

# Deformation of the N=Z nucleus $^{72}\text{Kr}$ via beta decay

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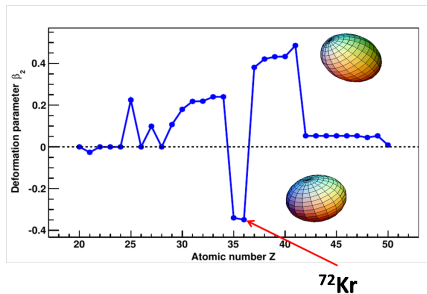
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*for the IS370 collaboration*

*"Advances in Radioactive Isotope Science Conference 2014"*  
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*1-6 June 2014*

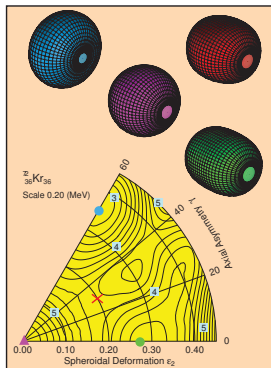
# Motivation: Why $^{72}_{36}\text{Kr}$ ?

Only  $^{70}\text{Br}$  and  $^{72}\text{Kr}$  predicted oblate deformed in the N=Z line from A=40 up to A=100.



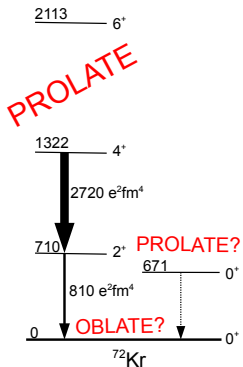
P. Möller et al., *At. Data and Nucl. Data Tables* 59, 185 (1995)

Predictions of **shape coexistence** in  $^{72}\text{Kr}$ :  
*"the poster child of nuclear shape isomers"*



P. Möller et al., *Phys. Rev. Lett.* 103, 212501 (2009)

# Motivation: Why ${}^{72}_{36}\text{Kr}_{36}$ ?



- ${}^{72}\text{Kr}$  ground state predicted oblate deformed [Naz85, Mol95].
- High spin states interpreted as a prolate band [DeA97]
- First excited 0<sup>+</sup> state: shape isomer head of the prolate band [Bou03]. Mixing  $\lambda=0.1$  with the 0<sup>+</sup> oblate gs (two-level calculation).
- $B(E2; 0_1^+ \rightarrow 2_1^+) = 4997(647) e^2\text{fm}^4$  [Gad05]  $\rightarrow |\beta_2| = \mathbf{0.330(21)}$ .  
 $\swarrow$   
 $B(E2; 2_1^+ \rightarrow 0_1^+) = 999(129) e^2\text{fm}^4$
- IS478 experiment (spokeperson B.S. Nara Singh, Univ. York) at ISOLDE (CERN) of  ${}^{72}\text{Kr}$  Coulex whose preliminary results indicate 2<sub>1</sub><sup>+</sup> state is prolate deformed.
- Recent results already shown today in H. Iwasaki talk [Iwa14]:  
 $B(E2, 4_1^+ \rightarrow 2_1^+) = 2720(550) e^2\text{fm}^4 \rightarrow \mathbf{2_1^+ \text{ Prolate}}$ ;  
 $B(E2, 2_1^+ \rightarrow 0_1^+) = 810(150) e^2\text{fm}^4 \rightarrow$  Small overlap between 0<sup>+</sup> and 2<sup>+</sup> w.f.  
 $\frac{B(E2; 4_1^+ \rightarrow 2_1^+)}{B(E2; 2_1^+ \rightarrow 0_1^+)} = \mathbf{3.4}$ ; 1.43 (rotor) and 2.0 (vibrator).

However, **no evidence on the sign of the ground state deformation** (prolate or oblate).

[Naz85] W. Nazarewicz *et al.*, Nucl. Phys. **A435**, 397 (1985)

[Mol95] P. Möller *et al.*, At. Data Nucl. Data Tables **59**, 185 (1995)

[DeA97] G. de Angelis *et al.*, Phys. Lett. B **415**, 217 (1997)

[Bou03] E. Bouchez *et al.*, Phys. Rev. Lett. **90**, 082502 (2003)

[Gad05] A. Gade *et al.*, Phys. Rev. Lett. **95**, 022502 (2005)

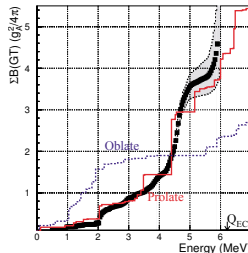
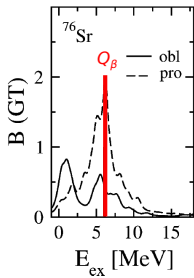
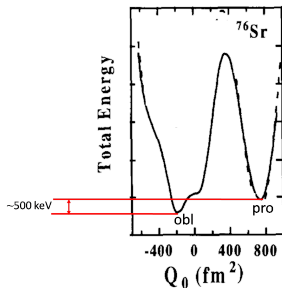
[Iwa14] H. Iwasaki *et al.*, Phys. Rev. Lett. **112**, 142502 (2014).

## Determination of nuclear shape via B(GT) distributions

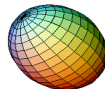
GT strength distributions found to **depend sensitively on the nuclear shape** (quadrupole deformation) for  $^{80}\text{Zr}$ ,  $^{76}\text{Sr}$  and  $^{72}\text{Kr}$  [Ham95].

Mean field calculations [Sar99] and [Sar01] predict **different B(GT) distributions for different deformations of the ground state of the parent nucleus.**

### $^{76}\text{Sr}$ (next N=Z even-even nucleus)



Prolate



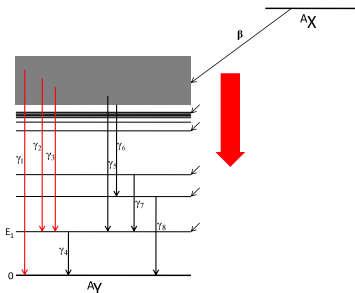
[Ham95] I. Hamamoto et al., Z. Phys. A353, 145 (1995)

[Sarr99] P. Sarriguren et al., Nucl. Phys. A658, 13 (1999)

[Sarr01] P. Sarriguren et al., Nucl. Phys. A691 631 (2001)

[Nac04] E. Náchter et al., PRL 92 232501 (2004)

# Determination of the beta feeding distribution



C.L. Duke *et al.*, Nuclear Physics A151, 609 (1970)

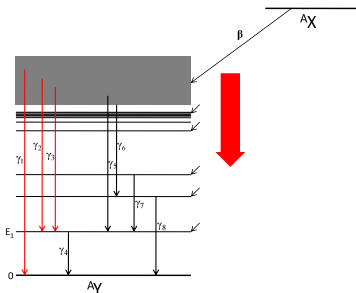
B. Rubio *et al.*, J. Phys. G 31, S1477 (2005)

- **High density of levels** for high excitation energies causing **very fragmented feeding distribution and de-excitation pattern**
- **Low photopeak efficiency** for high energy gammas with HPGe detectors
- Apparent strength is located at lower energies
- **As a result:** overestimated strength at low excitation energies and underestimated for high excitation energies

## Pandemonium effect

J.C. Hardy *et al.*, Phys. Lett. 71B, 307 (1977)

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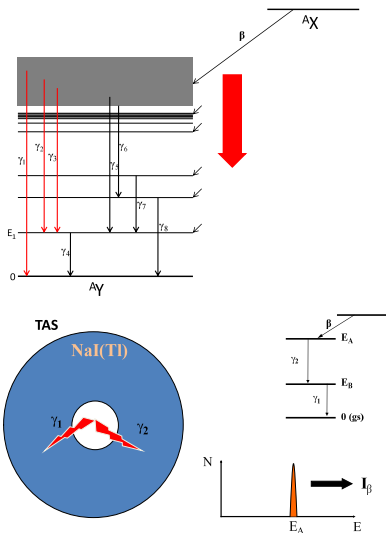
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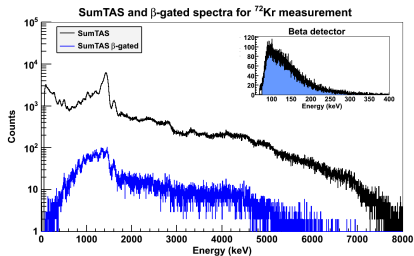
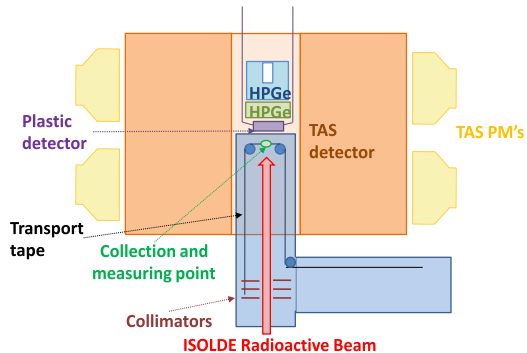
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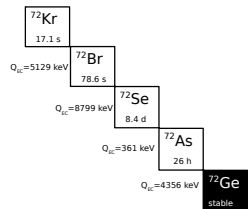
J.C. Hardy *et al.*, Phys. Lett. **71B**, 307 (1977)

# TAS experimental setup



Reduced statistics in  $\beta$ -gated spectrum due to:

- **Geometric efficiency of beta detector:**  
 $\approx 16\%$
- **Room background** suppressed by shielding components and coincidence condition.





# TAS data analysis

- **Experimental data (d)** is the result of the convolution of **Response function (R)** of TAS detector and the **feeding at a certain level (f)**:

$$d(i) = \sum_j R(i, j) \otimes f(j) + \text{contam.}$$

- Solve the **Inverse problem** with the *Expectation-Maximization Algorithm* [Dem77]:

$$f^s(j) = \frac{1}{\sum_i R(i, j)} \sum_i \frac{R(i, j) f^{s-1}(j) d(i)}{\sum_j R(i, j) f^{s-1}(j) + \text{contam.}}$$

$f^0$  is chosen as an uniform feeding distribution.

The application of this algorithm to the TAS problem is explained in detail in [Tai07]

**Relative gamma transition intensities measured with the HPGe detector are included in  $d(i)$ .**

Through this methodology we try to **reproduce both**:

- the **TAS experimental spectrum** and
- the **relative gamma transition intensities**.

[Dem77] A. P. Dempster *et al.* J. R. Statist. Soc. B 39 (1977) 1

[Tai07] J. L. Tañ, D. Cano-Ott Nucl. Inst. and Meth. A 571, (2007) 719 and 728

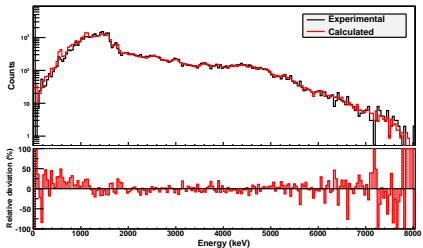
- **RESPONSE MATRIX (R)** is obtained from Monte Carlo simulations (GEANT4) and decay scheme information (High Resolution information available+Statistical Models).

# Beta gated analysis: Check of goodness

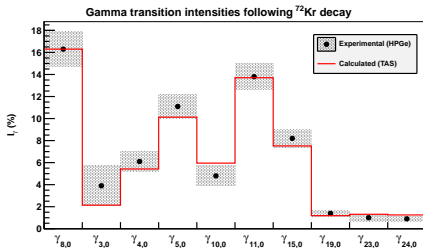
Check of results:

Reproduction of experimental TAS spectrum:

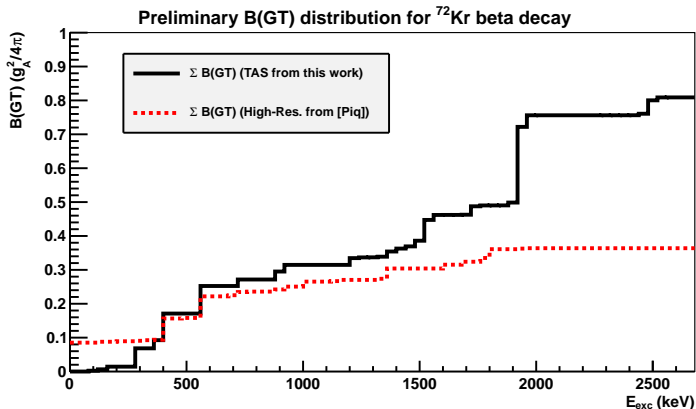
$$d(i) = \sum_j R(i, j) \otimes f(j) + \text{contam.}$$



Reproduction of gamma transition intensities measured with HPGe detector (10 most intense lines reaching the ground state).



# Result from first set of data

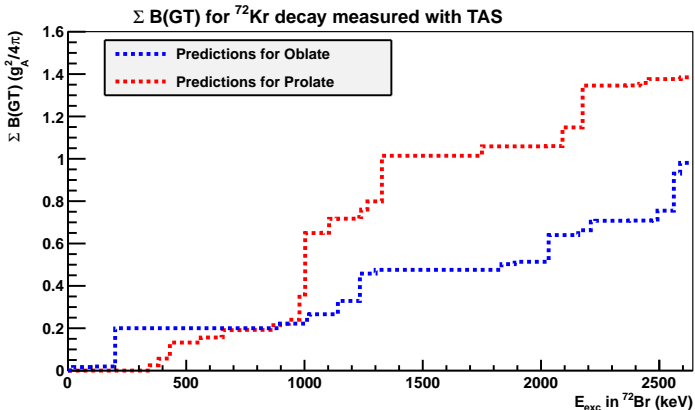


Result from the analysis of only a set of data, not full statistics.

**Evidence of “Pandemonium effect”**

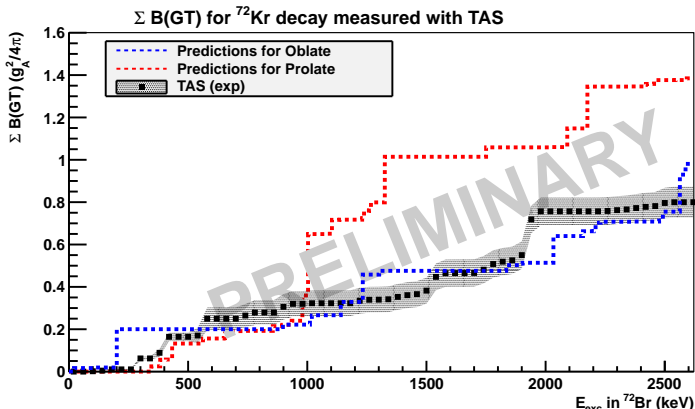
[Piq] I. Piquer *et al.*, *Eur. Phys. J. A* **16**, 313-329 (2003)

## Comparison with theoretical predictions (QRPA)



QRPA approach using the SLy4 Skyrme-type force for the oblate and prolate minima in the  $^{72}\text{Kr}$  potential energy surface. A standard quenching factor of 0.77 is used [Sar09].

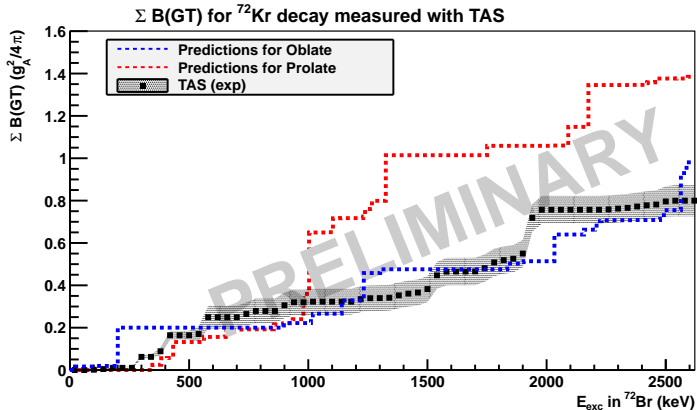
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[Sar09] P. Sarriguren, Phys. Rev. C **79**, 044315 (2009)

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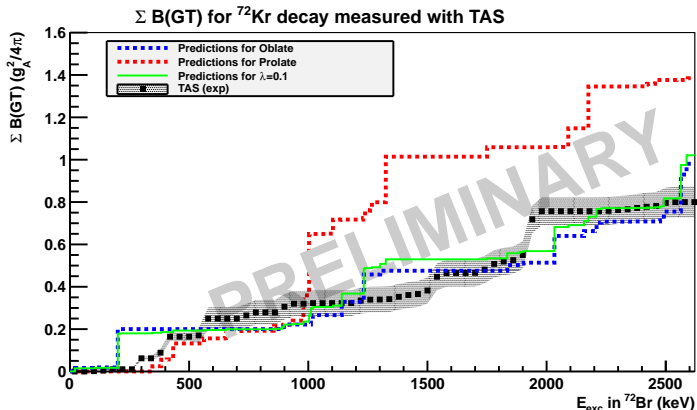
Preliminary results suggest:

- First experimental evidence of the negative sign of quadrupole moment of  $^{72}\text{Kr}$  gs  $\rightarrow \beta_2 < 0$ .
- First time an oblate deformed gs has been inferred from the B(GT) distribution of its  $\beta$  decay.

Oblate minimum corresponds to  $\beta_2 \approx -0.176$  (th.)

[Sar09] P. Sarriguren, Phys. Rev. C **79**, 044315 (2009)

## Comparison with theoretical predictions (QRPA)



Preliminary results are compatible with 10 % mixing<sup>1</sup> [Bou03] with the prolate  $0^+$  excited state but no improvement is observed.

[Sar09] P. Sarriguren, Phys. Rev. C **79**, 044315 (2009)

[Bou03] E. Bouchez et al., Phys. Rev. Lett. **90**, 082502 (2003)

<sup>1</sup>The distribution for 10 % mixing ratio is a rough estimation to guide the eye (0.1 times the value of  $B(\text{GT})$  for prolate minimum plus 0.9 times the value for the oblate minimum) and not strictly an appropriate calculation.

# Conclusions

- 1 The preliminary results from our study suggest a **dominantly oblate deformation of the  $^{72}\text{Kr}$  in the ground state.**



- 2 Preliminary, we conclude that it is the **first time an oblate deformed gs** has been **inferred from the B(GT) distribution** of its  $\beta$  decay. **First experimental evidence of the sign of the deformation** (and the intrinsic quadrupole moment) of the  $^{72}\text{Kr}$  ground state.
- 3 The preliminary experimental B(GT) distribution **does not exclude a certain prolate mixing** for the dominantly oblate ground state but it does not improve the experiment-theory agreement.



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J. A. Briz<sup>1</sup>, M. J. G. Borge<sup>1</sup>, O. Tengblad<sup>1</sup>,  
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<sup>6</sup> ISOLDE, CERN, CH-1211 Geneva 23, Switzerland.