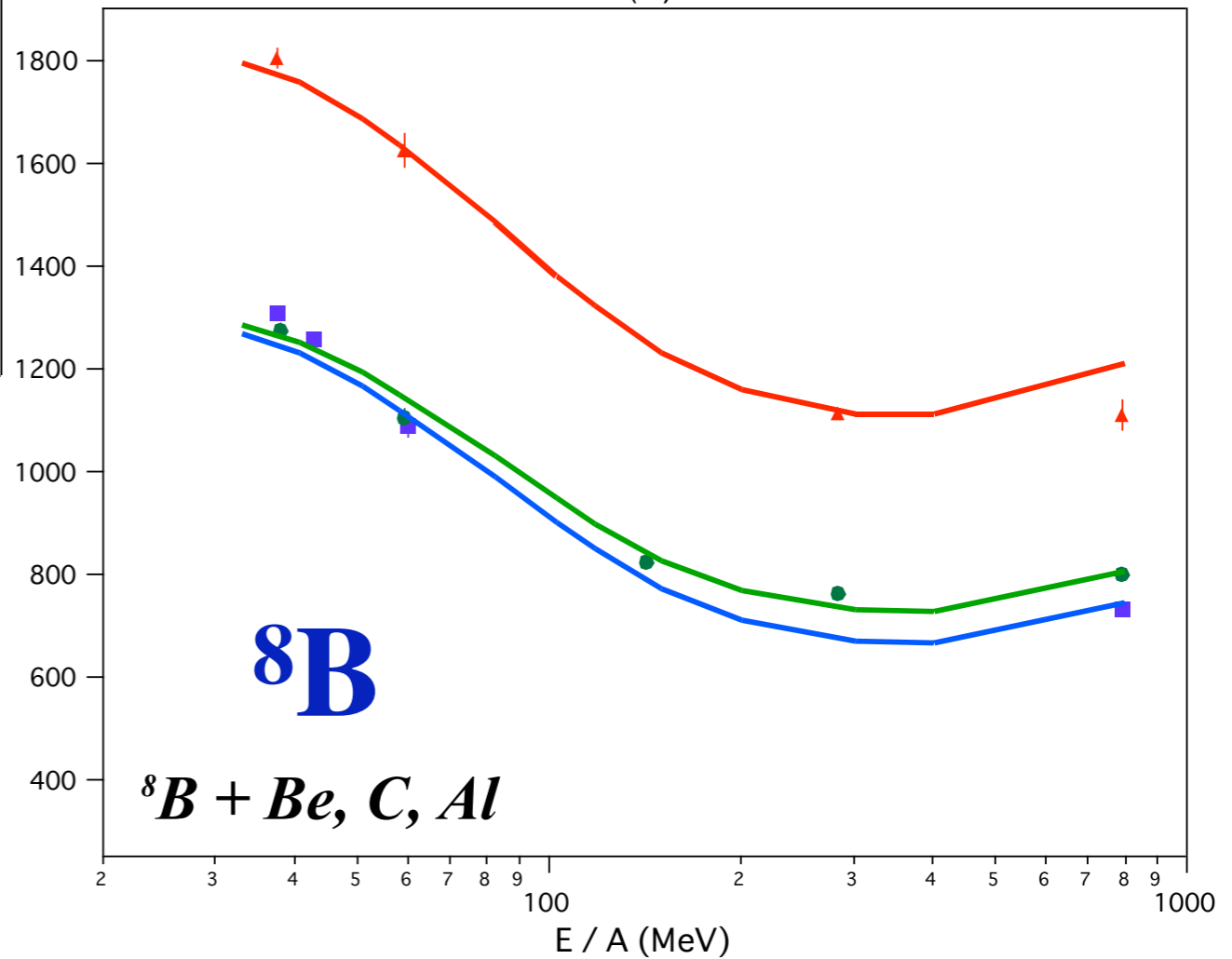
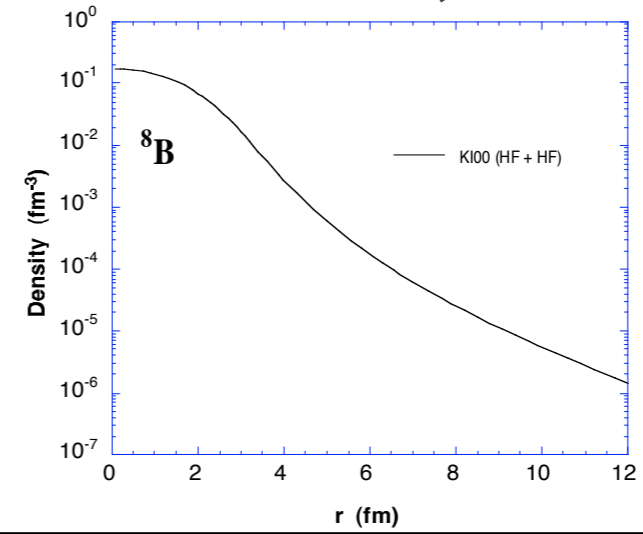
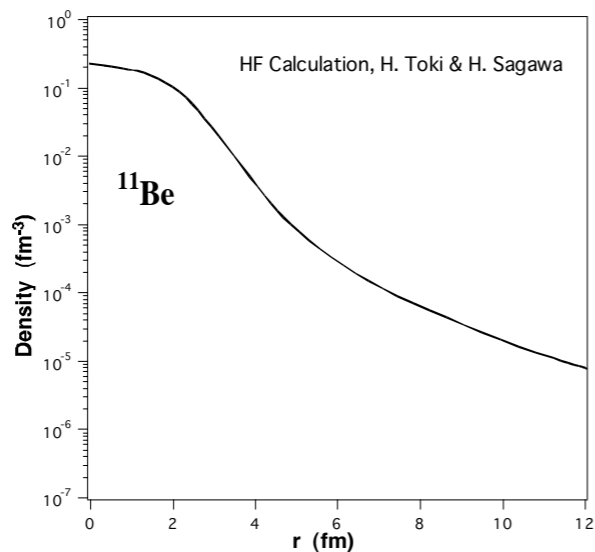
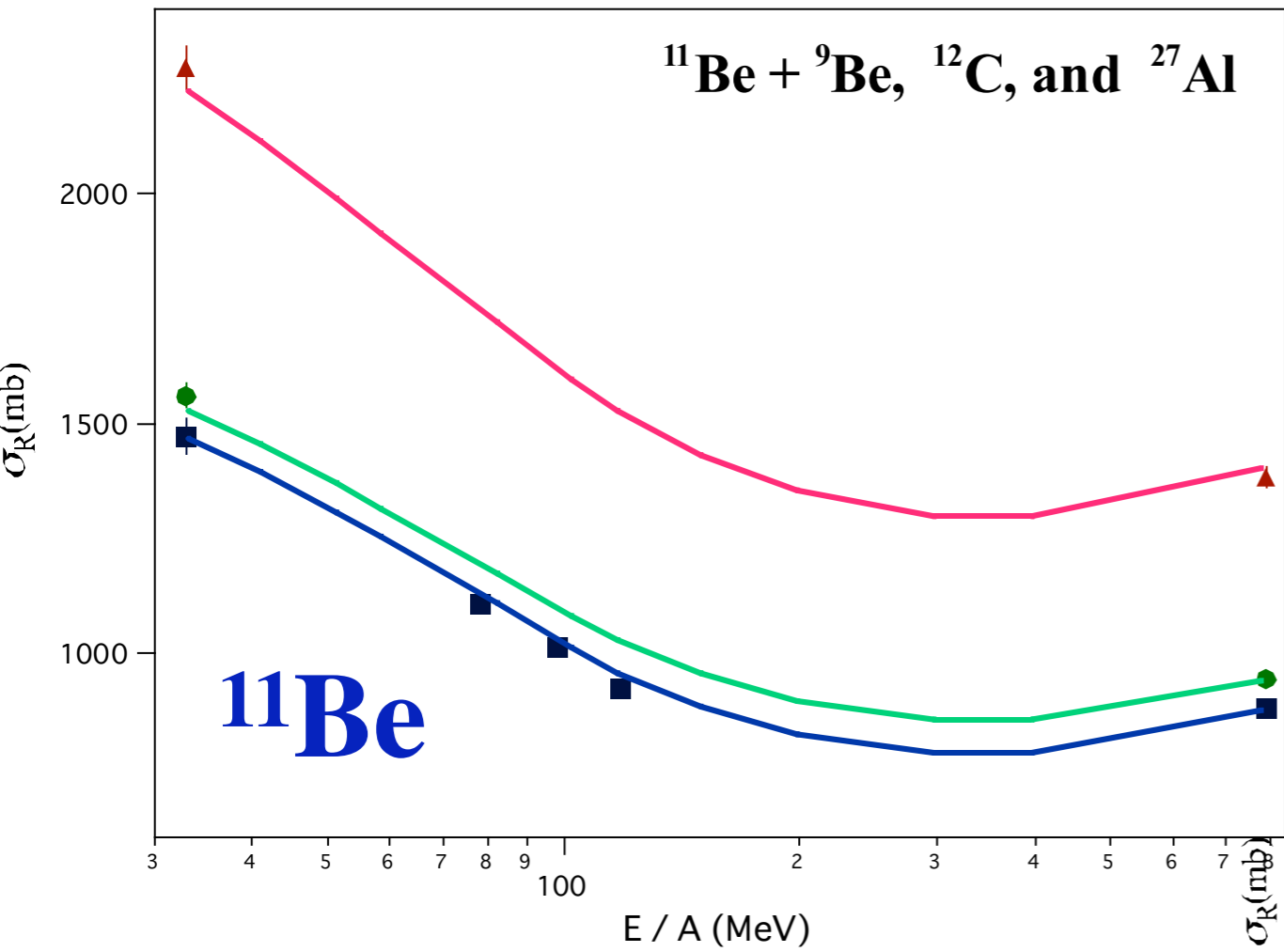


Modified Glauber Calculation
Successfully Reproduce our Data

Comparison with the Data for Unstable Nuclei


Well-Known Halo Nuclei

^{11}Be , ^8B




M. Fukuda et al., Nucl. Phys. A **656** (1999) 209.
I. Tanihata et al., Phys. Lett. **206B** (1988) 592

B. Blank et al., Nucl. Phys. A **624** (1997) 242.
M. Obuti et al., Nucl. Phys. A **609** (1996) 74.



Modified Glauber Calculation successfully reproduces σ_R for various nuclei including halo nuclei.
The Problem ($\sigma_{R(\text{calc.})} < \sigma_{R(\text{Expt.})}$) has been solved.



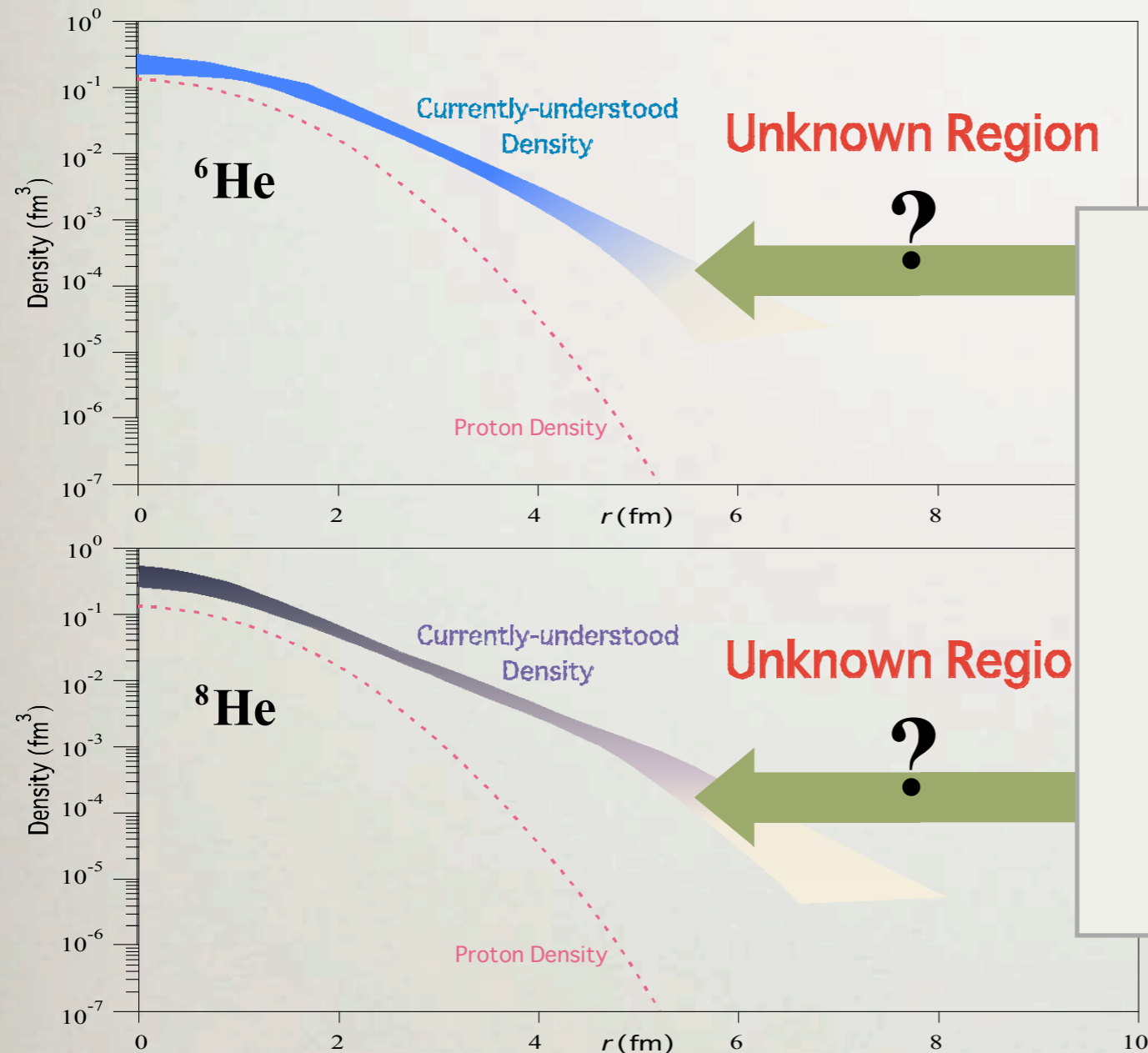
Now we can deduce nucleon density
distributions of unstable nuclei

We have already investigated several nuclei.

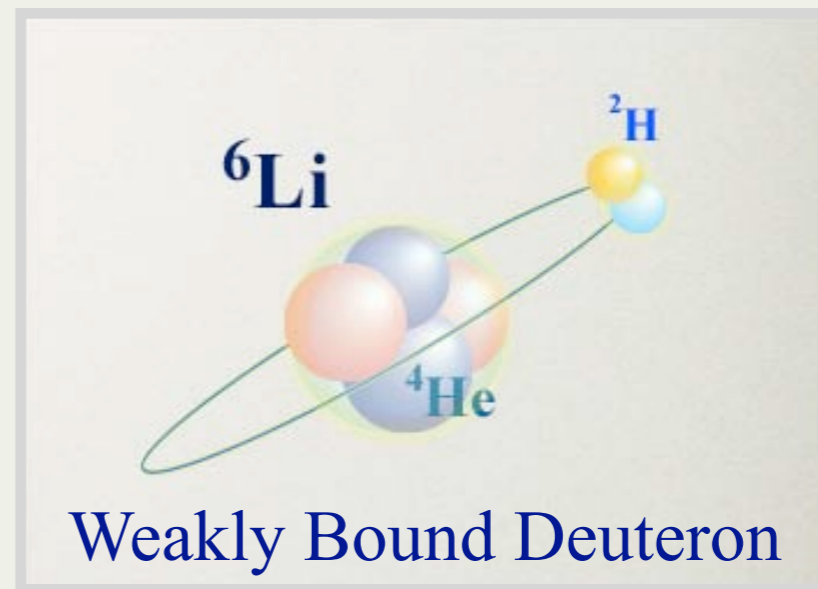
${}^6\text{He}$, ${}^8\text{He}$, and ${}^6\text{Li}$

Skin and Halo Nuclei

${}^6\text{He}$, ${}^8\text{He}$ so-called **Neutron-Skin Nuclei**



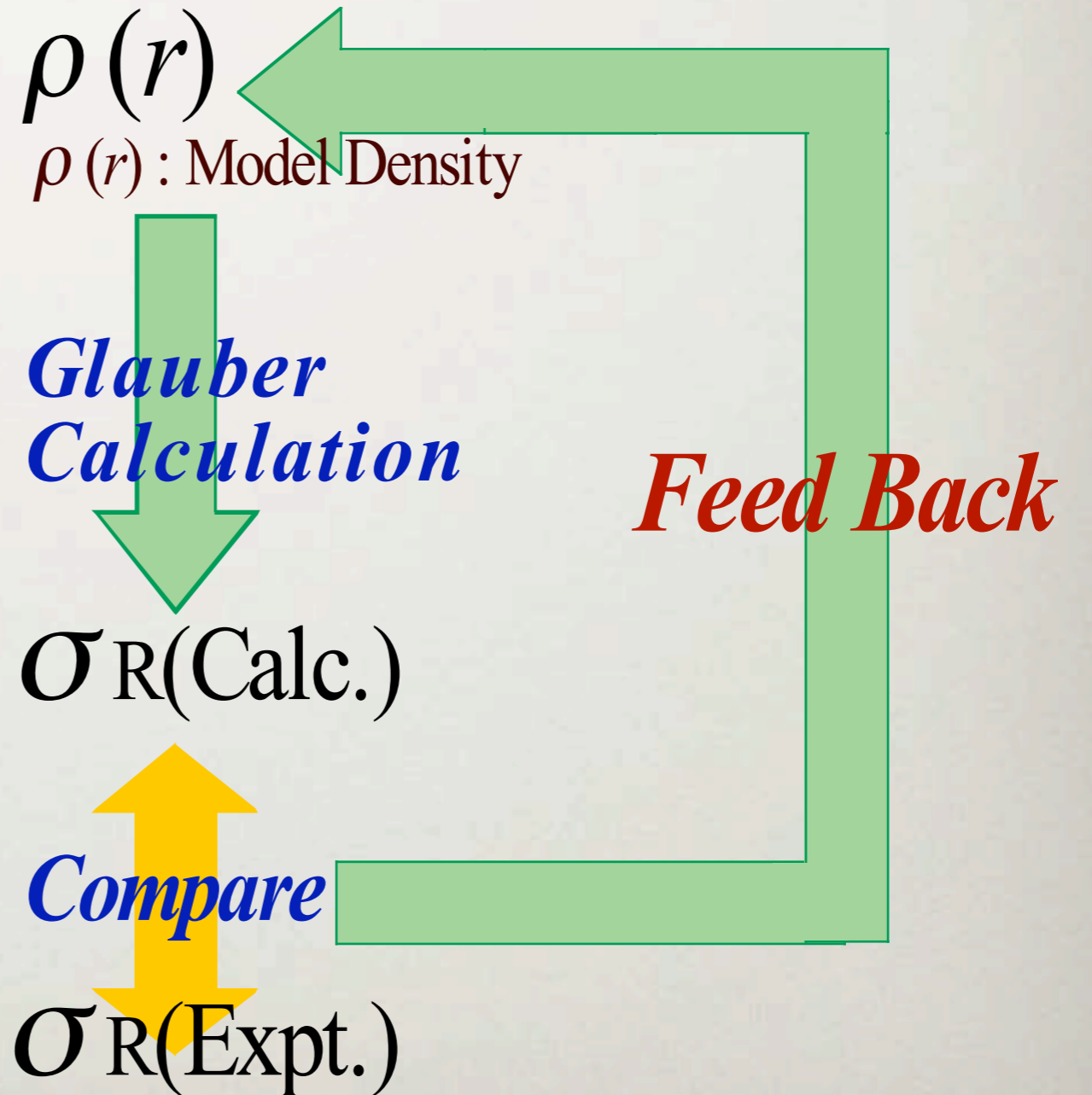
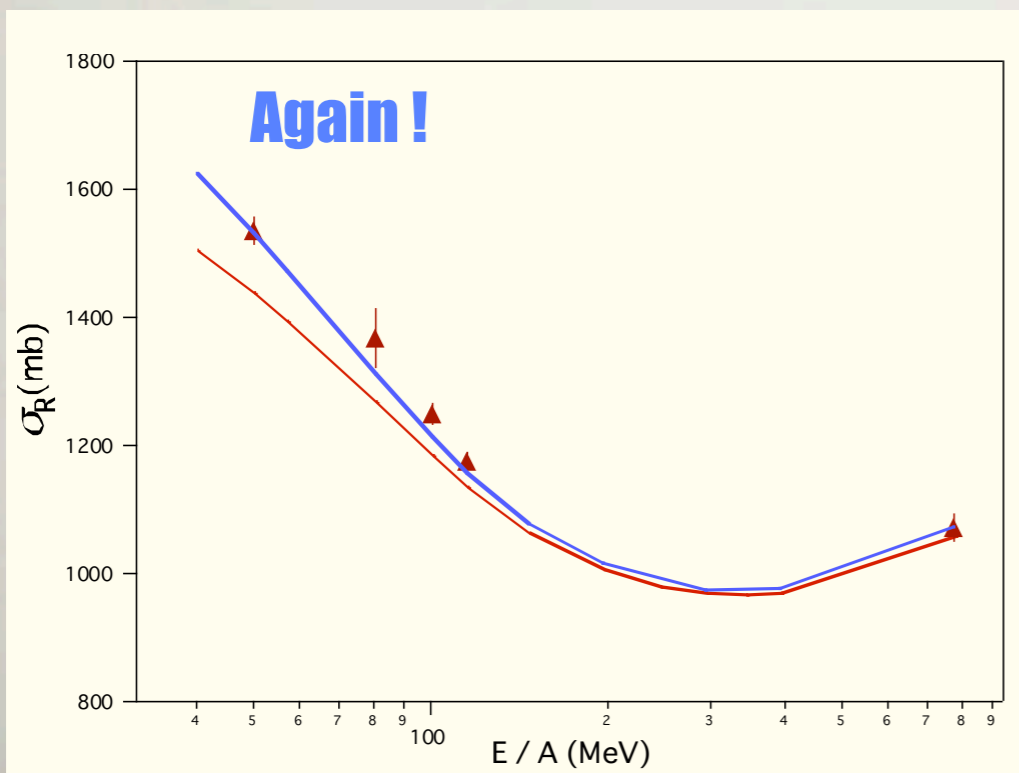
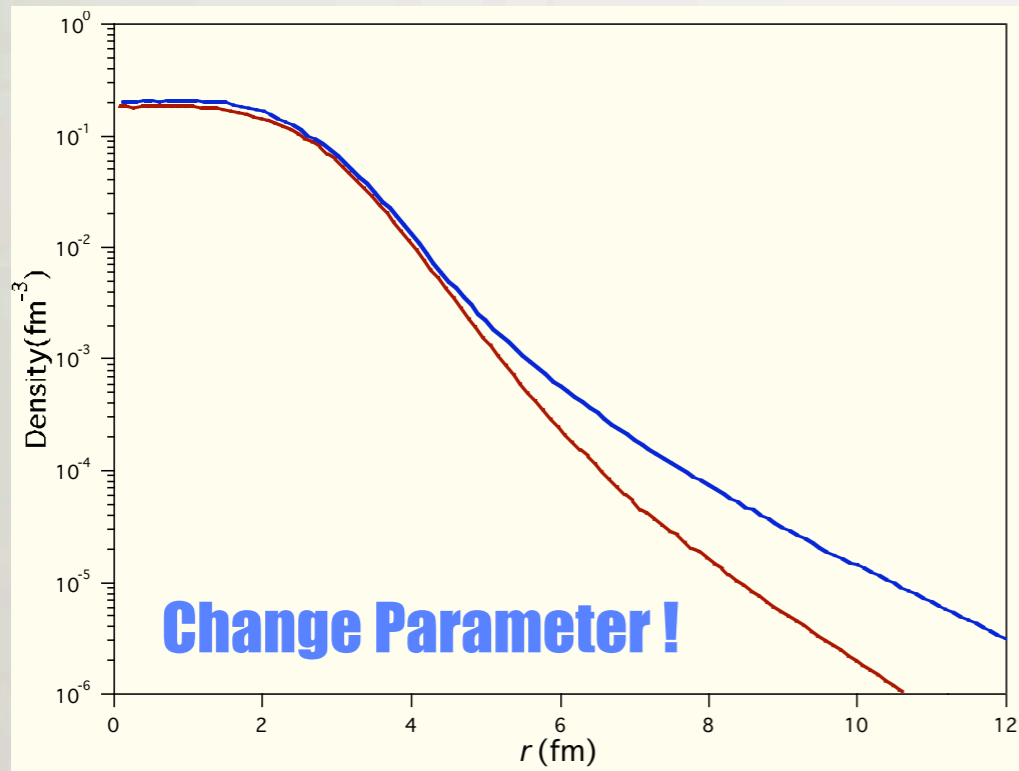
and ${}^6\text{Li}$ Cluster Structure



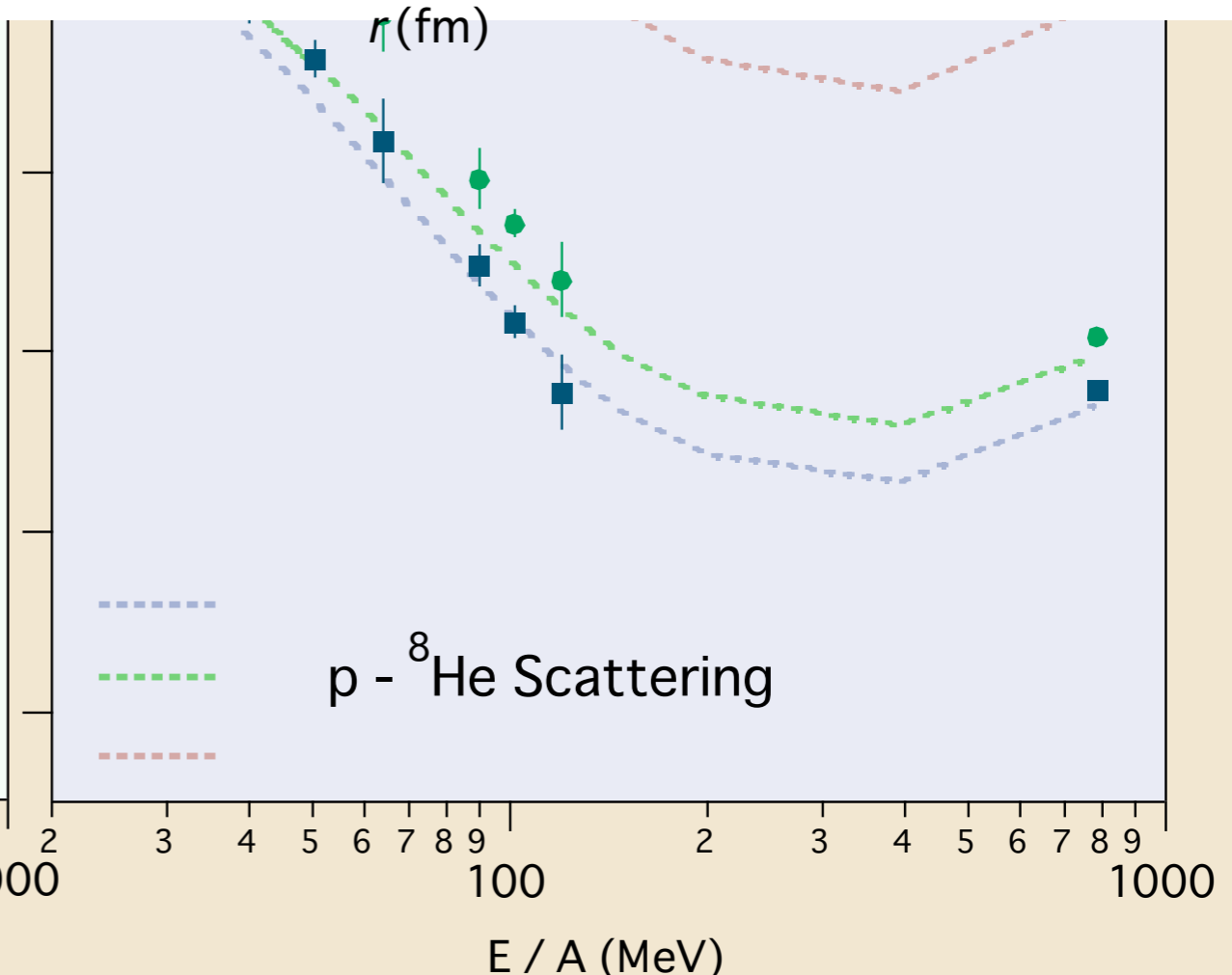
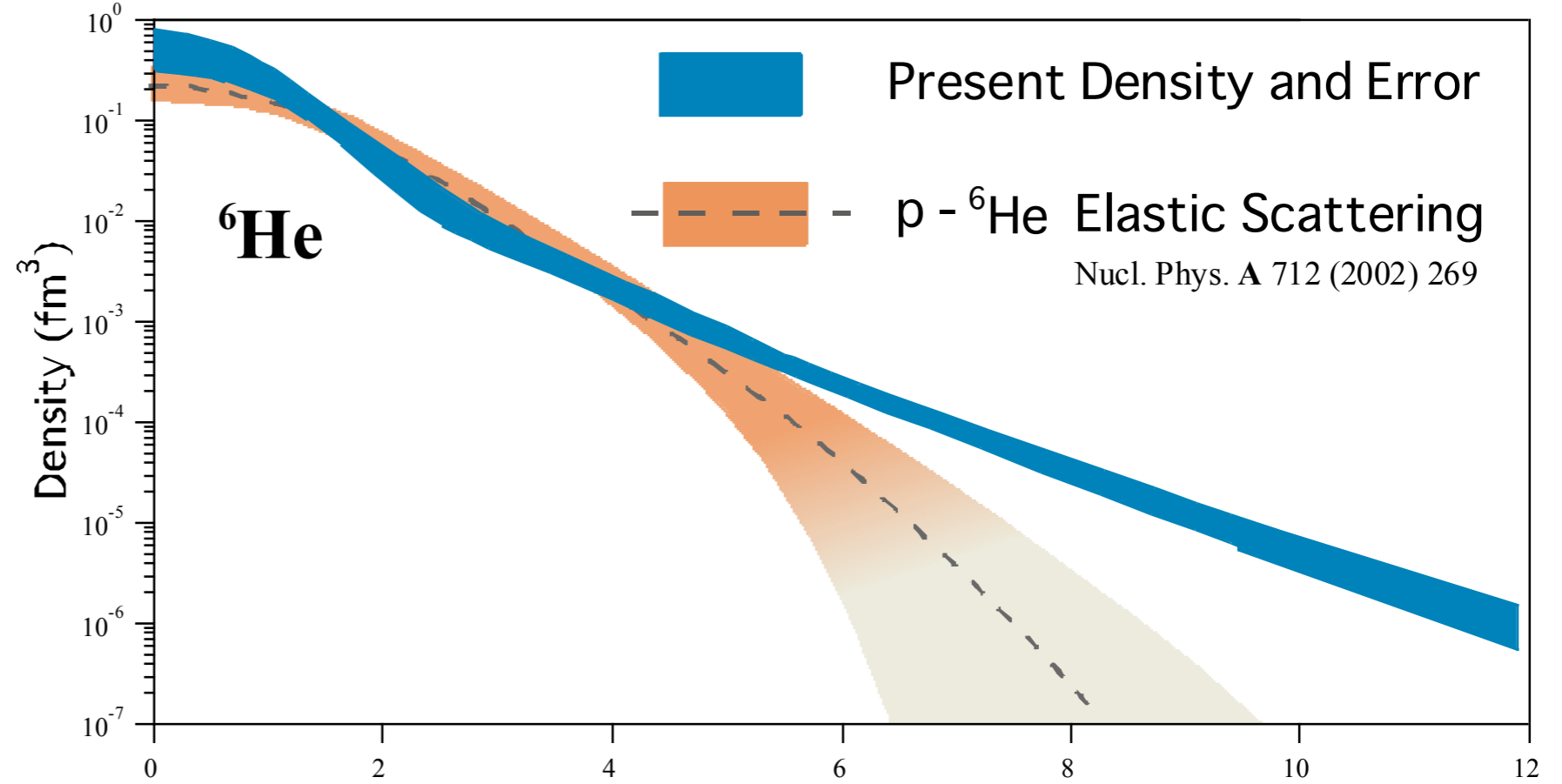
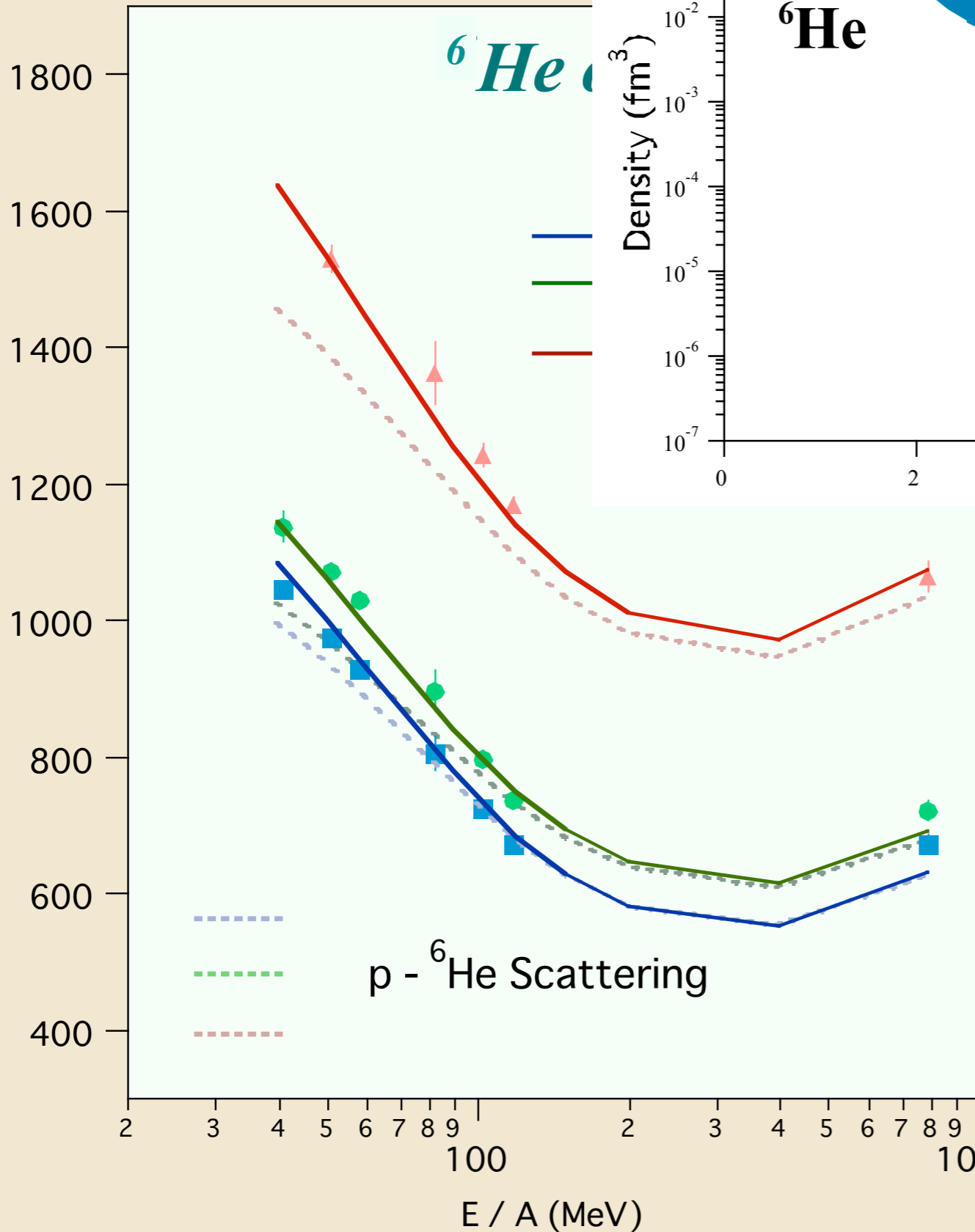
*It is not Clear whether there is Halo Tail
Halo or Skin ?*

How to Deduce Nucleon Density Distribution

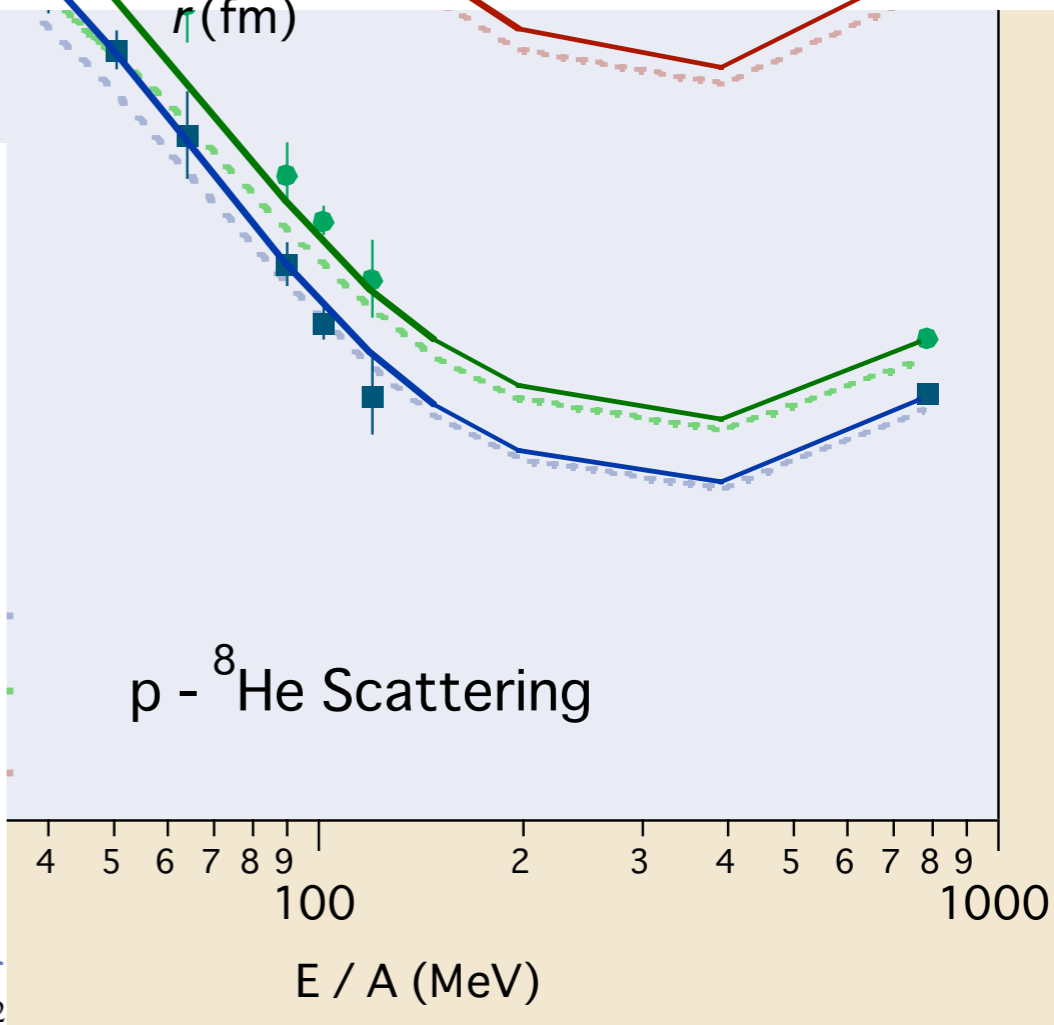
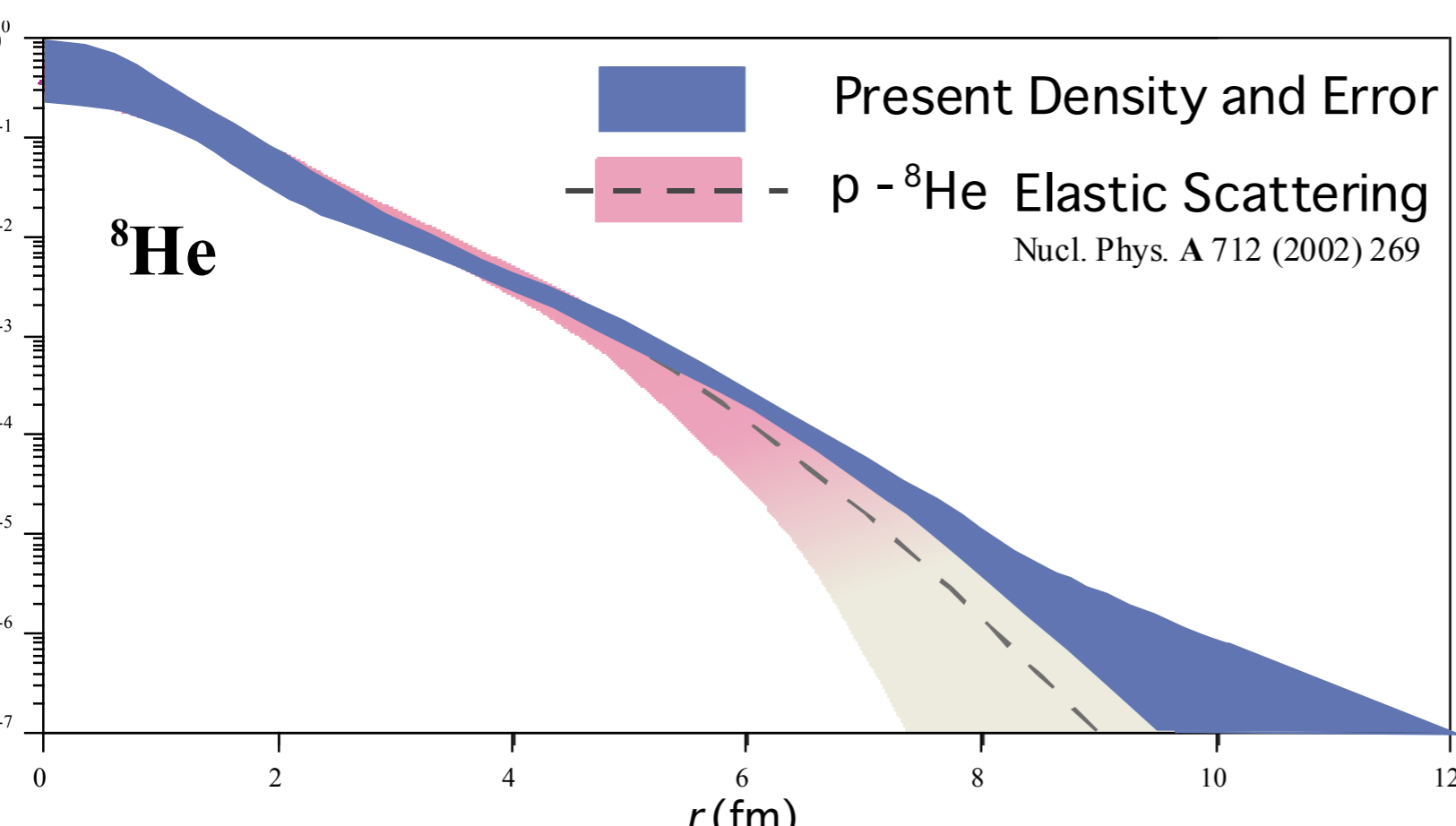
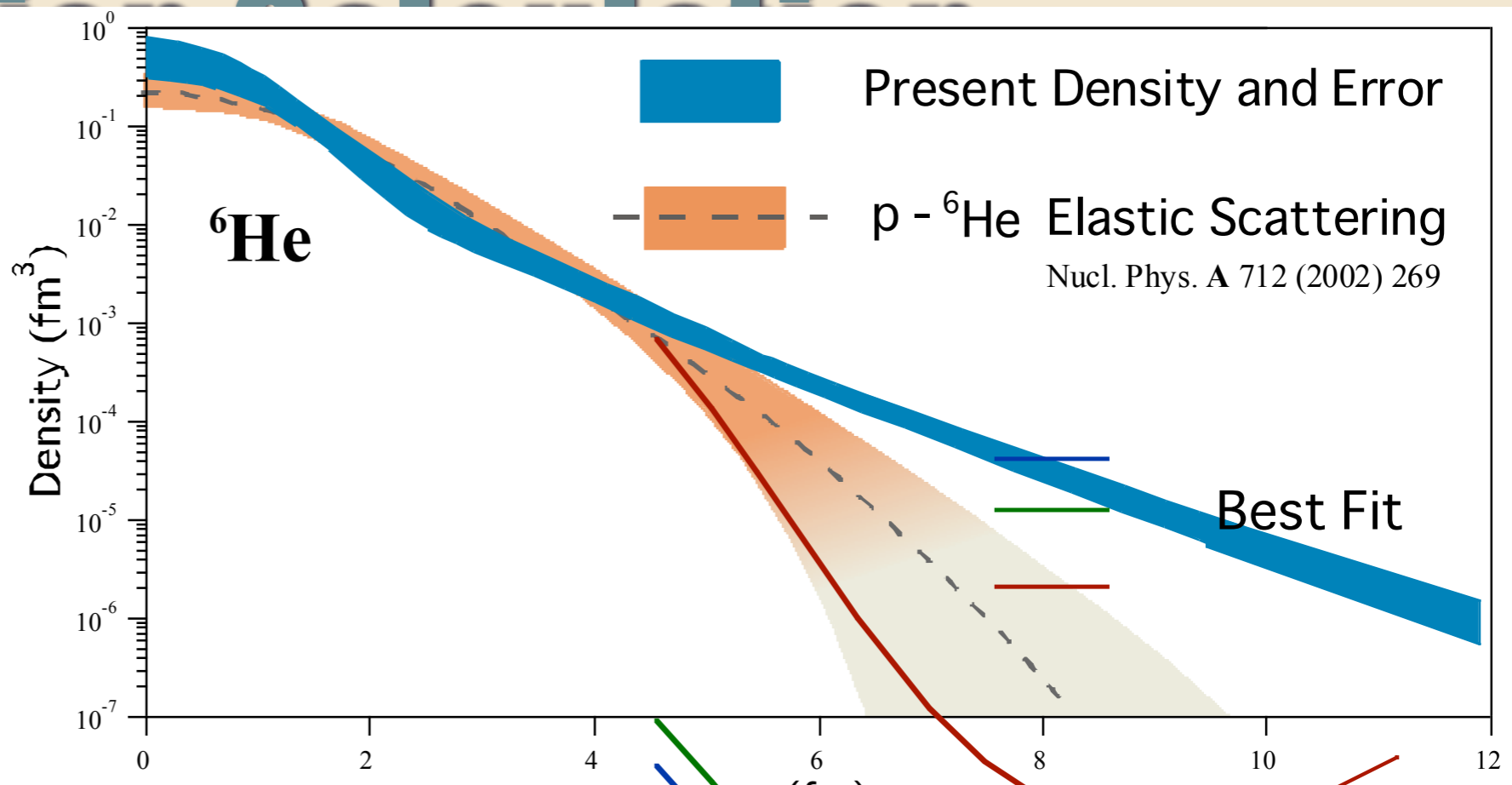
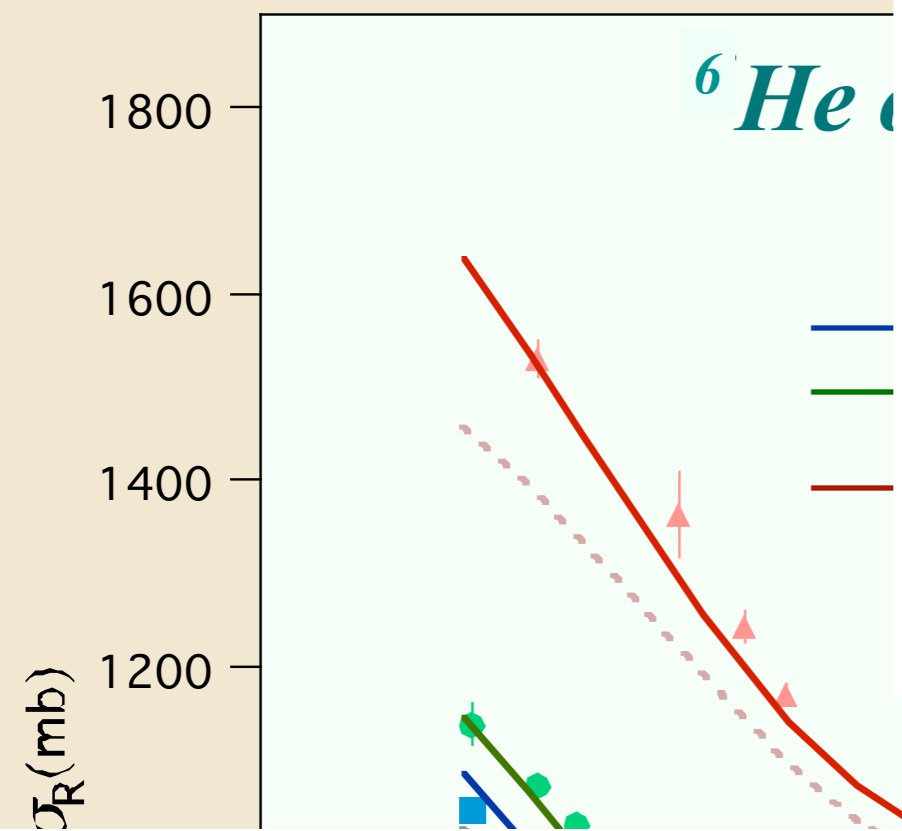
~ χ^2 fitting procedure ~



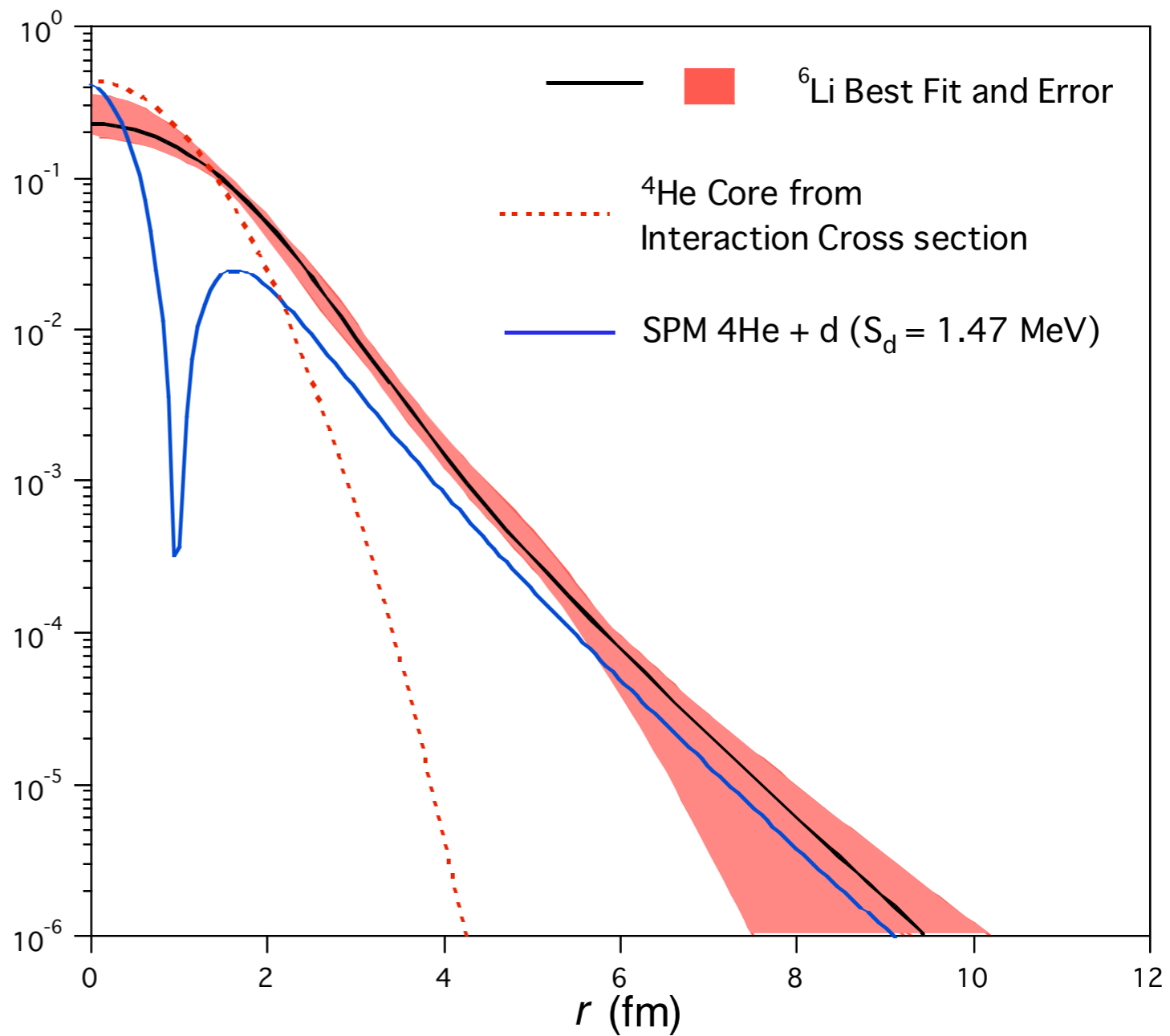
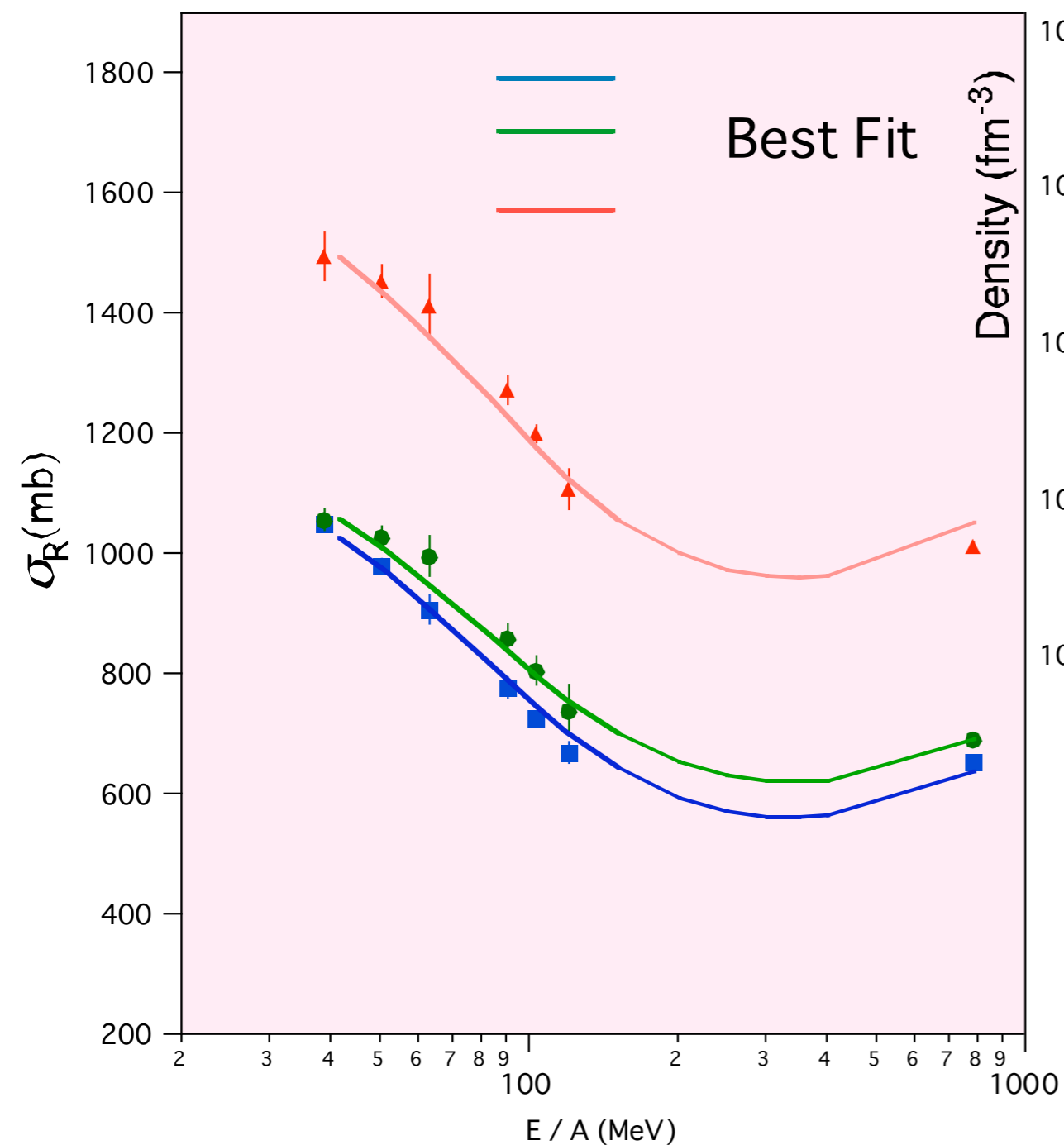
Cross Sect






Cross Sect



Result for ${}^6\text{Li}$



Summary

-  We precisely measured reaction cross sections for ^{12}C and ^{11}Be at intermediate energies to investigate the applicability of Glauber Calculation to the intermediate energy region.
-  By taking into account Fermi-Motion Effect, Multiple Scattering Effect, and Finite Range Effect, Glauber Calculation successfully reproduce the data.
-  Using Modified Glauber Calculation, investigations of nucleon density distributions for various nuclei will be carried out.