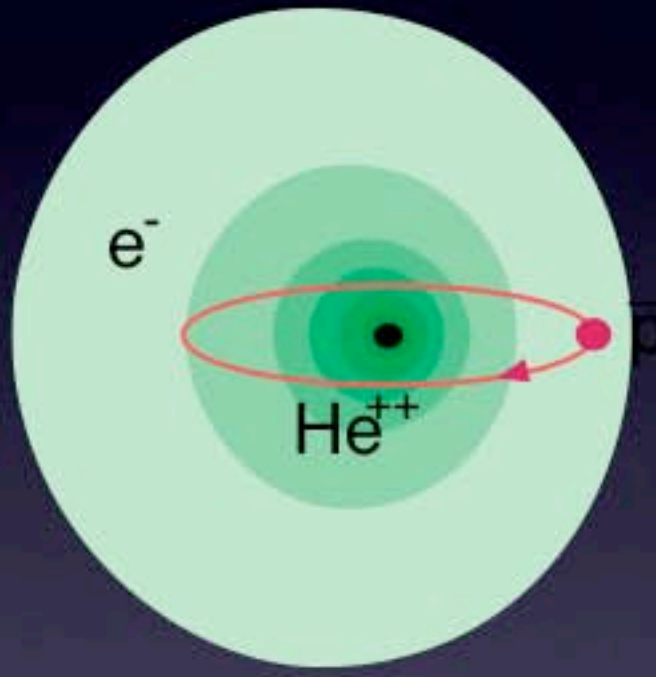
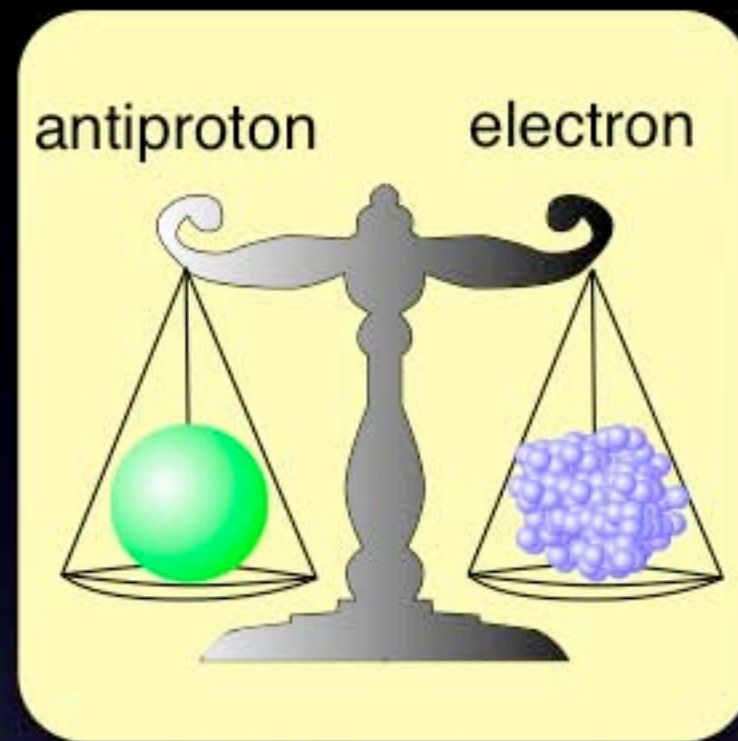


反陽子ヘリウム原子分光で 反陽子の重さを量る

早野 龍五

The University of Tokyo





CPT定理



陽子・電子質量比

Determination of the Antiproton-to-Electron Mass Ratio by Precision Laser Spectroscopy of $\bar{p}\text{He}^+$

M. Hori,^{1,2} A. Dax,² J. Eades,² K. Gomikawa,² R. S. Hayano,² N. Ono,² W. Pirkl,² E. Widmann,³ H. A. Torii,⁴
B. Juhász,^{5,3} D. Barna,^{6,2} and D. Horváth⁶

¹*CERN, CH-1211 Geneva 23, Switzerland*

²*Department of Physics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan*

³*Stefan Meyer Institut für Subatomare Physik, Boltzmannngasse 3, Vienna 1090, Austria*

⁴*Institute of Physics, University of Tokyo, Komaba, Meguro-ku, Tokyo 153-8902, Japan*

⁵*Institute of Nuclear Research of the Hungarian Academy of Sciences, H-4001 Debrecen, Hungary*

⁶*KFKI Research Institute for Particle and Nuclear Physics, H-1525 Budapest, Hungary*

(Received 10 April 2006; published 19 June 2006)

Antiprotonic helium and CPT invariance,
R.S. Hayano, M. Hori, D. Horvath, E. Widmann,
Reports on Progress in Physics 70, 1–74 (2007)

始

introduction
(&conclusion)

陽子の質量は電子質量の約1800倍
(理科教科書)

もうちょっと詳しく言うと
(理科年表)

陽子質量は電子質量の
1836.1526725 倍

1 2 3 4 5 6 7 8 9 10 11

電子との質量比

1 2 3 4 5 6 7 8 9 10

陽子 1836.1526725

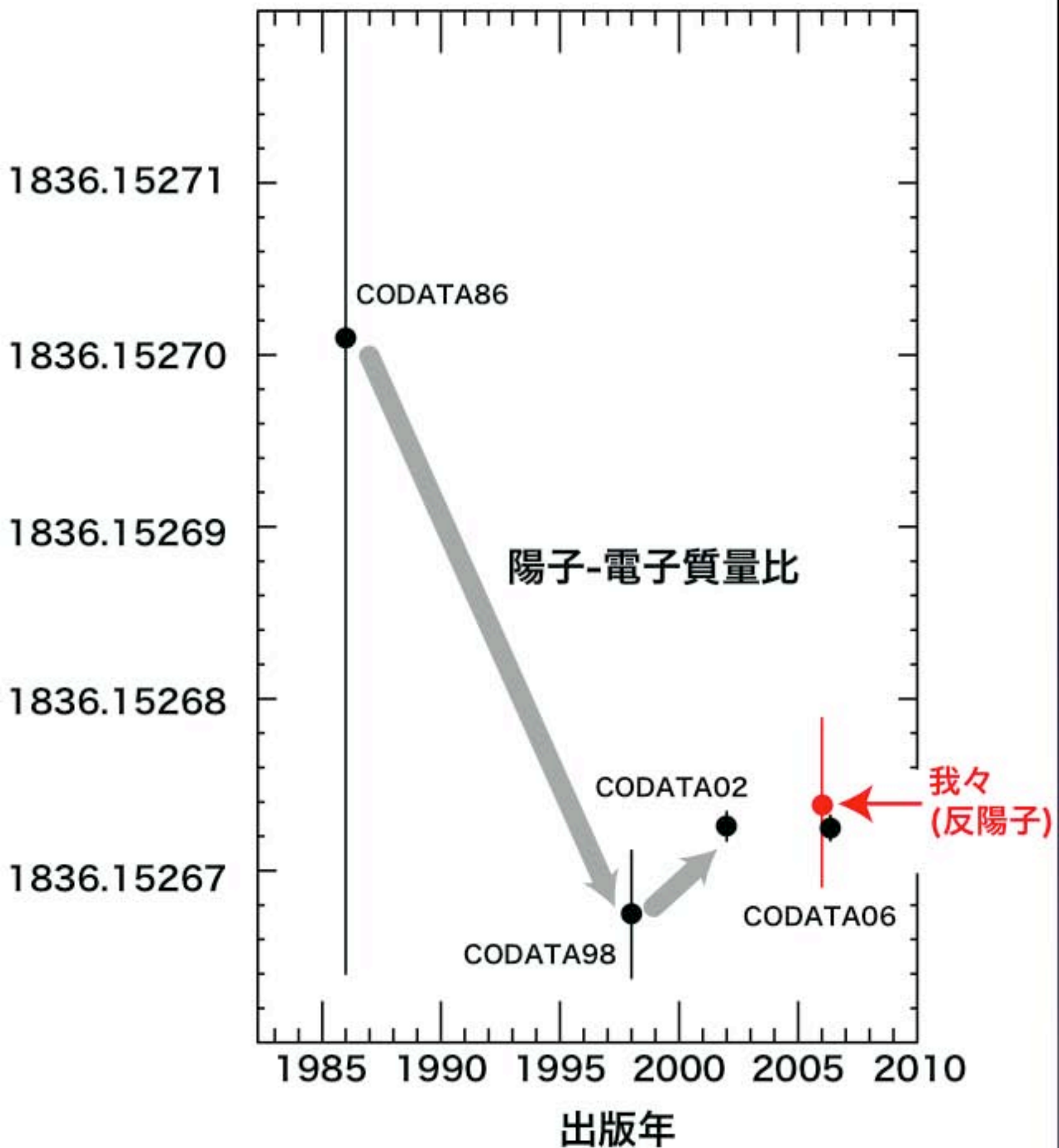
我々2006→ 反陽子 1836.152674

± 0.000005

9桁目までは完全に一致

10桁目も誤差の範囲で一致

グラフで示すと



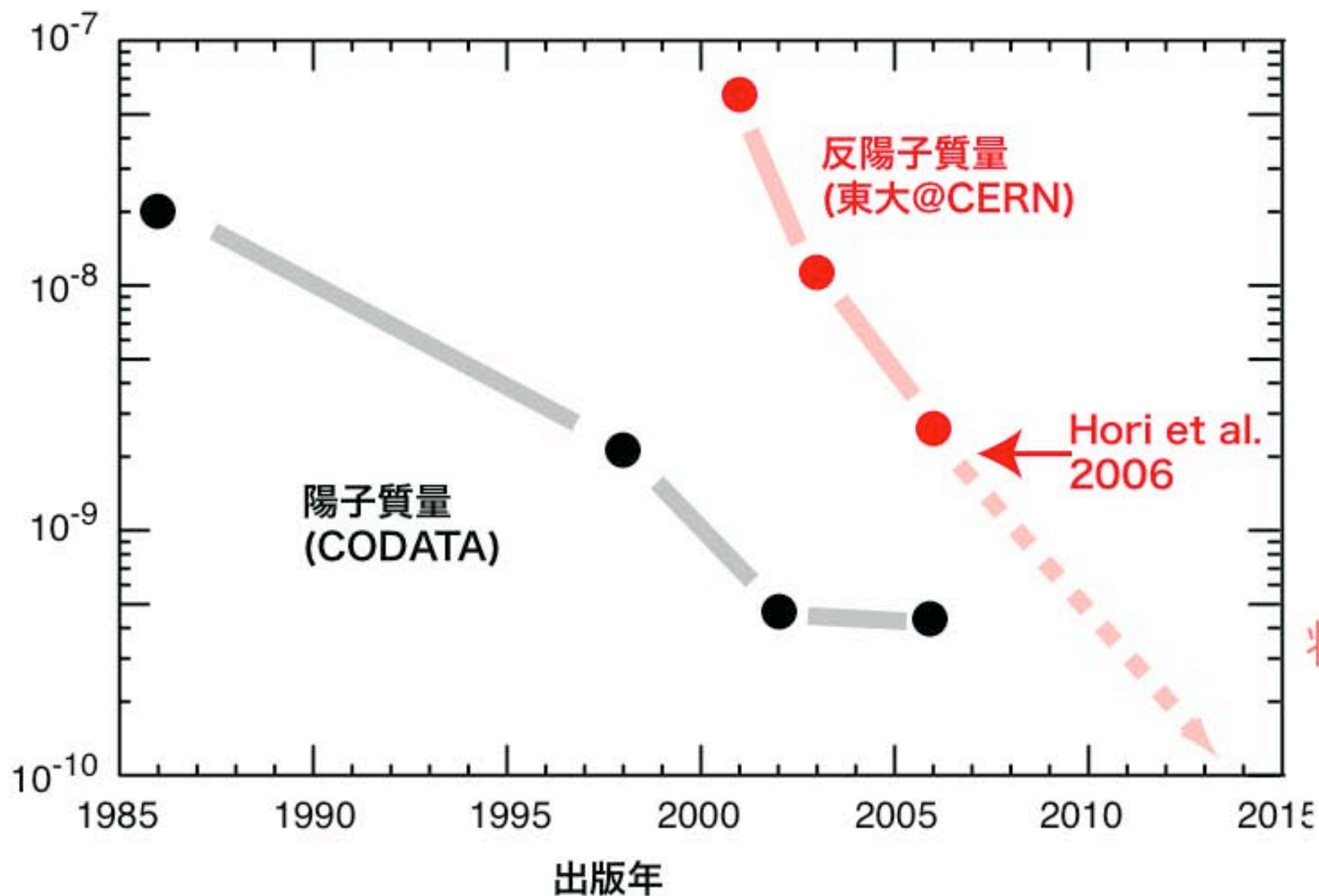
1. 物質・反物質対称性の精密検証

2. 基礎物理定数への貢献

近未来の可能性

“理科年表更新”

相对標準不確かさ



まだ
5倍負けているが
将来逆転...するぞ!

基礎物理定数の例
CODATA 2006より
(単位系に深く関係している)

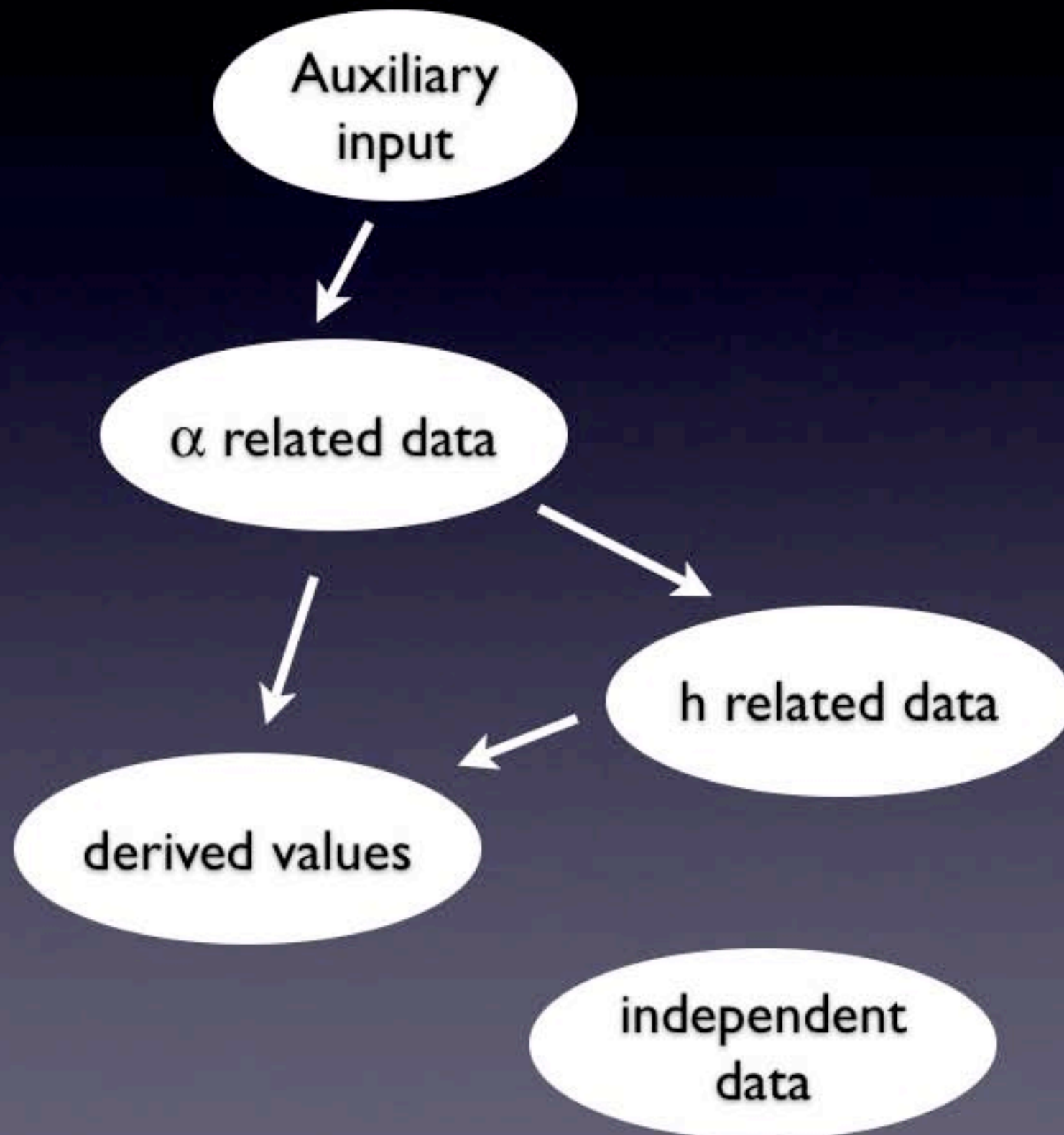
ppb=10億分の1

物理定数	数値 (下線の桁に不確定性がある)	単位	精度	
光速	299 792 458	m s ⁻¹	定義値	
万有引力定数	6.674 <u>3</u>	x 10 ⁻¹¹ m ³ kg ⁻¹ s ⁻²	5桁	100000 ppb
アボガドロ数	6.022 141 <u>8</u>	x 10 ²³ mol ⁻¹	8桁	50 ppb
プランク定数	6.626 068 <u>9</u>	x 10 ⁻³⁴ J s	8桁	50 ppb
陽子の質量	1.672 621 <u>64</u>	x 10 ⁻²⁷ kg	9桁	50 ppb
電子の電荷	1.602 176 <u>49</u>	x 10 ⁻¹⁹ C	9桁	25 ppb
陽子・電子質量比	1836.152 672 <u>5</u>		11桁	0.43 ppb
リュードベリ定数	10 973 731.568 <u>52</u>	m ⁻¹	13桁	0.0066 ppb

T.W. Hänsch et al., hydrogen spectroscopy
using frequency comb, Nobel Prize 2005

CODATA adjustment flowchart

from S.G. Karshenboim



Auxiliary data = the most accurate data which are to be evaluated prior to the adjustment, R_∞ , $\underline{m_e/m_p}$, ...

Arrows are equations

Derived: m_p [kg], m_e [MeV/c²], etc...

ちなみに

m_p/m_e はどうやって量っているか

一様磁場

電子スピン回転周波数 $\propto 1/(\text{電子質量})$



$^{12}\text{C}^{5+}$ サイクロトロン周波数
 $\propto 1/(\text{C原子核質量})$

二つの周波数の比 \rightarrow 量子電磁力学補正 \rightarrow
C原子核と電子の質量比 \rightarrow 陽子・電子質量比

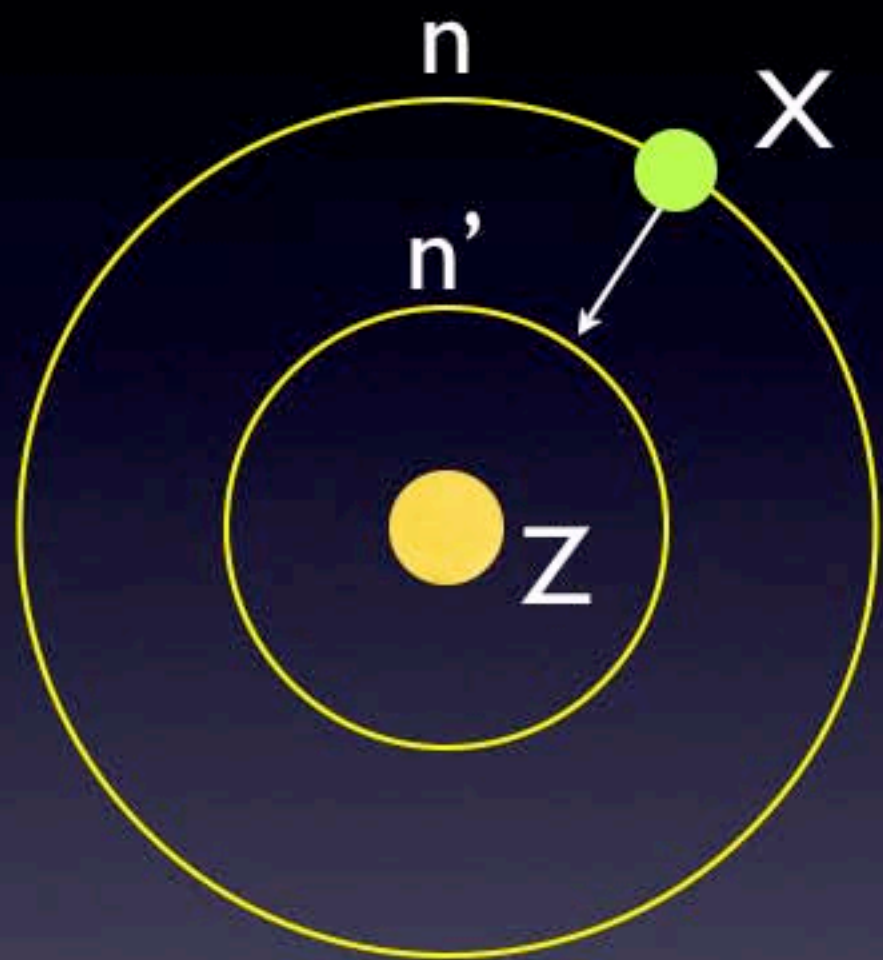
陽子のようにありふれたものですら、質量を10桁以上の精度で決めるのは容易でない

反陽子のように自然界に存在しないものの質量をどうやって測定するの？

素粒子の質量 (PDG)

Particle	How?	eV/c^2 での精度 ppm	u での精度ppm
e^-	Penning trap	0.078	0.00044
p	Penning trap	0.085	0.00013
μ^+	μ^+e^- laser, HFS	0.085	0.027
π^-	X-ray	2.5	-
K^-	X-ray	32.4	-

Exotic atomの脱励起



$$\Delta\nu_{n,\ell \rightarrow n',\ell'} = Rc \frac{m_X^*}{m_e} Z^2 \left(\frac{1}{n'^2} - \frac{1}{n^2} \right)$$

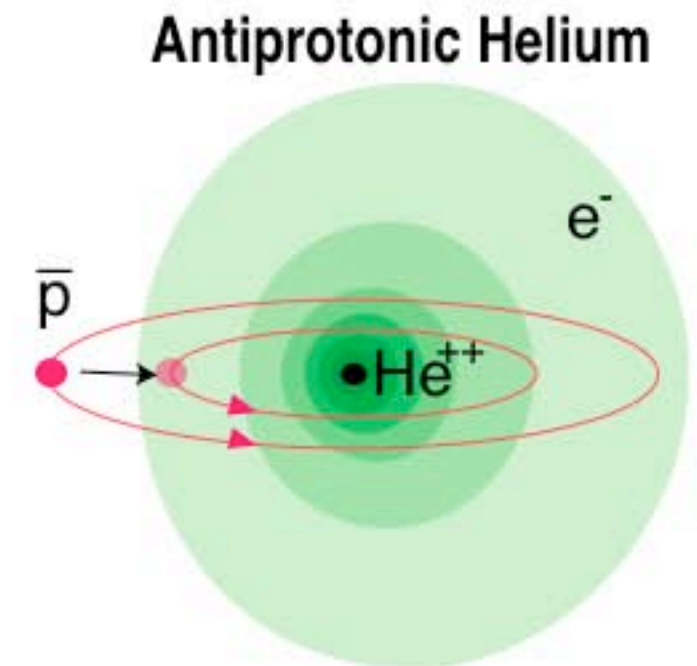
Laser resonance to change \bar{p} orbit → \bar{p} - e mass ratio

For antiprotonic helium ($\bar{p} + e^- + \alpha$),

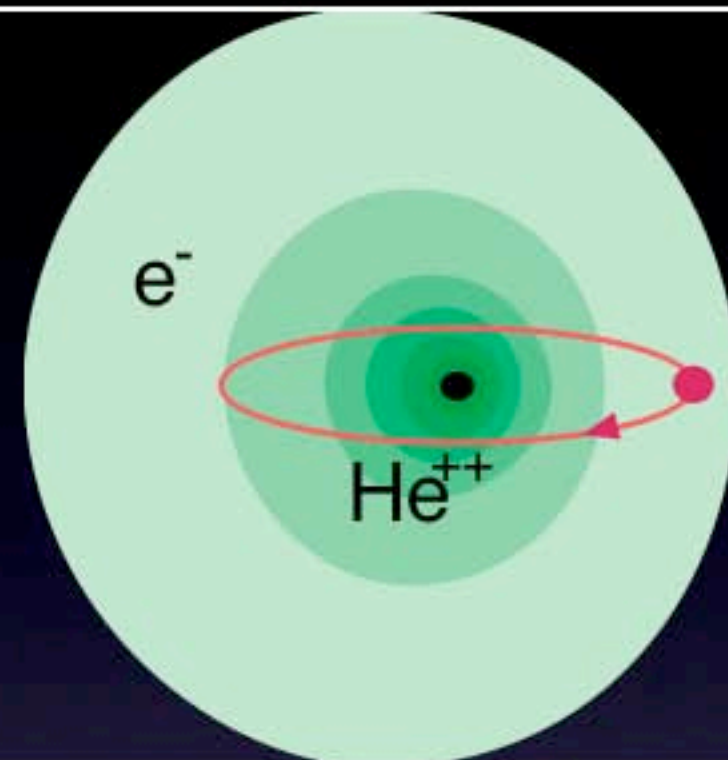
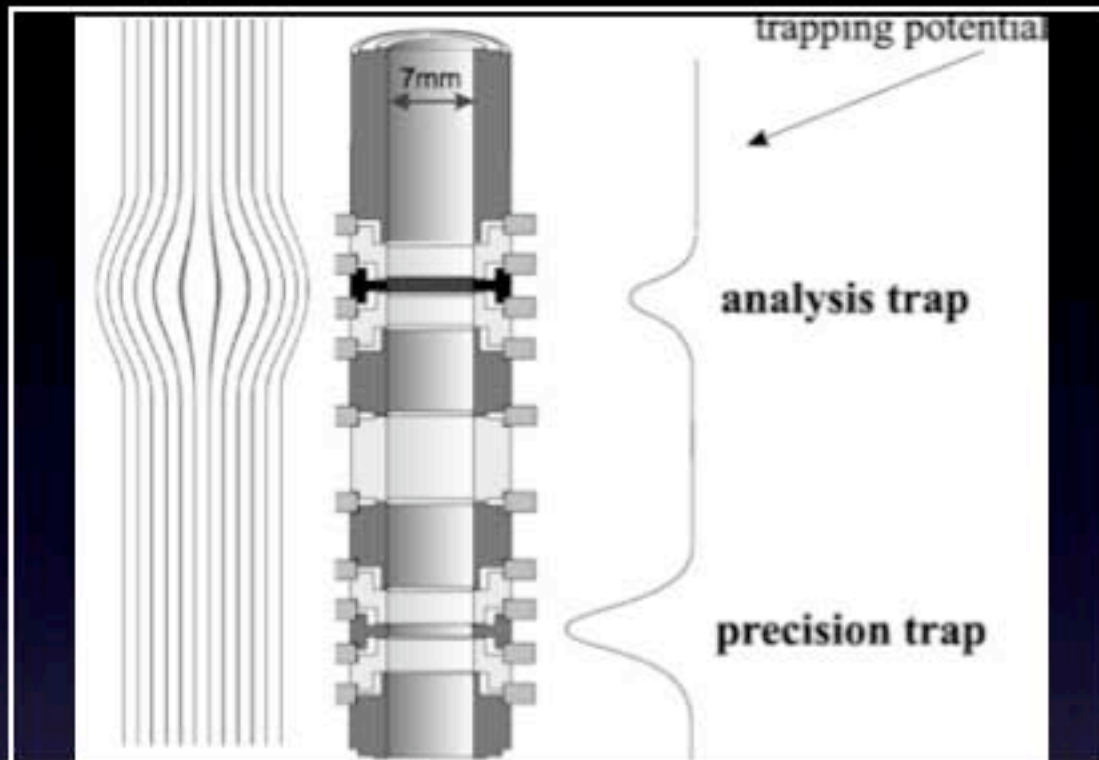
$$\nu(n, n') = Rc \frac{M_{\bar{p}}^*}{m_e} Z_{\text{eff}}^2 \left(\frac{1}{n^2} - \frac{1}{n'^2} \right)$$

Would be exact for $\bar{p}\text{He}$ ion
approximate for the 3-body system

Z_{eff}^2 : helium charge, shielded by
electron (calculated by theory)



- +relativistic correction
- +QED correction
- + hyperfine

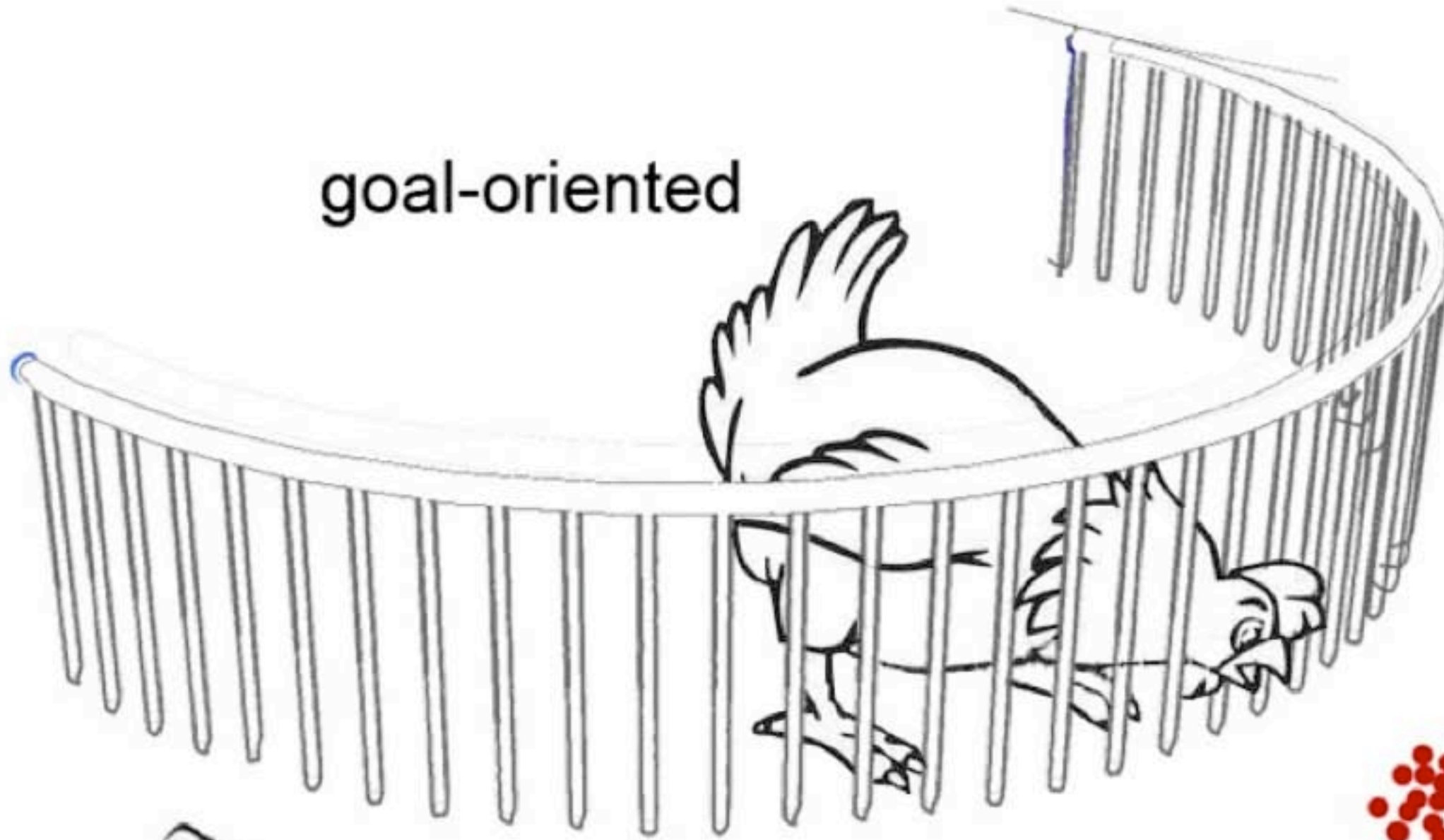


Penning trap:
man-made trap

Antiprotonic helium:
naturally-occurring
trap

しかし我々は最初から
 m_p/m_e 測定を目指したのではない

goal-oriented



curiosity-driven

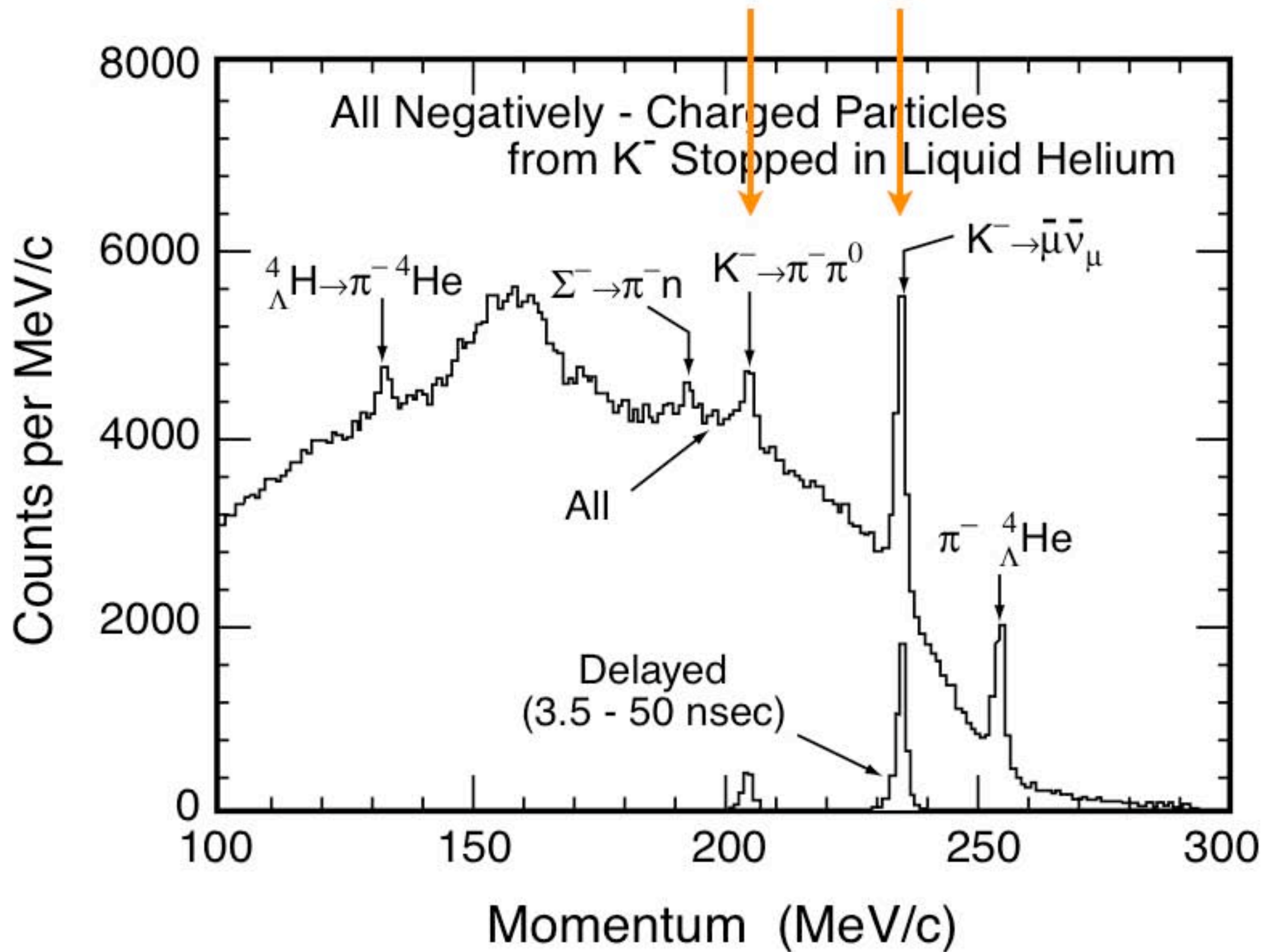


歷史

Historical

ハイパー核研究 液体ヘリウムに止めたK-

Kaon weak decay peaks

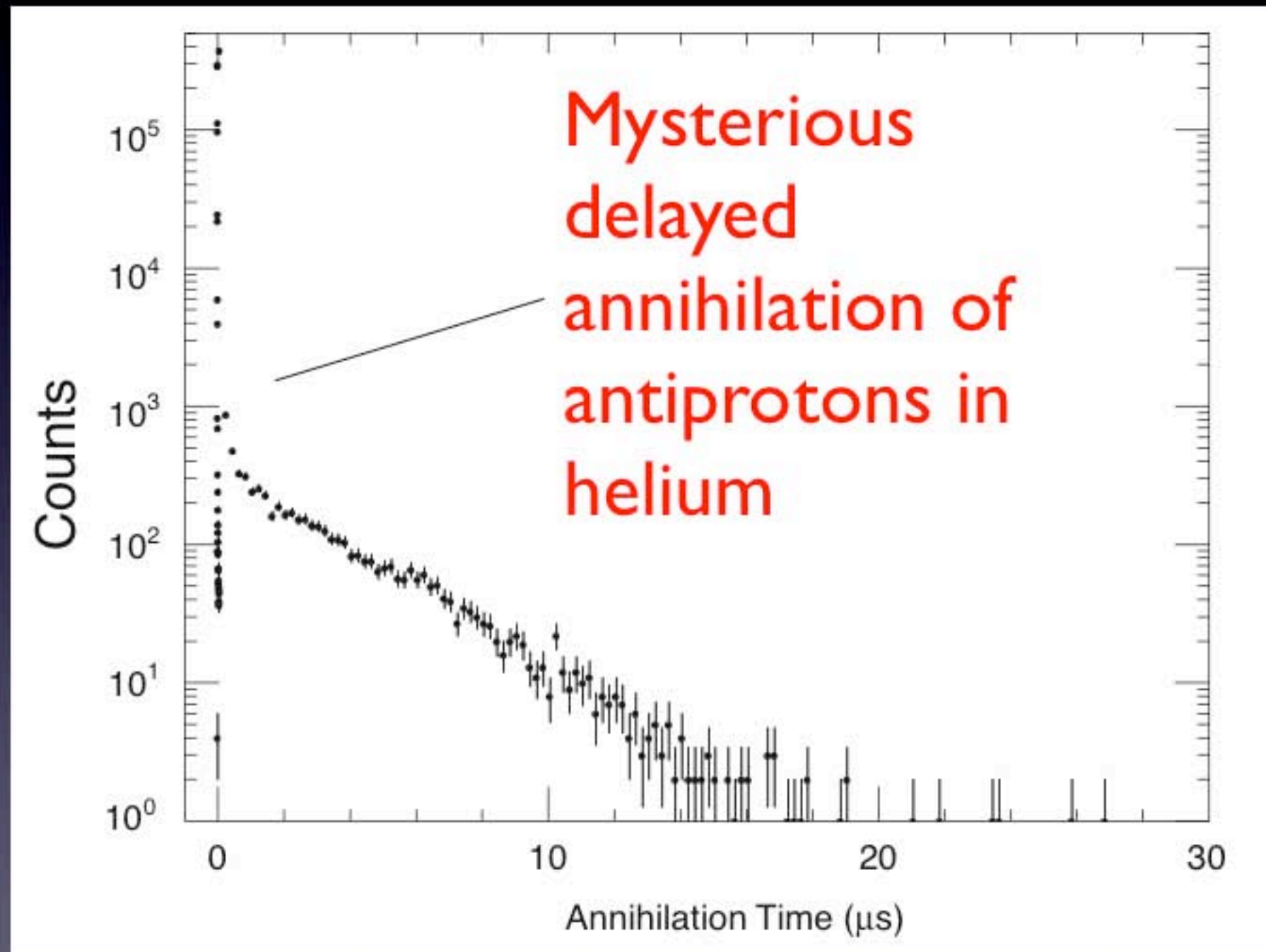


how can K^- weak decay (lifetime 12ns) be visible when cascade & nuclear capture can be as fast as <1 ns?

これは異常だ

反陽子でも異常が見えるか？

Serendipitous discovery of naturally-occurring \bar{p} trap

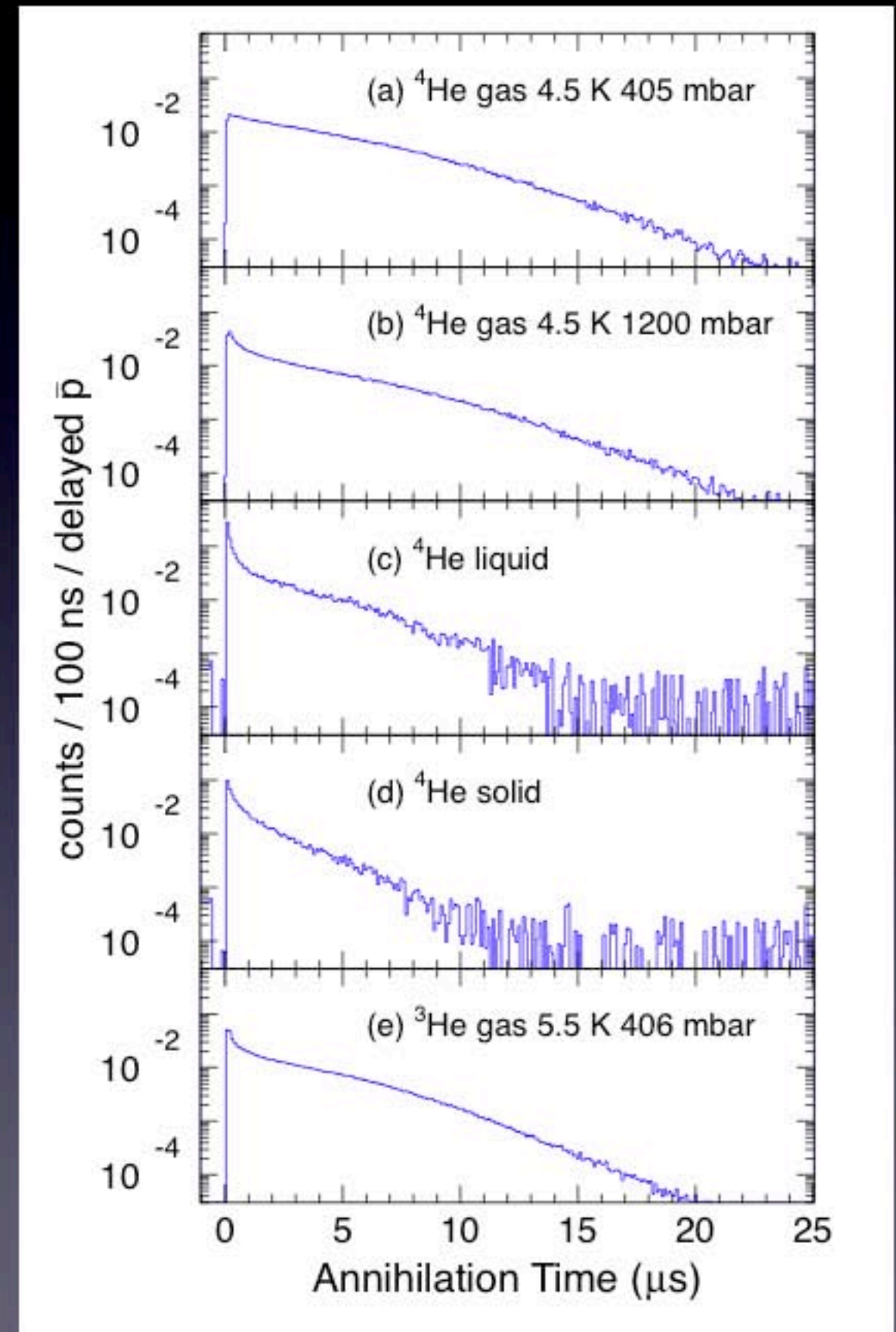


Not just in liquid

Measurements
continued at CERN
LEAR

Established
antiproton longevity
in gas, liquid, solid
helium-3 & helium-4

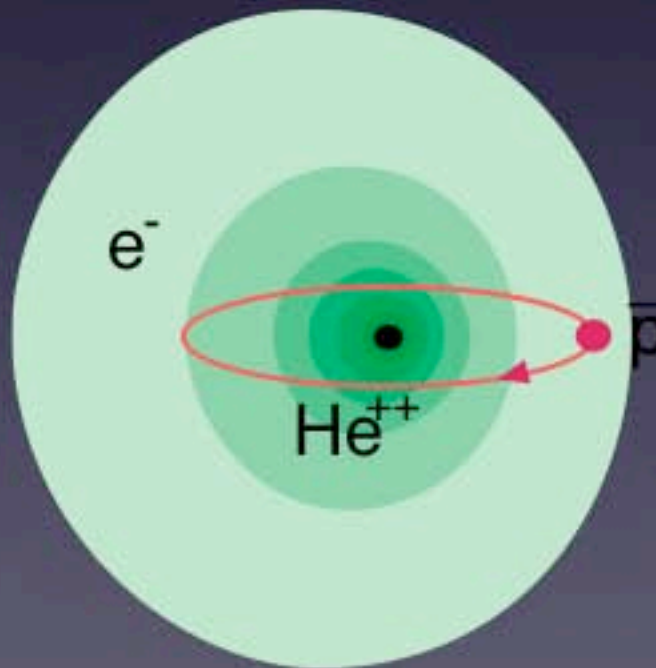
T. Yamazaki et al, 特別推進研究
@LEAR 1992-1996



antiprotonic helium

a naturally-occurring
antiproton trap

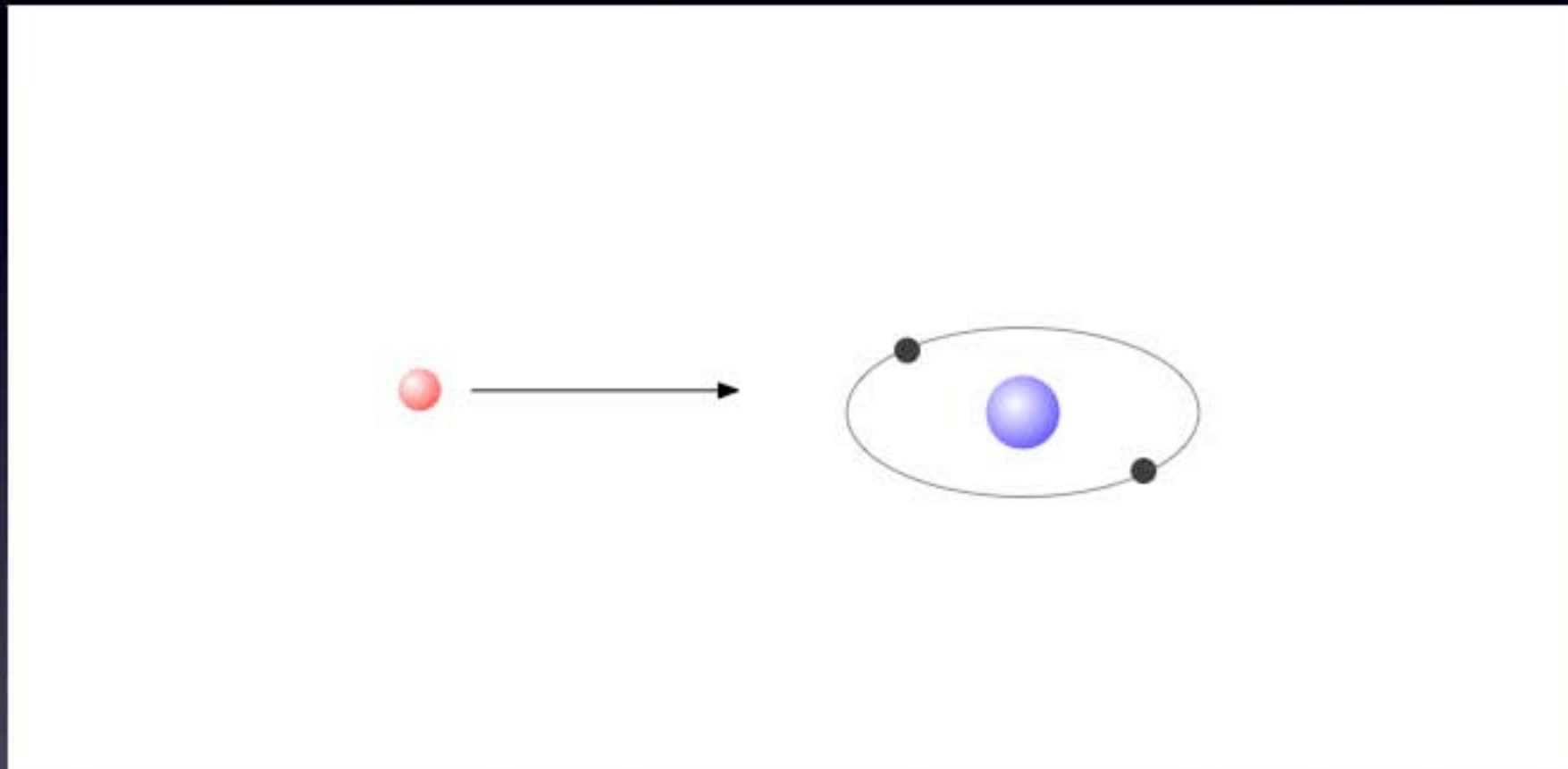
electron is in $\sim 1s$
(slightly polarized to
the opposite side of \bar{p})

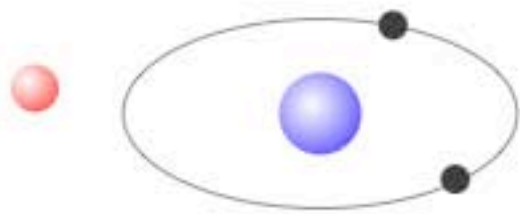


antiproton is in a
highly excited
($n \sim 40$) orbit

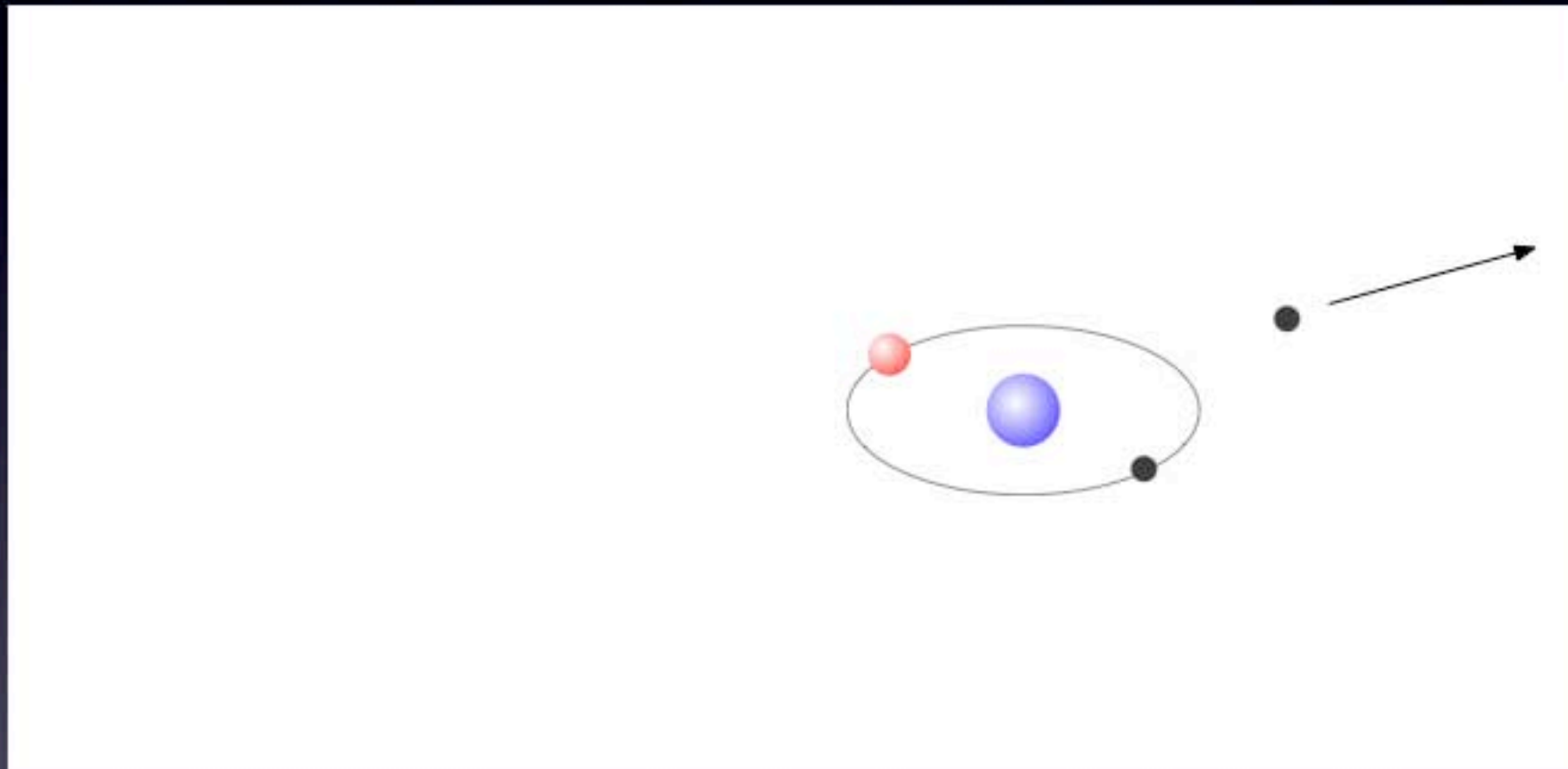
Easy production
Large yield
Long lifetime

Stop antiprotons in a low-temperature, dilute helium gas



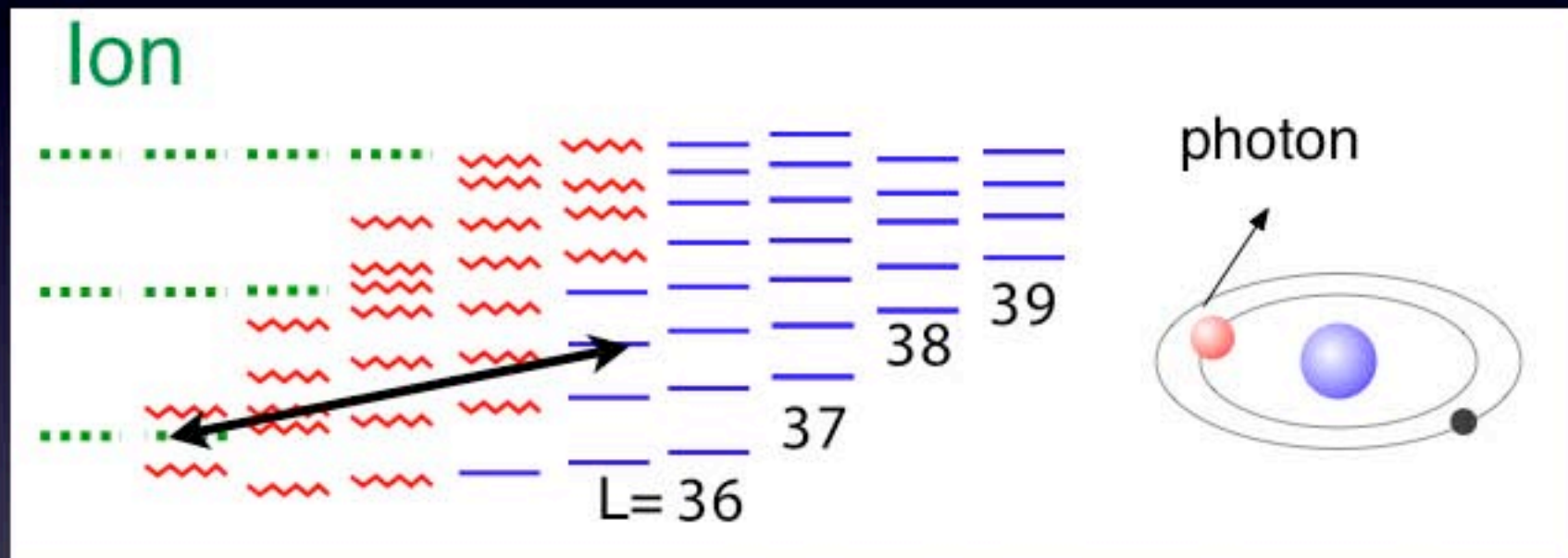


One of the two electrons of He, replaced by \bar{p}



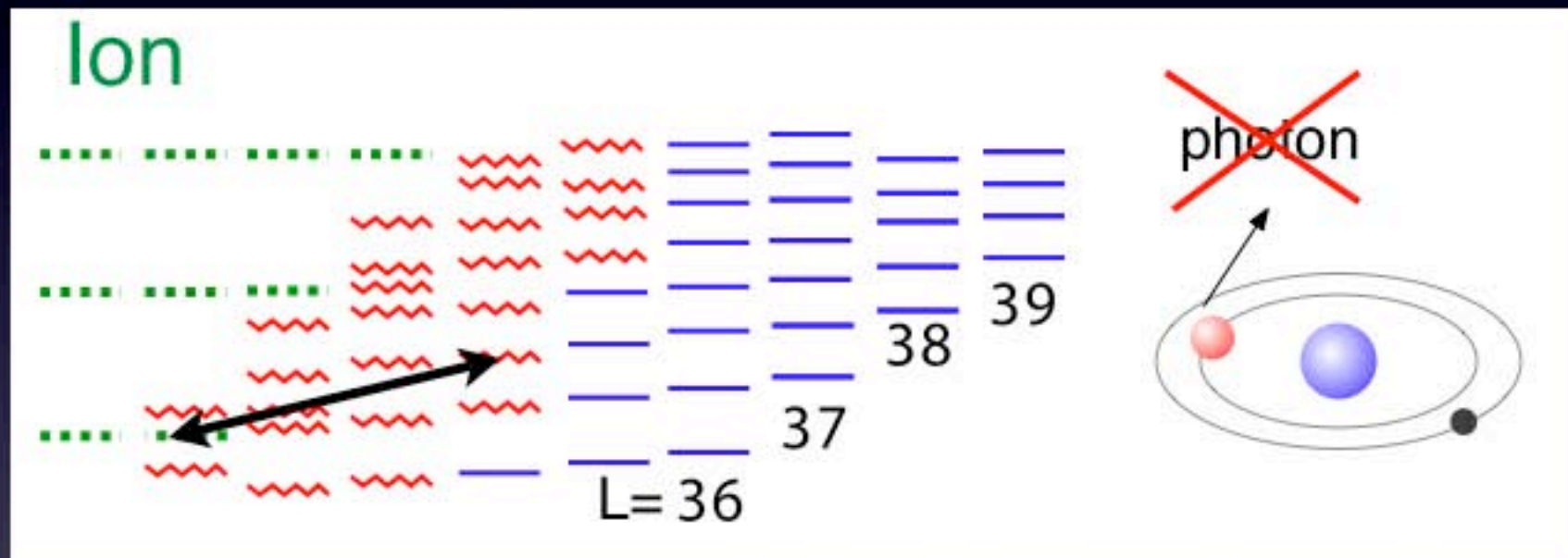
3% of stopped antiprotons form $\bar{p}\text{He}$, lifetime $> 3 \mu\text{s}$

Mechanism of longevity



If Auger is hindered (high multipolarity ΔL)
slow radiative deexcitation ($\sim \mu\text{s} / \text{step}$)

Mechanism of longevity

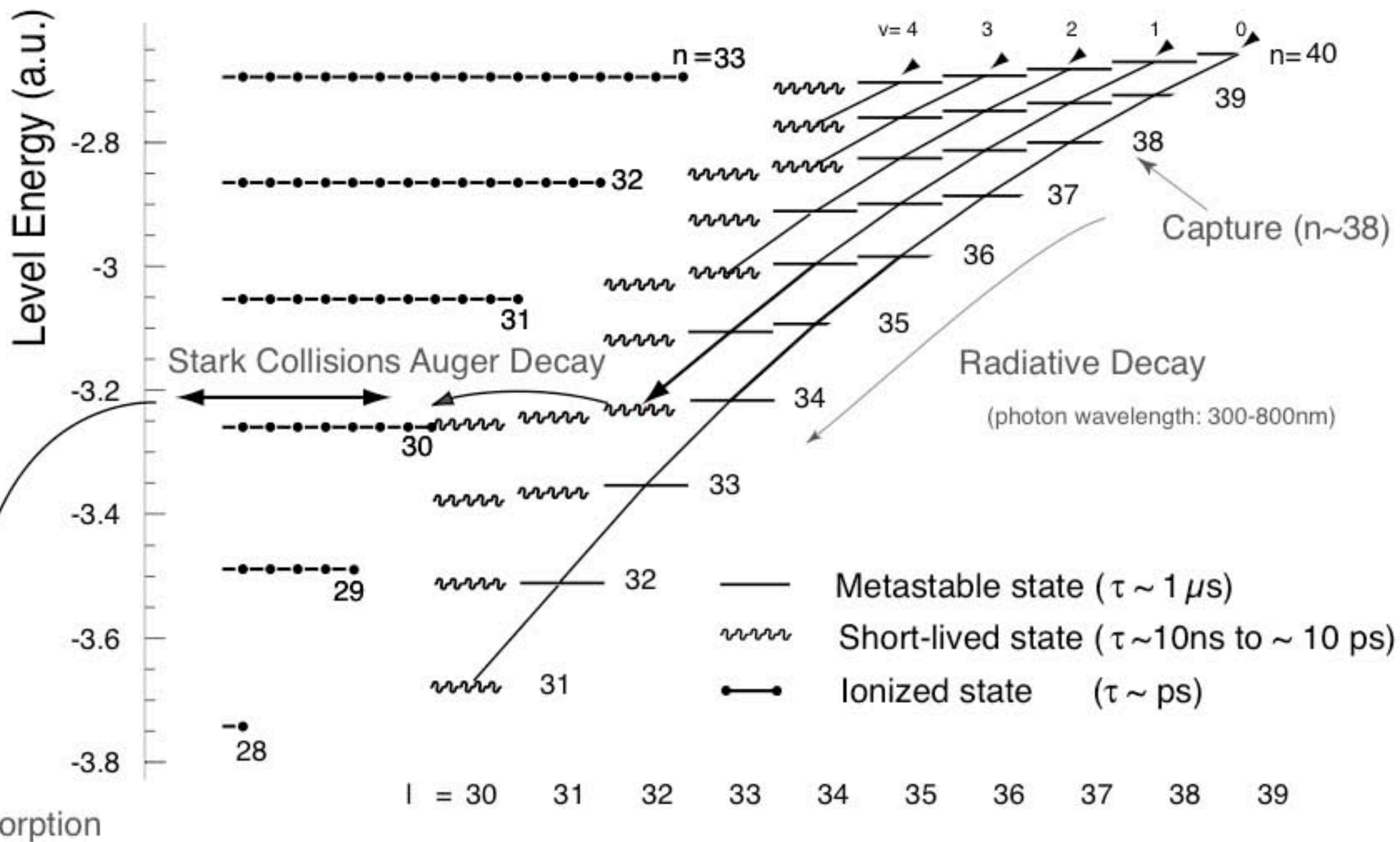
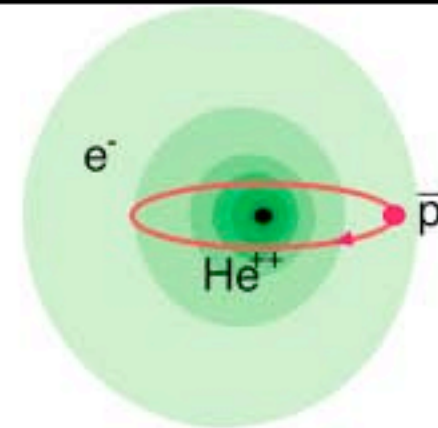
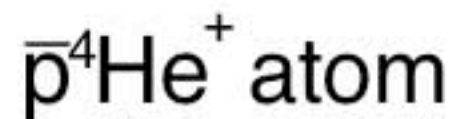
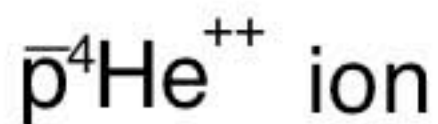
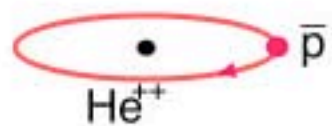


$$\Delta L=3, \Gamma_{\text{auger}} > \Gamma_{\text{radiative}}$$

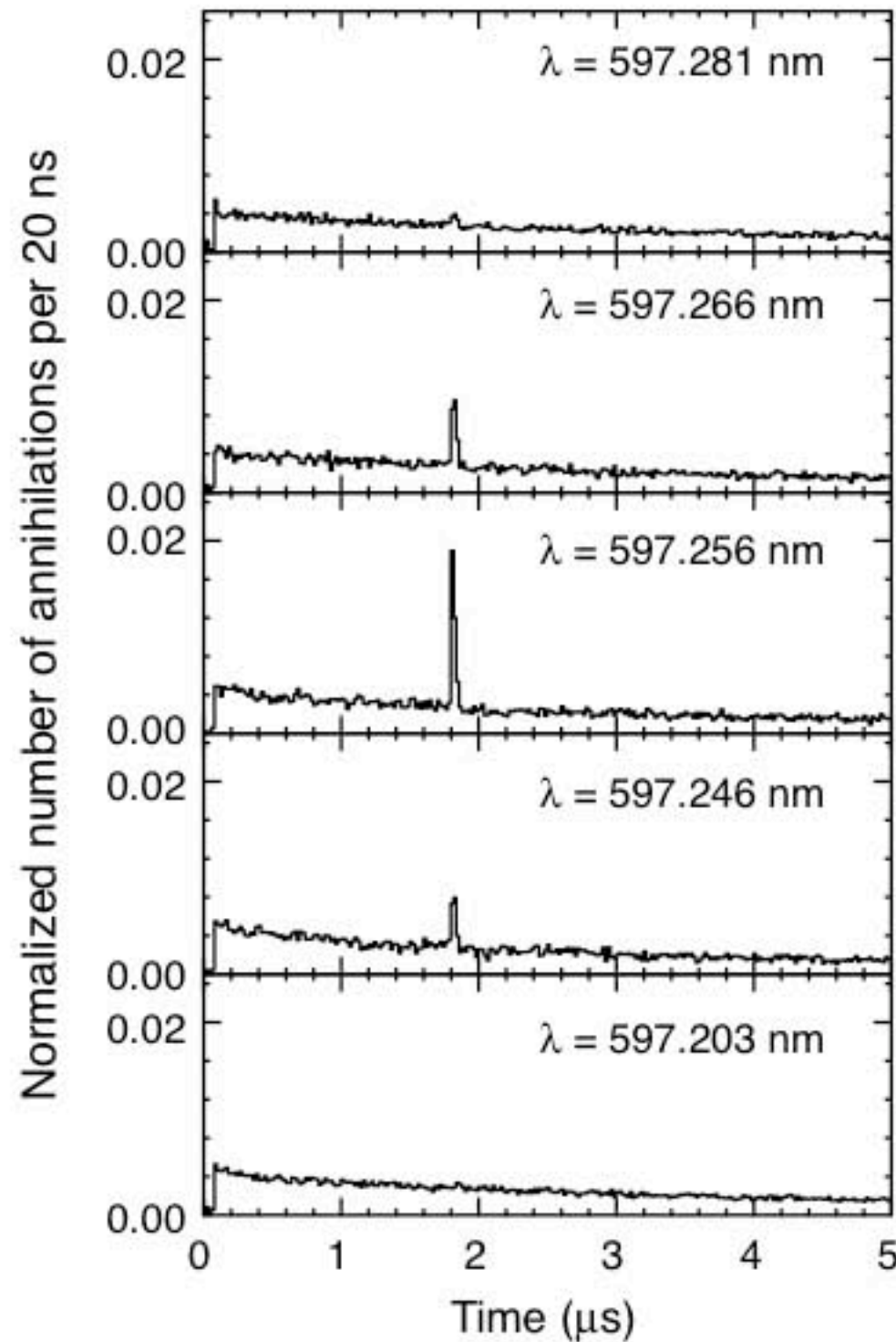
If Auger is fast, the system is short lived

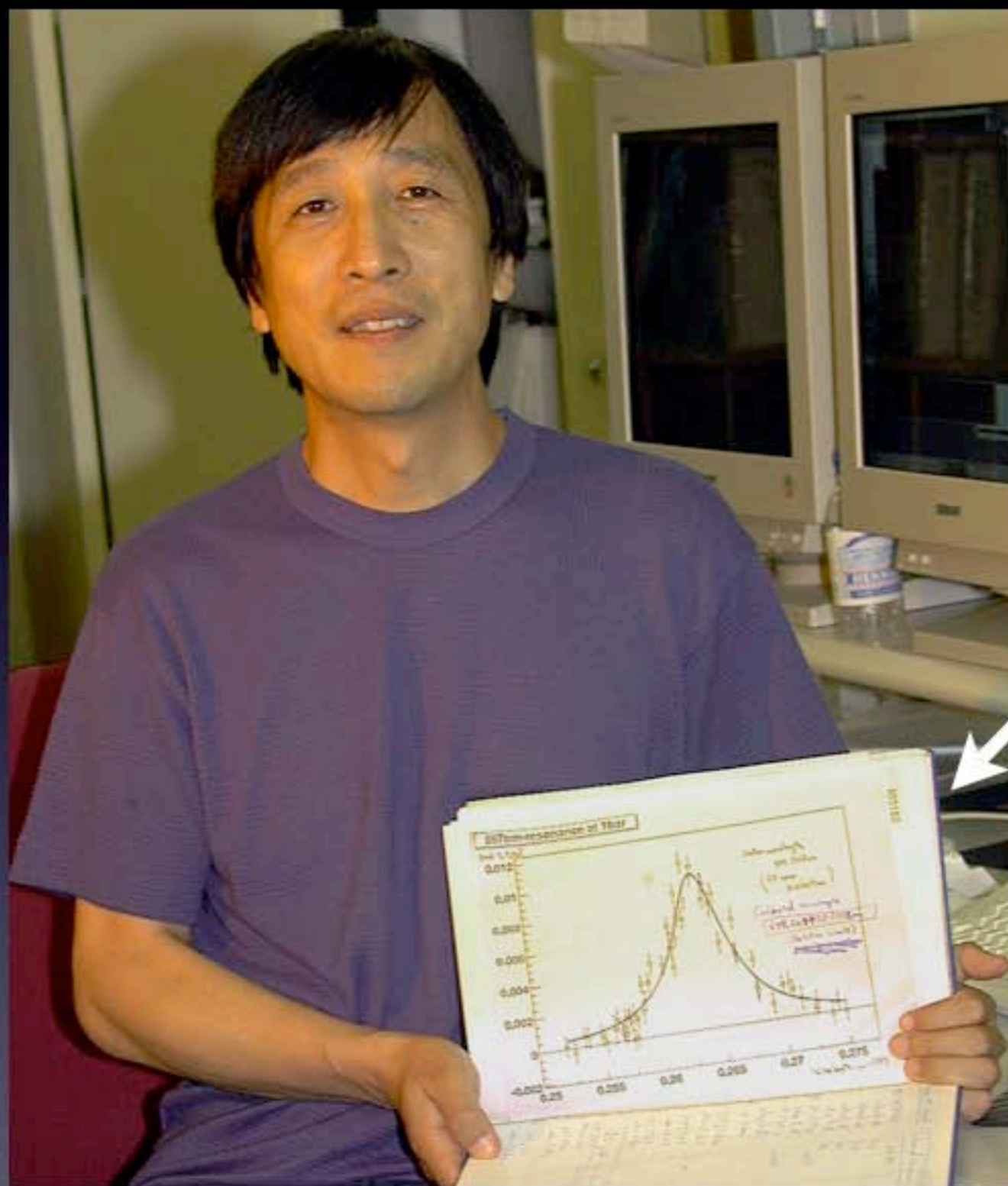
分光原理

laser-induced
annihilation



An example, $(n,l)=(39,35) \rightarrow (38,34)$





レーザー共鳴を示す
グラフ
(共鳴強度 vs 周波数)



Photo CERN

remember:

volume $> \text{cm}^3$

auger lifetime $< 10 \text{ ns}$



laser power density $\sim \text{MW}/\text{cm}^2$

パルスレーザー必須

also remember:

typical transition 10^{15} Hz



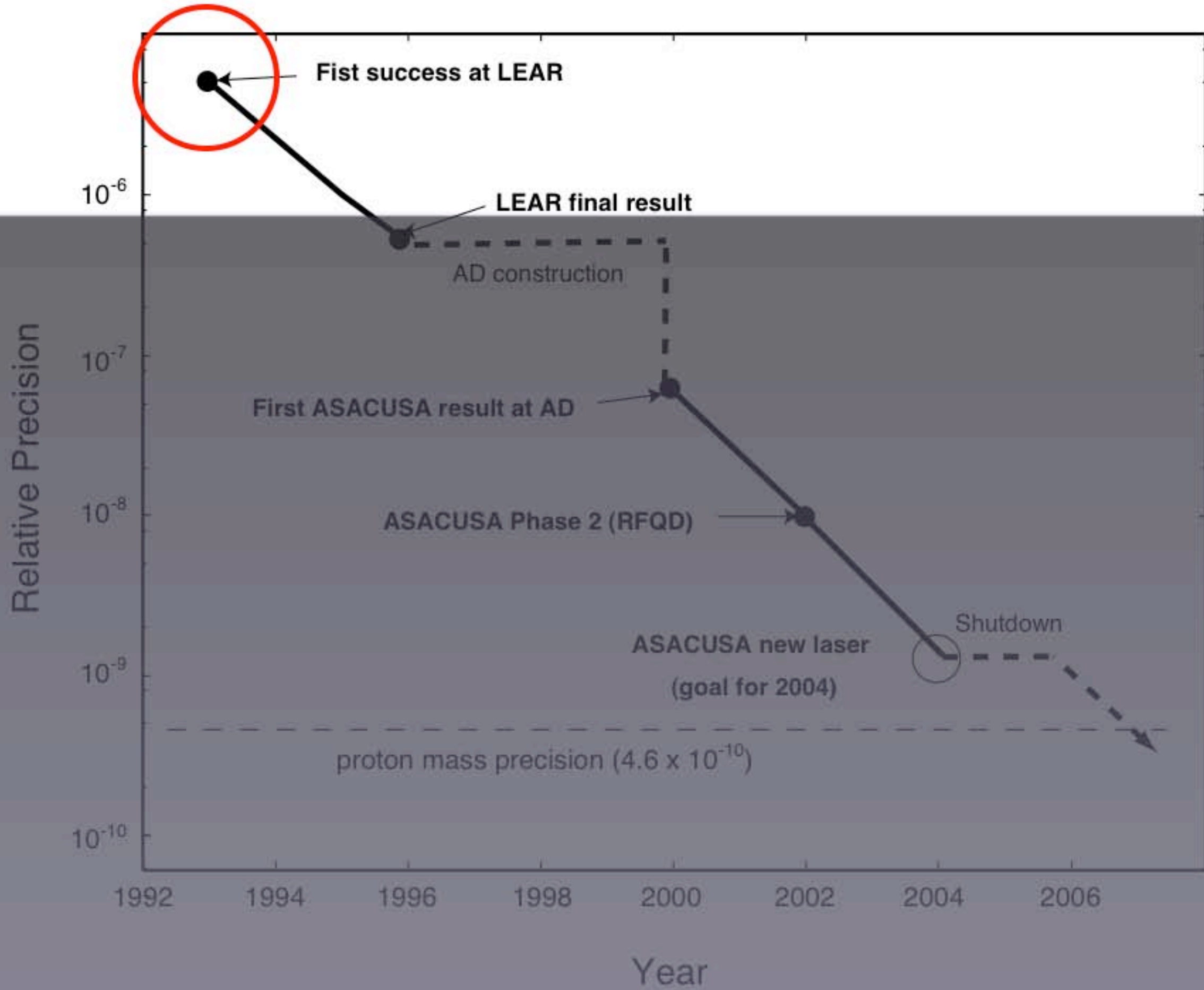
measurement precision of 1 MHz

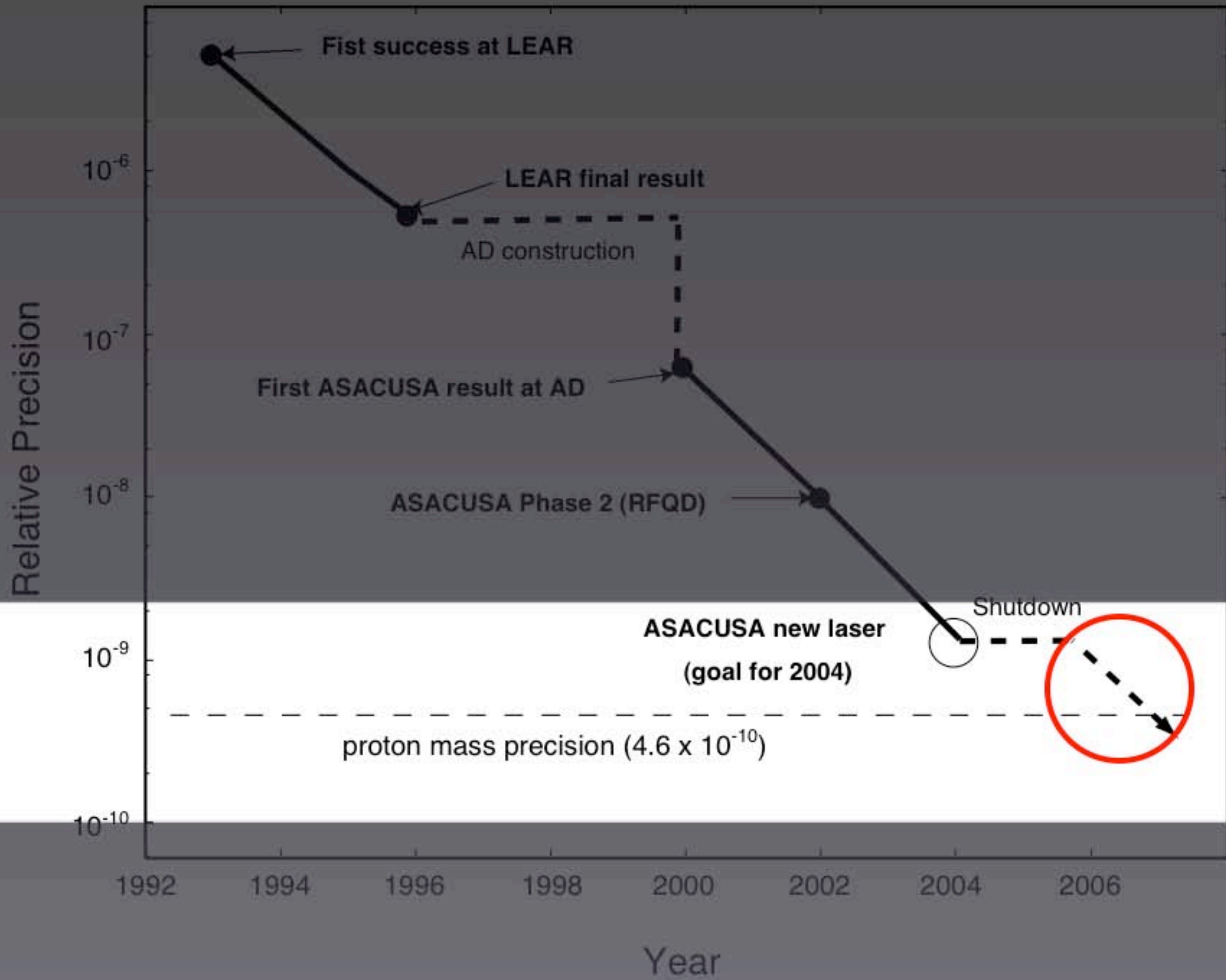


relative uncertainty 10^{-9} (ppb)

精度

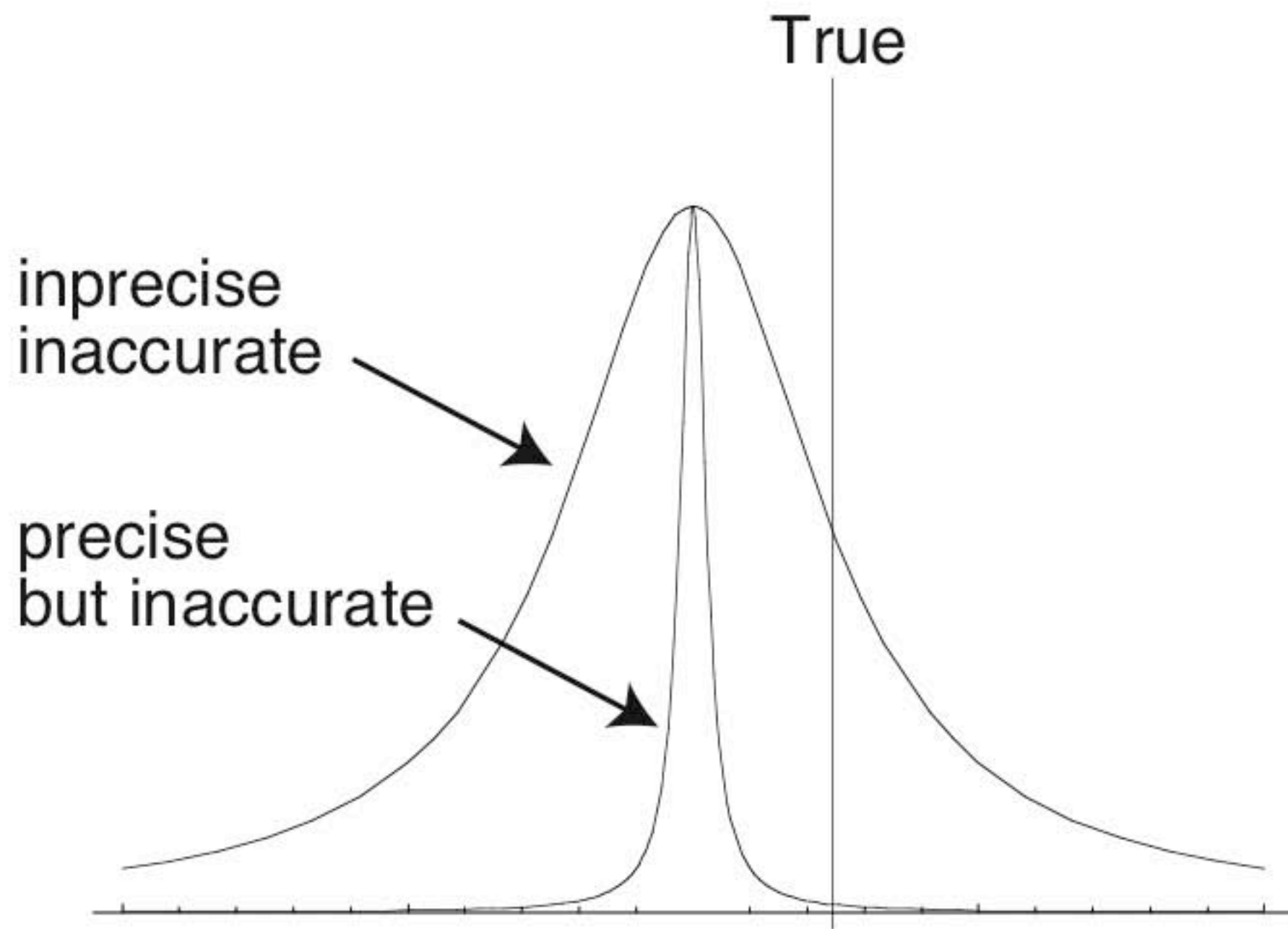
reducing uncertainty





uncertaintyはどうやれば減るか

統計	ideally $\sigma = \frac{\text{line width}}{\sqrt{N}}$
<u>線幅</u>	
systematics	
systematics	
systematics	
systematics	
...	



幅の要因

自然幅	15MHz - 150kHz
Fourier幅	パルスレーザー パルス長
衝突	RFQD
ドップラー幅	2光子分光
レーザー単色性	パルスレーザー →CWレーザー

シフトの要因

衝突	RFQD
チャープ	~2MHz, パルスレーザー不可避
周波数較正	光周波数comb
AC Stark shift	\propto Power
(理論)	~MHz?

反陽子減速器

CERN AD

(Antiproton Decelerator)

and ASACUSA RFQD

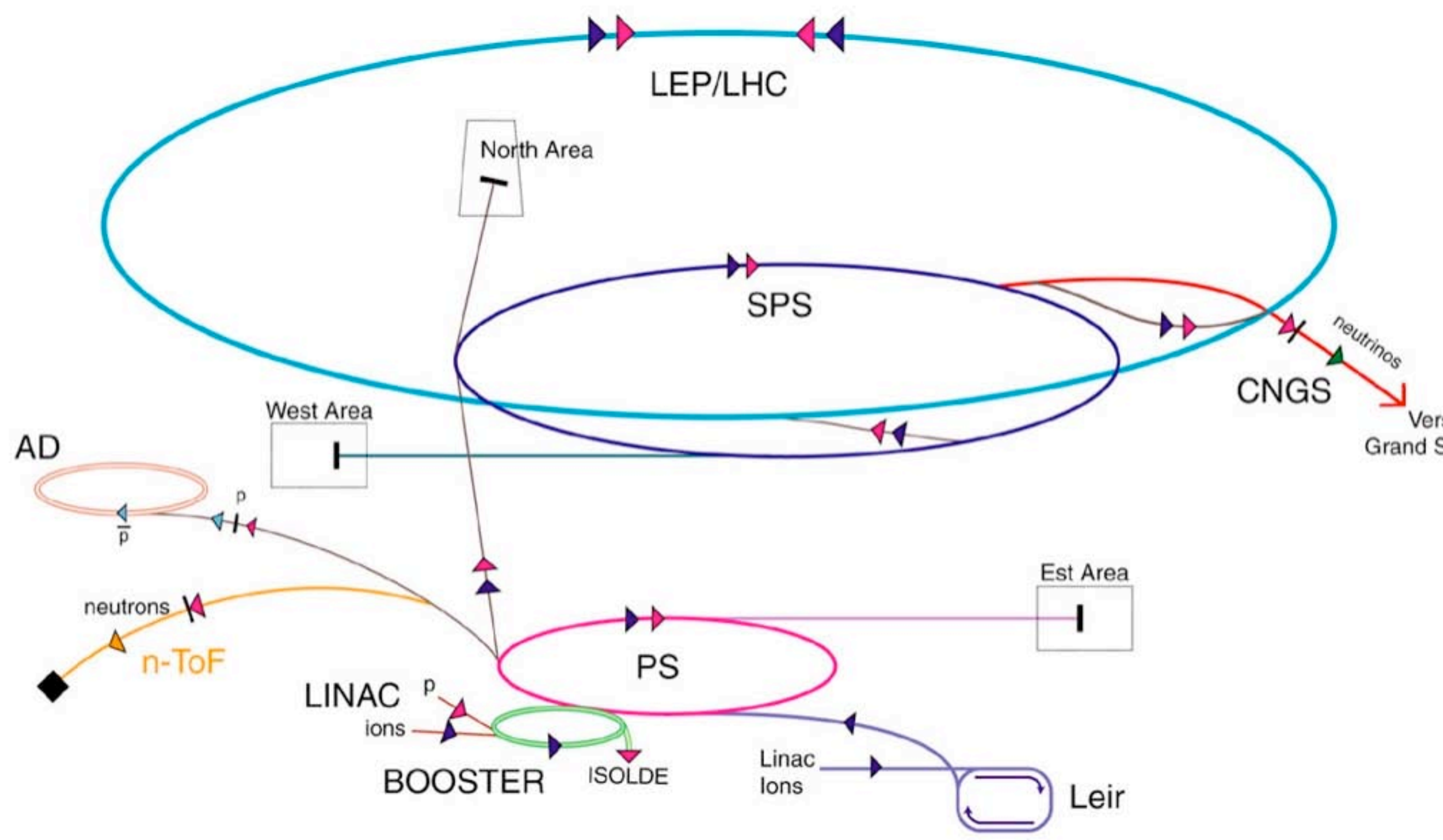
(radio-frequency quadrupole decelerator)

ASACUSA



atomic spectroscopy
and
collisions using
slow antiprotons

Accelerator chain of CERN (operating or approved projects)



- | | | | |
|------------|------------------------------|------------------------------|---------------------------------|
| p (proton) | \bar{p} (antiproton) | AD Antiproton Decelerator | LHC Large Hadron Collider |
| ion | proton/antiproton conversion | PS Proton Synchrotron | n-ToF Neutrons Time of Flight |
| neutrons | neutrinos | SPS Super Proton Synchrotron | CNGS Cern Neutrinos Grand Sasso |



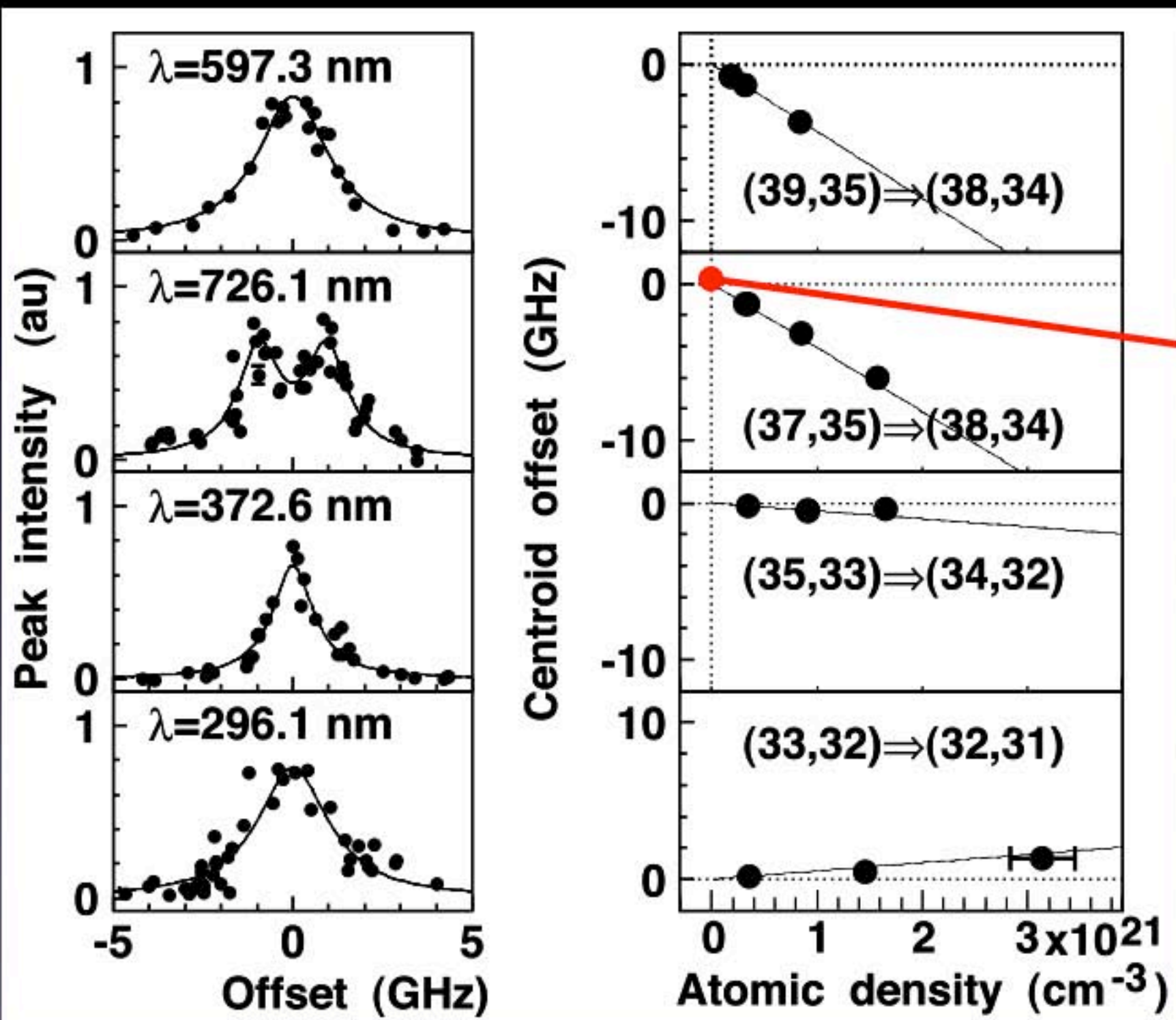
3×10^7 antiprotons @ 5 MeV
100ns pulse
every ~ 90 seconds

初

the first result @ AD

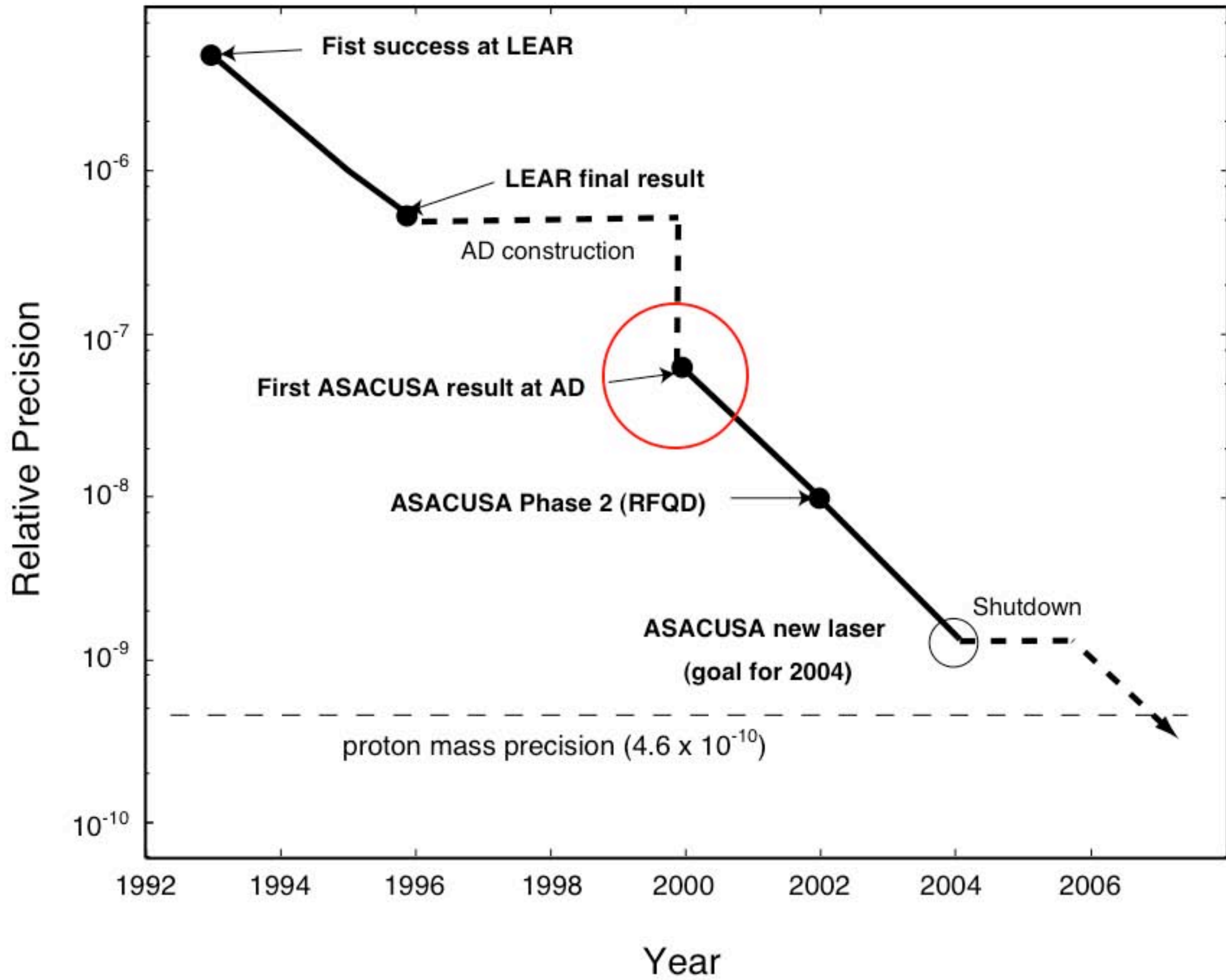
M. Hori et al., Phys. Rev. Lett. 87, 093401(2001).

Collisional frequency shift correction



Antiprotons stopped in a dense (~ 1 bar, ~ 5 K) helium gas target

zero-density extrapolation needed



衝突

reducing collision

M. Hori et al., Phys. Rev. Lett. 91, 123401(2003).

幅の要因

自然幅	15MHz - 150kHz
Fourier幅	パルスレーザー パルス長
衝突	RFQD
ドップラー幅	2光子分光
レーザー単色性	パルスレーザー →CWレーザー

シフトの要因

衝突	RFQD
チャープ	~2MHz, パルスレーザー不可避
周波数較正	光周波数comb
AC Stark	\propto Power
(理論)	~MHz?

Photo CERN

small (a few MHz)
collisional shift and width
(which we correct)

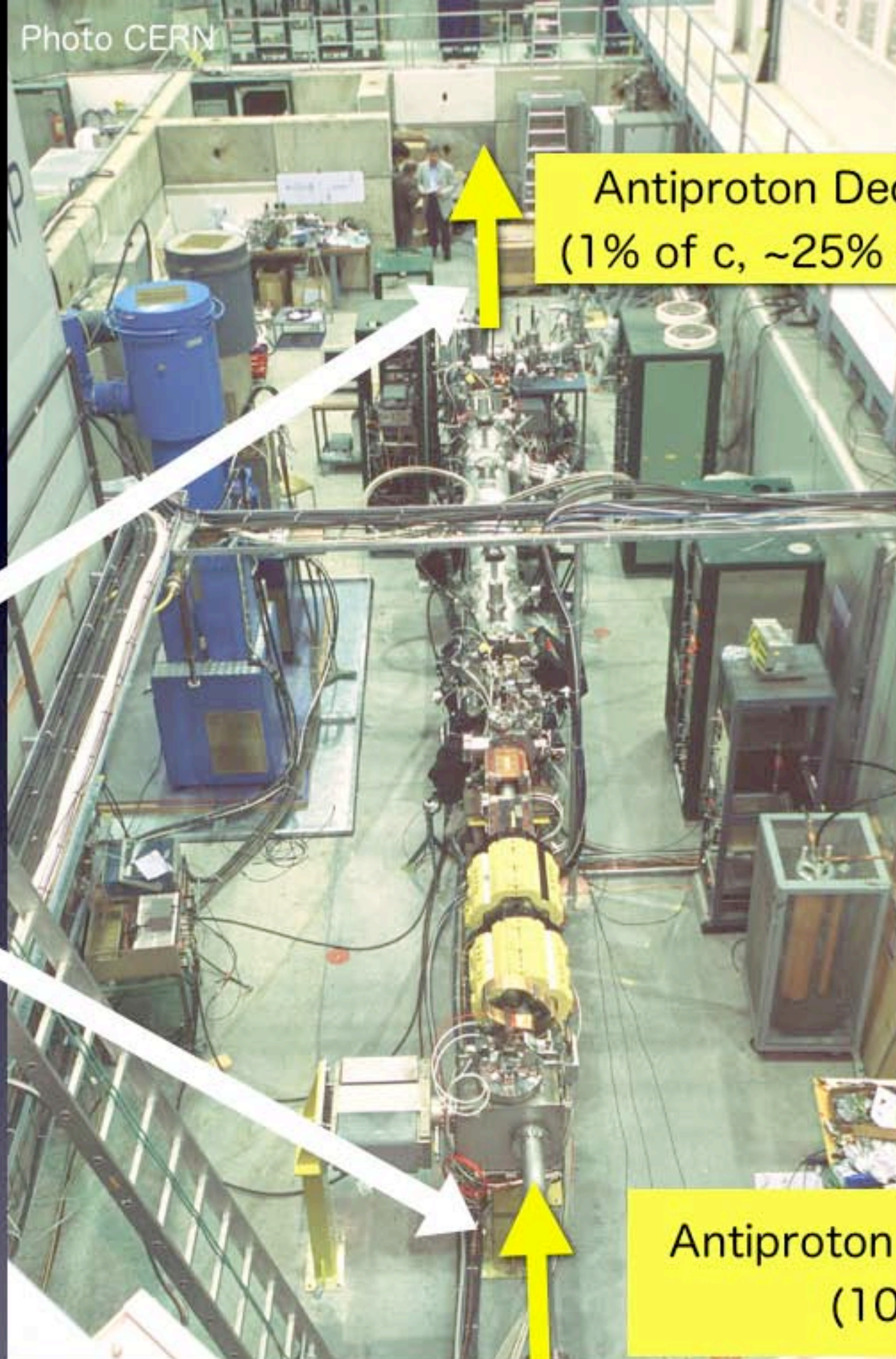
Typical target
density

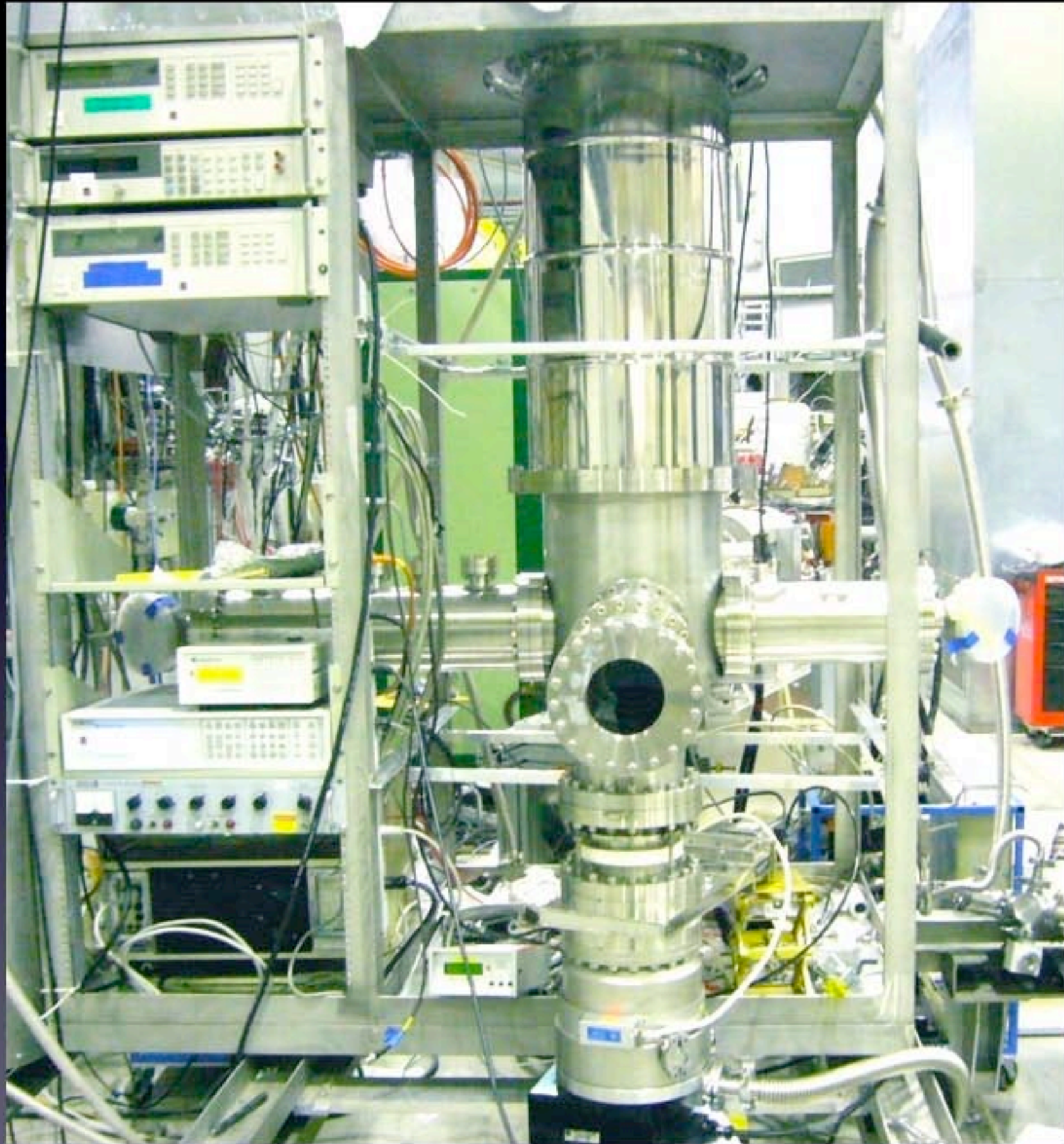
10^{16} - 10^{18} cm⁻³

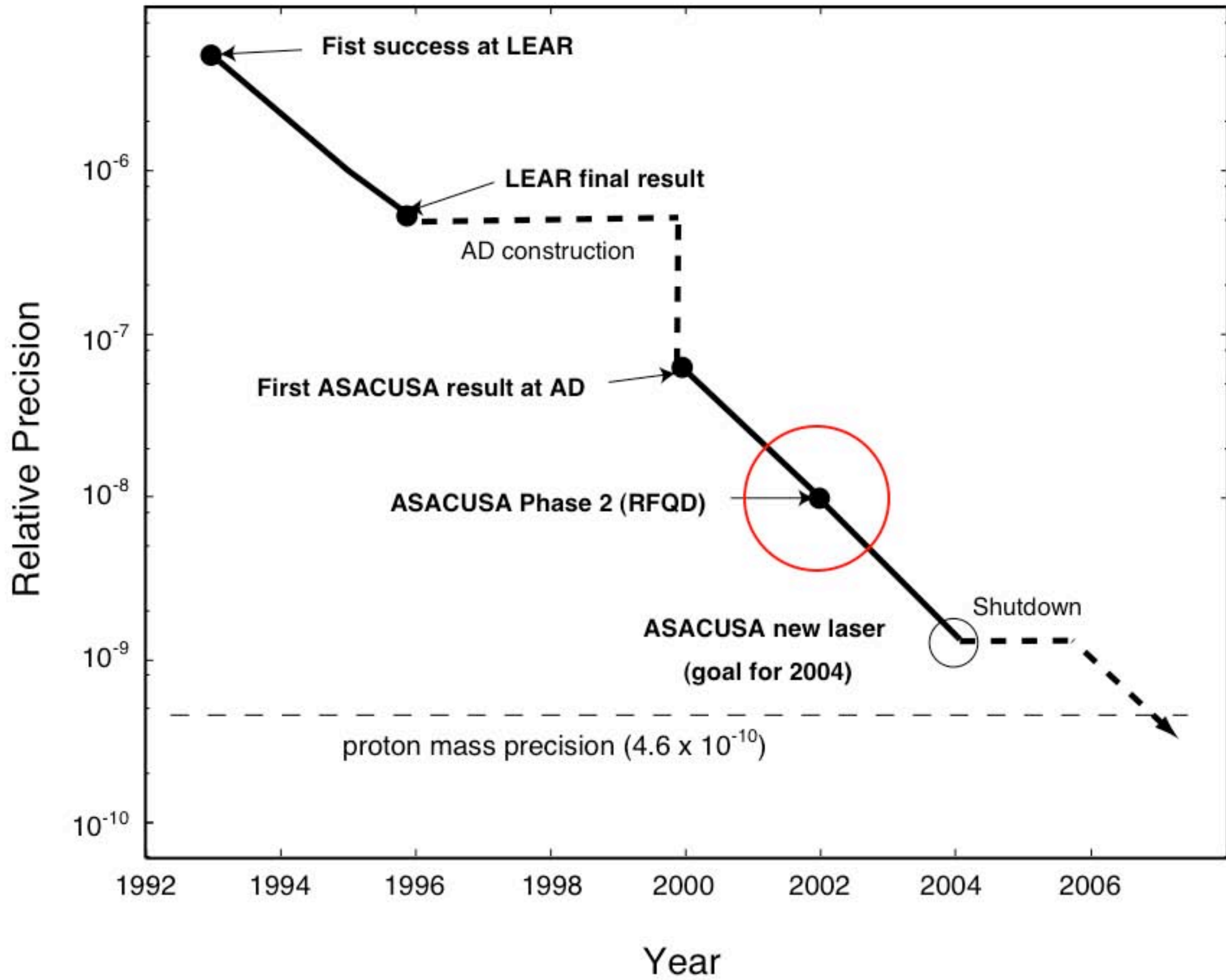
10^{21} cm⁻³

Antiproton Decelerator
(1% of c, ~25% efficiency)

Antiproton pulse from AD
(10% of c)







单色

better laser

M. Hori et al., Phys. Rev. Lett. 96, 243401(2006)

幅の要因

自然幅	15MHz - 150kHz
Fourier幅	パルスレーザー パルス長
衝突	RFQD
ドップラー幅	2光子分光
レーザー単色性	パルスレーザー →CWレーザー

シフトの要因

衝突	RFQD
チャープ	~2MHz, パルスレーザー不可避
周波数較正	光周波数comb
AC Stark	\propto Power
(理論)	~MHz?

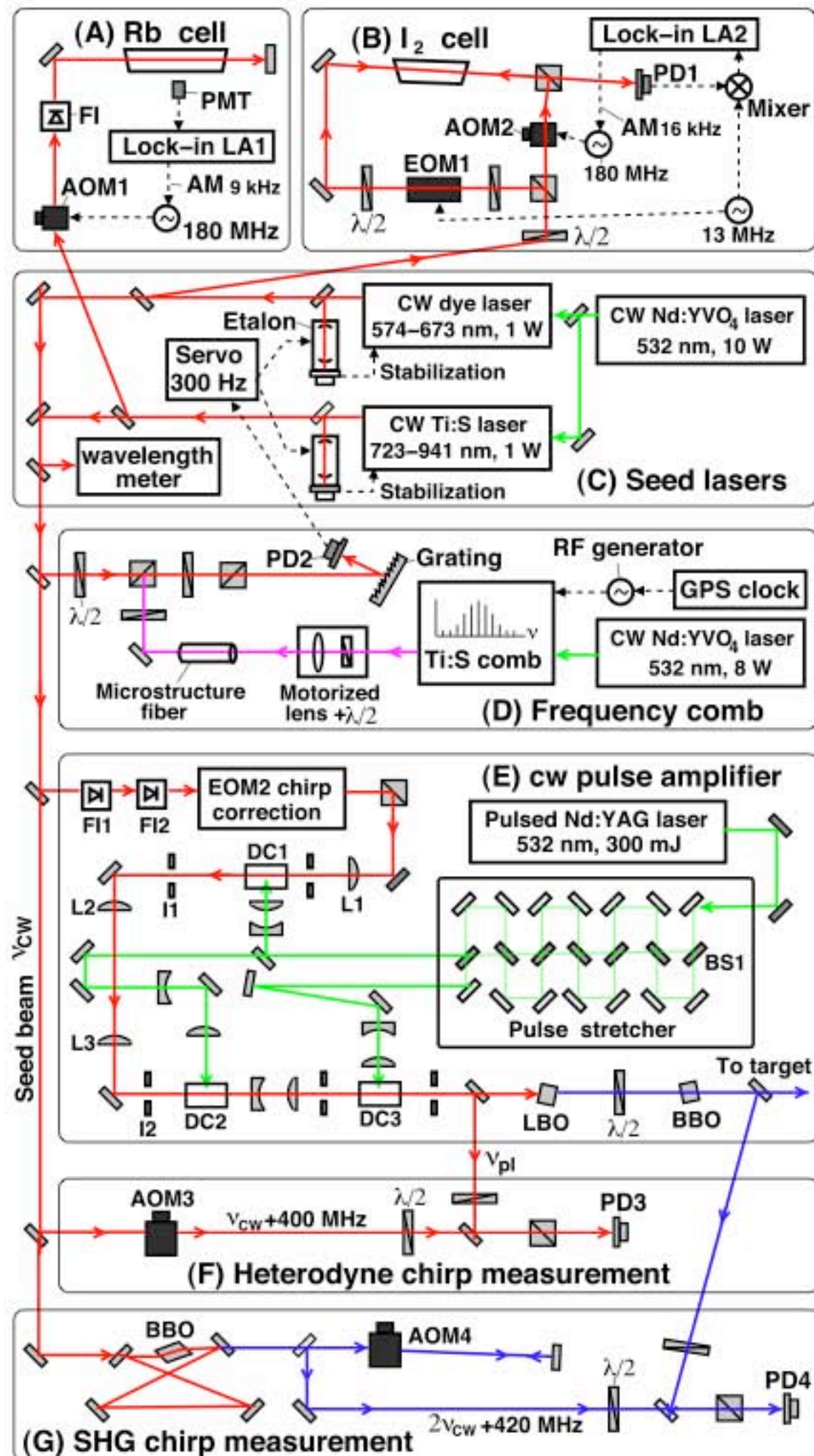
Known
lines

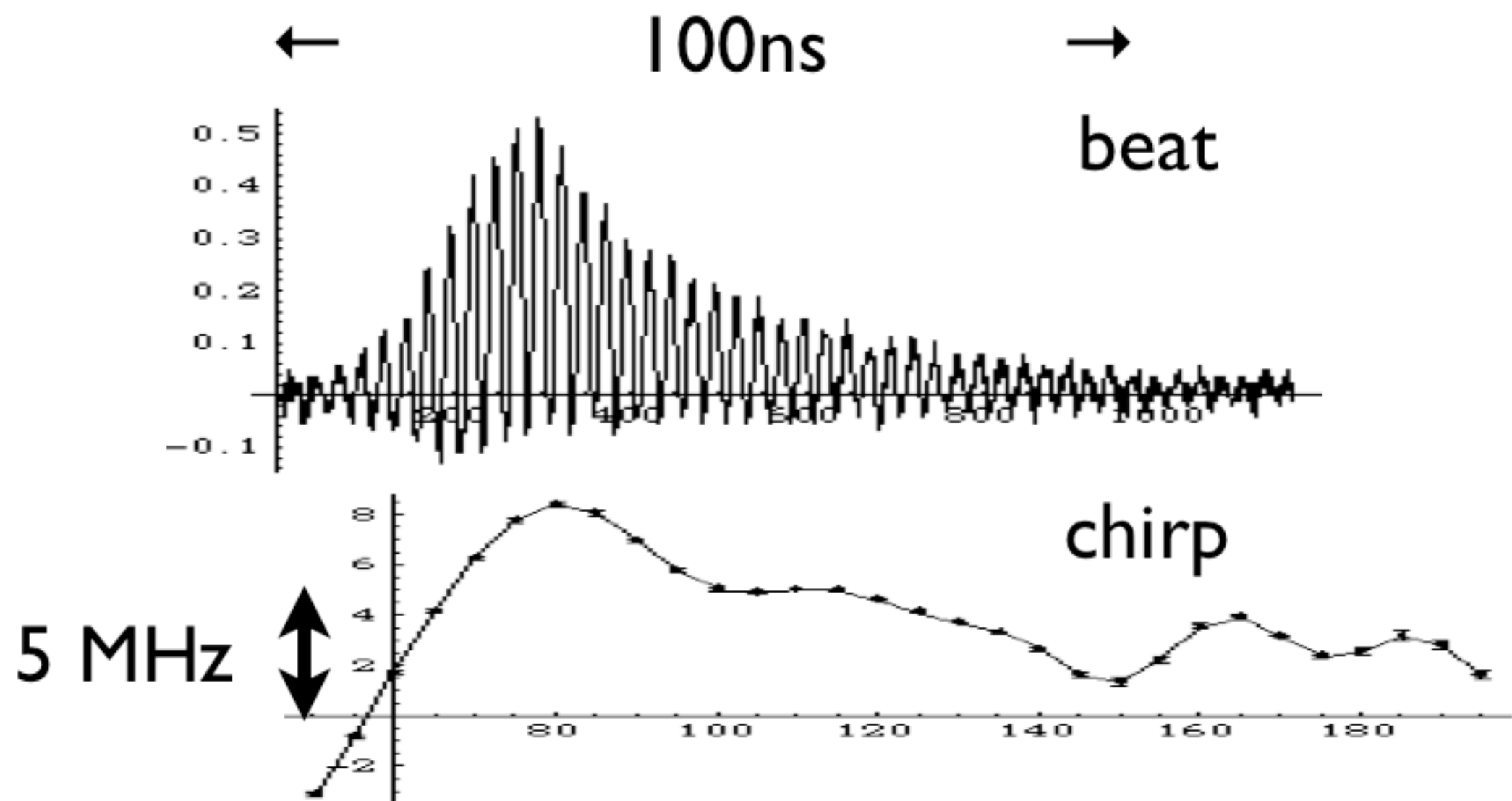
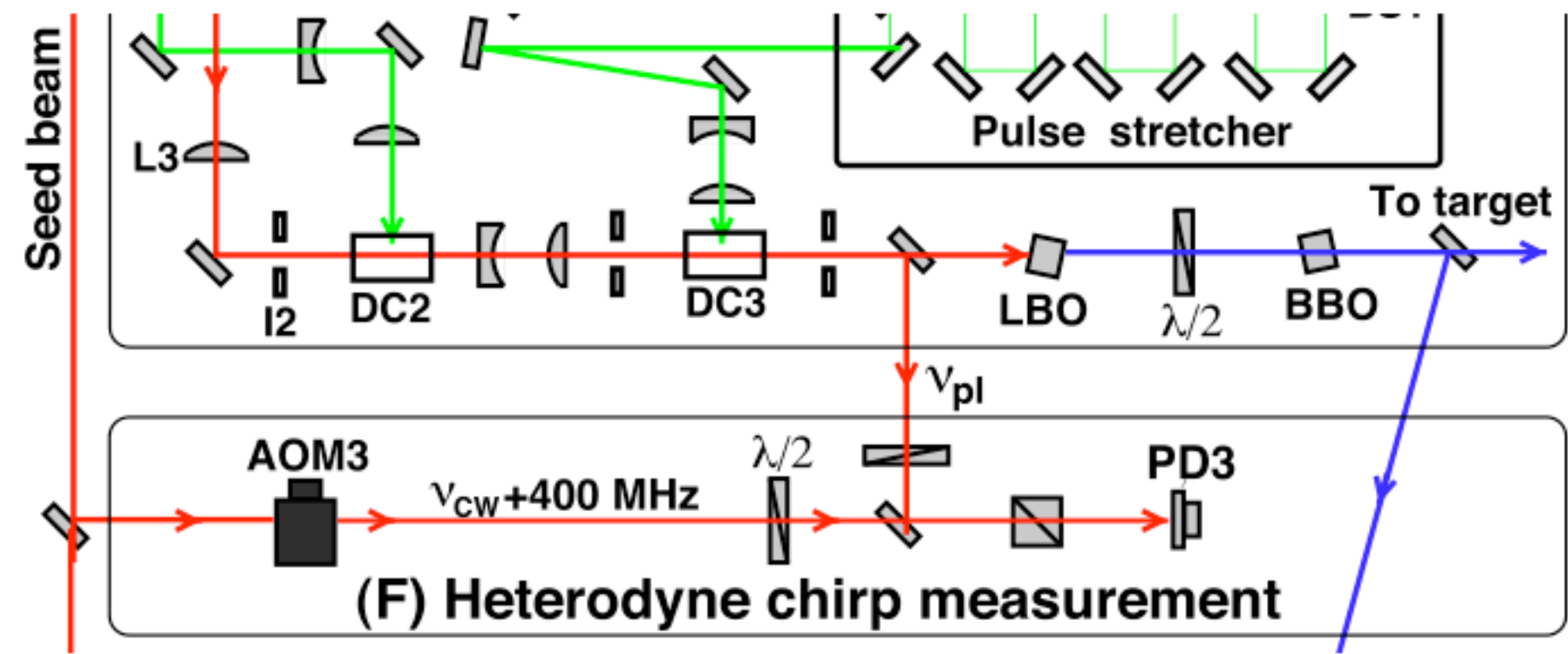
CW

Comb

Amplifier
stretcher

Chirp

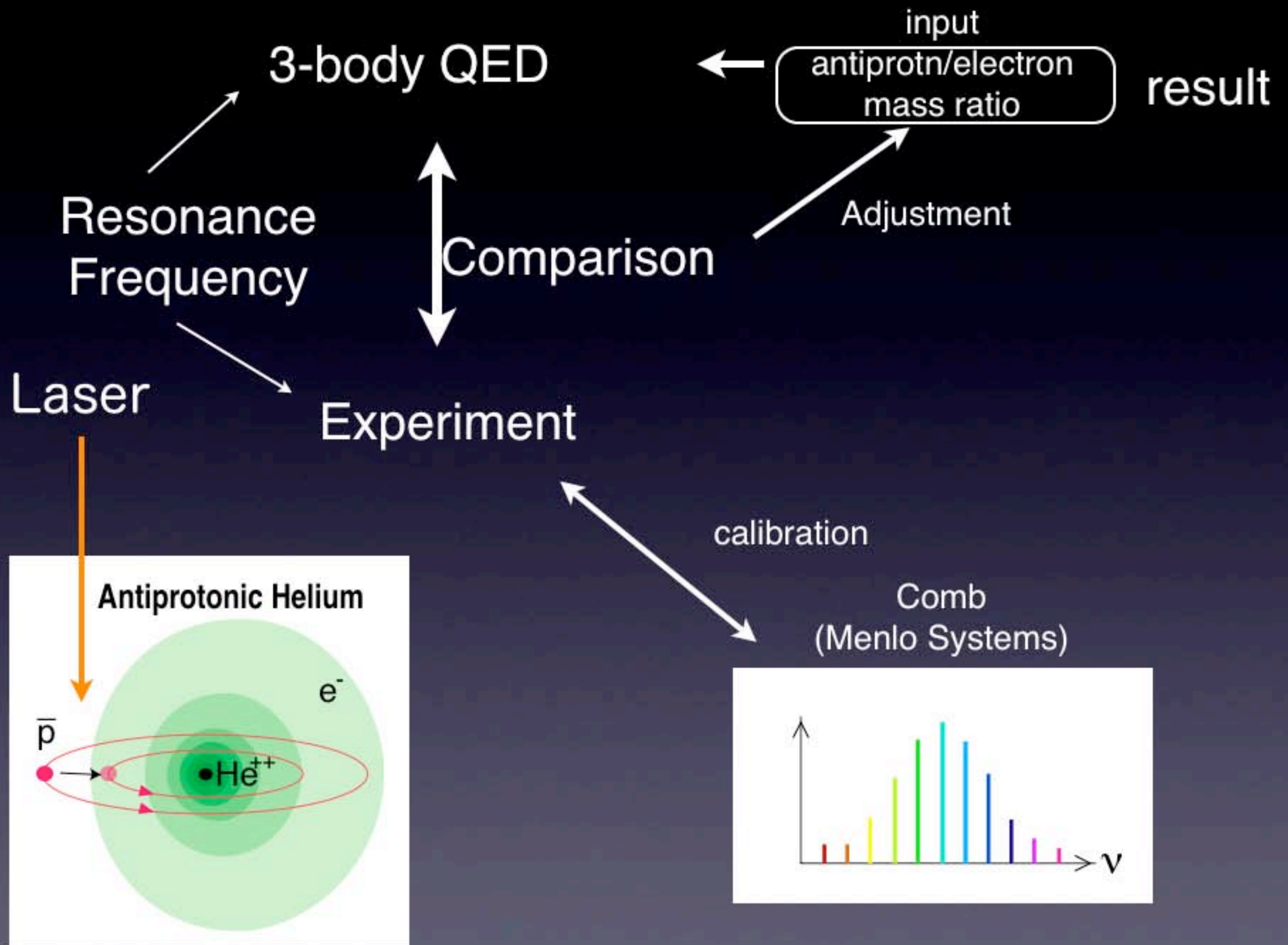




質量比

How to obtain

$$m_{\bar{p}}/m_e$$

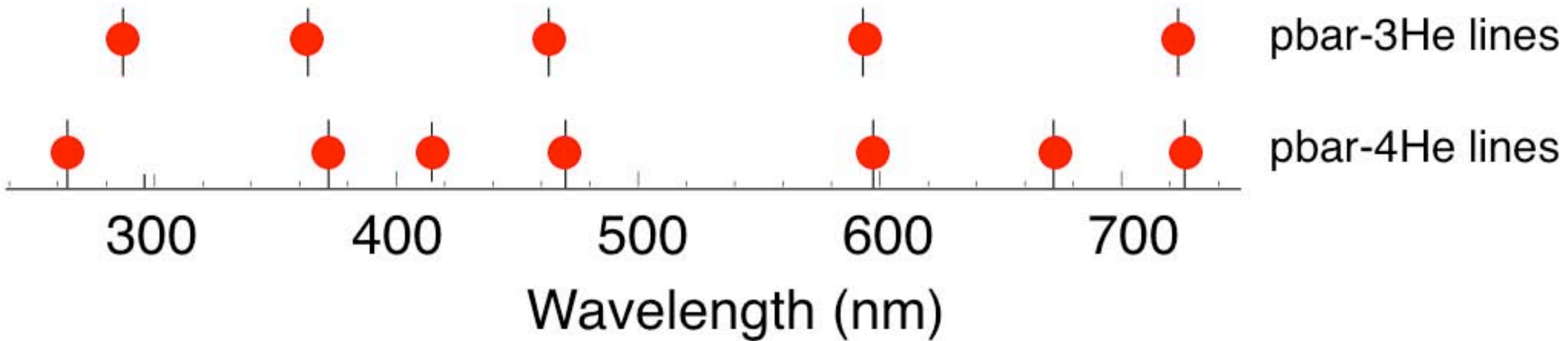


wavelengths of the resonance lines

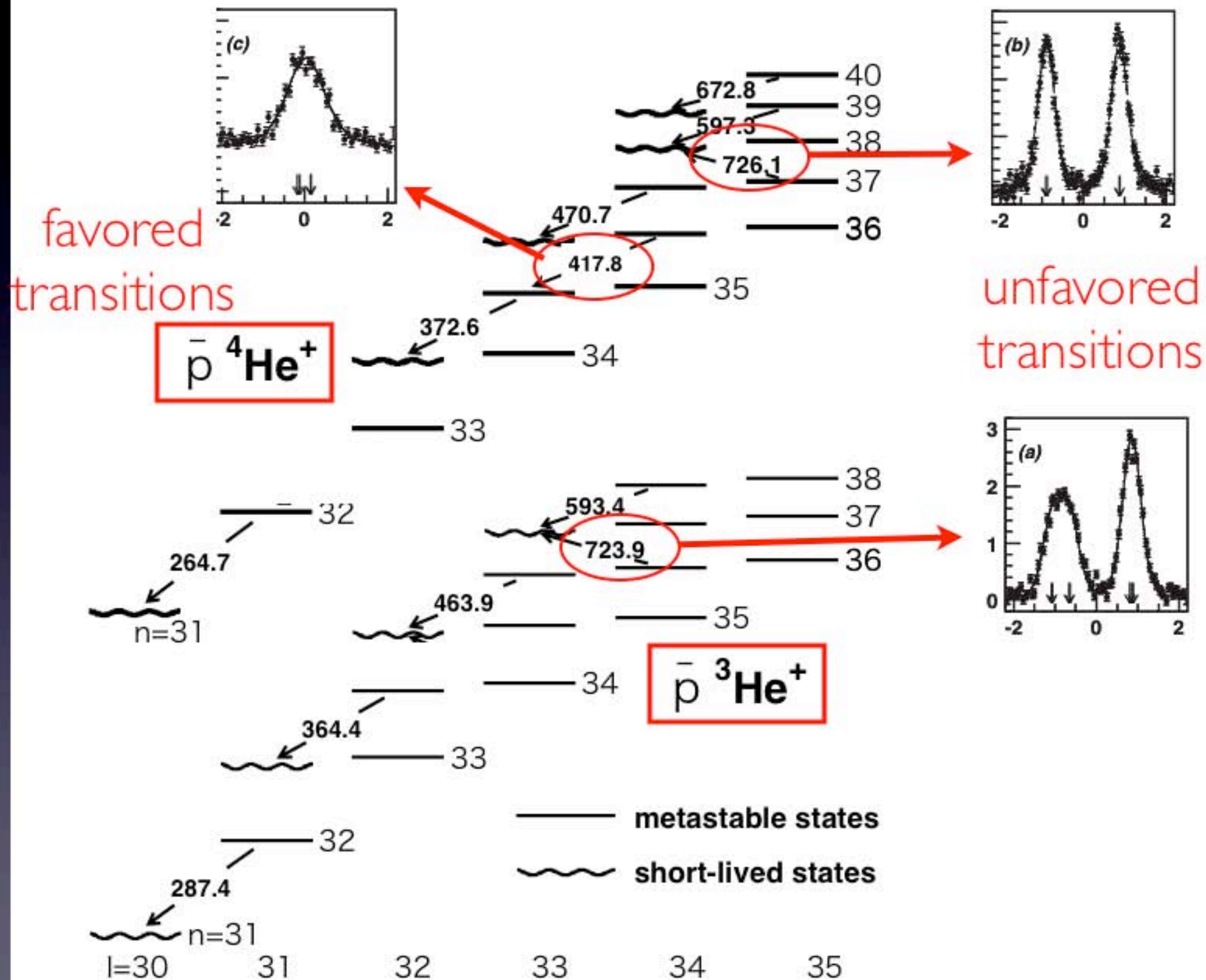
UV



IR



12 transitions were measured



理論

and the results were compared with
(spinless) 3-body QED theoretical calculations

Theory - non-relativistic H

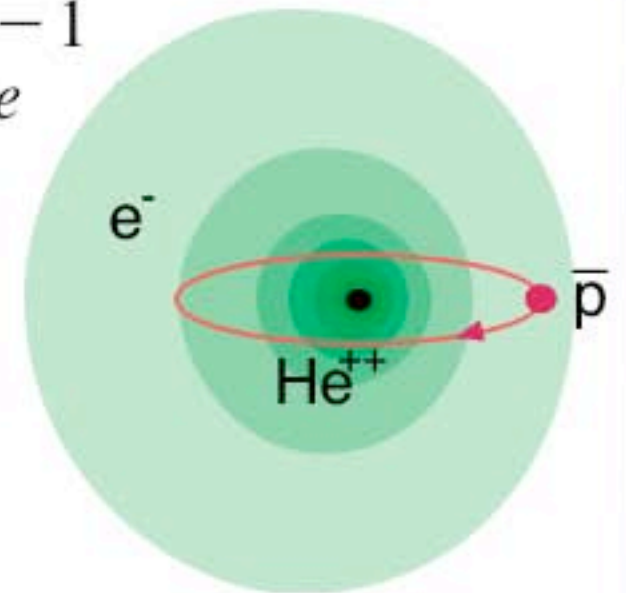
antiproton

electron

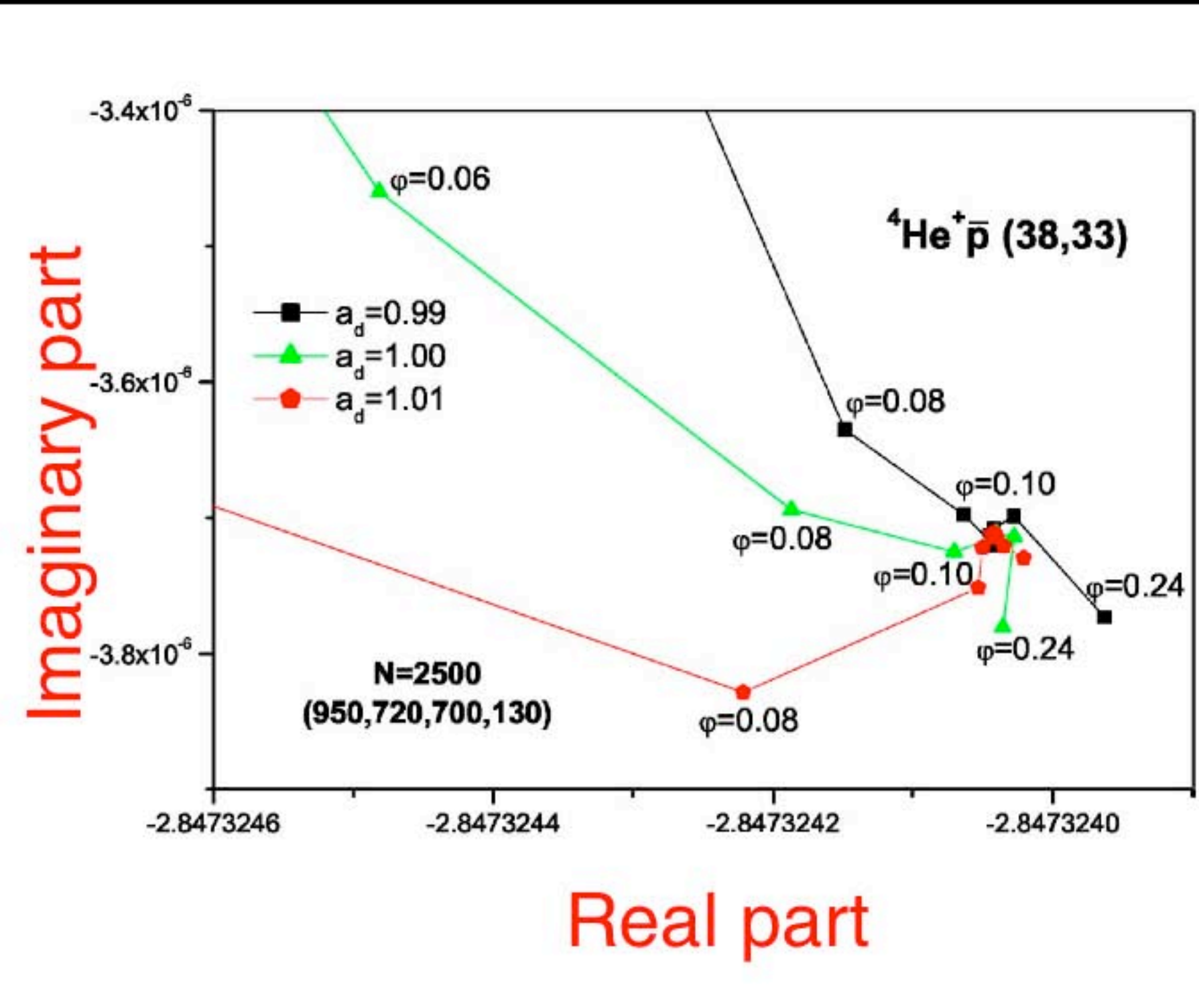
$$H = T + V$$

$$= -\frac{1}{2\mu_1} \nabla_{\mathbf{R}}^2 - \frac{1}{2\mu_2} \nabla_{\mathbf{r}}^2 - \frac{1}{M_{\text{He}}} \nabla_{\mathbf{R}} \cdot \nabla_{\mathbf{r}} - \frac{2}{R} - \frac{2}{r} + \frac{1}{|\mathbf{R} - \mathbf{r}|},$$

$$\mu_1^{-1} = M_{\text{He}}^{-1} + M_X^{-1}, \quad \mu_2^{-1} = M_{\text{He}}^{-1} + m_e^{-1}$$



Complex coordinate rotation (CCR) method



Not true bound states

Careful treatment of Auger decay is needed

CCR calculates complex eigen values

add relativistic correction (~ 100 ppm)

$$H = T + V$$

$$= -\frac{1}{2\mu_1} \nabla_{\mathbf{R}}^2 - \frac{1}{2\mu_2} \nabla_{\mathbf{r}}^2 - \frac{1}{M_{\text{He}}} \nabla_{\mathbf{R}} \cdot \nabla_{\mathbf{r}} - \frac{2}{R} - \frac{2}{r} + \frac{1}{|\mathbf{R} - \mathbf{r}|},$$

$$\mu_1^{-1} = M_{\text{He}}^{-1} + M_X^{-1}, \quad \mu_2^{-1} = M_{\text{He}}^{-1} + m_e^{-1},$$

$$E_{rc} = \alpha^2 \left\langle -\frac{\mathbf{p}_e^4}{8m_e^3} + \frac{4\pi}{8m_e^2} [Z_{\text{He}} \delta(\mathbf{r}_{\text{He}}) + Z_p^- \delta(\mathbf{r}_p^-)] \right\rangle.$$

add self energy (~ 15 ppm)

$$H=T+V$$

$$= -\frac{1}{2\mu_1} \nabla_{\mathbf{R}}^2 - \frac{1}{2\mu_2} \nabla_{\mathbf{r}}^2 - \frac{1}{M_{\text{He}}} \nabla_{\mathbf{R}} \cdot \nabla_{\mathbf{r}} - \frac{2}{R} - \frac{2}{r} + \frac{1}{|\mathbf{R}-\mathbf{r}|}$$

$$\mu_1^{-1} = M_{\text{He}}^{-1} + M_X^{-1}, \quad \mu_2^{-1} = M_{\text{He}}^{-1} + m_e^{-1}$$

$$E_{rc} = \alpha^2 \left\langle -\frac{\mathbf{p}_e^4}{8m_e^3} + \frac{4\pi}{8m_e^2} [Z_{\text{He}} \delta(\mathbf{r}_{\text{He}}) + Z_p^- \delta(\mathbf{r}_p^-)] \right\rangle$$

Bethe logarithm

$$E_{se} = \frac{4\alpha^3}{3m_e^2} \left[\ln \frac{1}{\alpha^2} - \ln \frac{k_0}{R_\infty} + \frac{5}{6} - \frac{3}{8} \right] \langle Z_{\text{He}} \delta(\mathbf{r}_{\text{He}}) + Z_p^- \delta(\mathbf{r}_p^-) \rangle$$

$$+ \frac{4\alpha^4}{3m_e^2} \left[3\pi \left(\frac{139}{128} - \frac{1}{2} \ln 2 \right) \right] \langle Z_{\text{He}}^2 \delta(\mathbf{r}_{\text{He}}) + Z_p^-^2 \delta(\mathbf{r}_p^-) \rangle$$

$$- \frac{4\alpha^5}{3m_e^2} \left[\frac{3}{4} \right] \langle Z_{\text{He}}^3 \ln^2(Z_{\text{He}} \alpha)^{-2} \delta(\mathbf{r}_{\text{He}})$$

$$+ Z_p^-^3 \ln^2(Z_p^- \alpha)^{-2} \delta(\mathbf{r}_p^-) \rangle,$$

(39,35) → (38,34) example (Korobov)

$$E_{nr} = 501\,972\,347.9$$

$$E_{rc} = -27\,525.3$$

$$E_{rc-qed} = 233.3$$

$$E_{se} = 3\,818.0$$

$$E_{vp} = -122.5$$

$$E_{kin} = 37.3$$

$$E_{exch} = -34.7$$

$$E_{\alpha^3-rec} = 0.8$$

$$E_{two-loop} = 0.9$$

$$E_{nuc} = 2.4$$

$$E_{\alpha^4} = -2.6$$

$$\Delta E_{vp} = \frac{4z_i\alpha^3}{3m_3^2} \left[-\frac{1}{5} + (z_i\alpha)\pi \frac{5}{64} \right] \langle \delta(\mathbf{r}_i) \rangle,$$

$$\Delta E_{kin} = \alpha^2 \left\langle -\frac{\nabla_1^4}{8m_1^3} - \frac{\nabla_2^4}{8m_2^3} + \frac{(1+2a_2)z_2}{8m_2^2} 4\pi\delta(\mathbf{r}_2) \right\rangle,$$

$$\Delta E_{exch} = -\alpha^2 \frac{z_i}{2m_i m_3} \left\langle \frac{\nabla_i \nabla_3}{r_i} + \frac{\mathbf{r}_i (\mathbf{r}_i \nabla_i) \nabla_3}{r_i^3} \right\rangle,$$

$$\Delta E_{recoil}^{(3)} = \frac{z_i\alpha^3}{m_i m_3} \left\{ \frac{2}{3} \left(-\ln\alpha - 4\beta + \frac{31}{3} \right) \langle \delta(\mathbf{r}_i) \rangle - \frac{14}{3} \langle Q(\mathbf{r}_i) \rangle \right\},$$

$$\Delta E_{two-loop} = \alpha^4 \frac{z_i}{m_3^2 \pi} \left[-\frac{6131}{1296} - \frac{49\pi^2}{108} + 2\pi^2 \ln 2 - 3\zeta(3) \right] \langle \delta(\mathbf{r}_i) \rangle$$

$$\Delta E_{nuc} = \frac{2\pi z_i (R_i/a_0)^2}{3} \langle \delta(\mathbf{r}_i) \rangle,$$

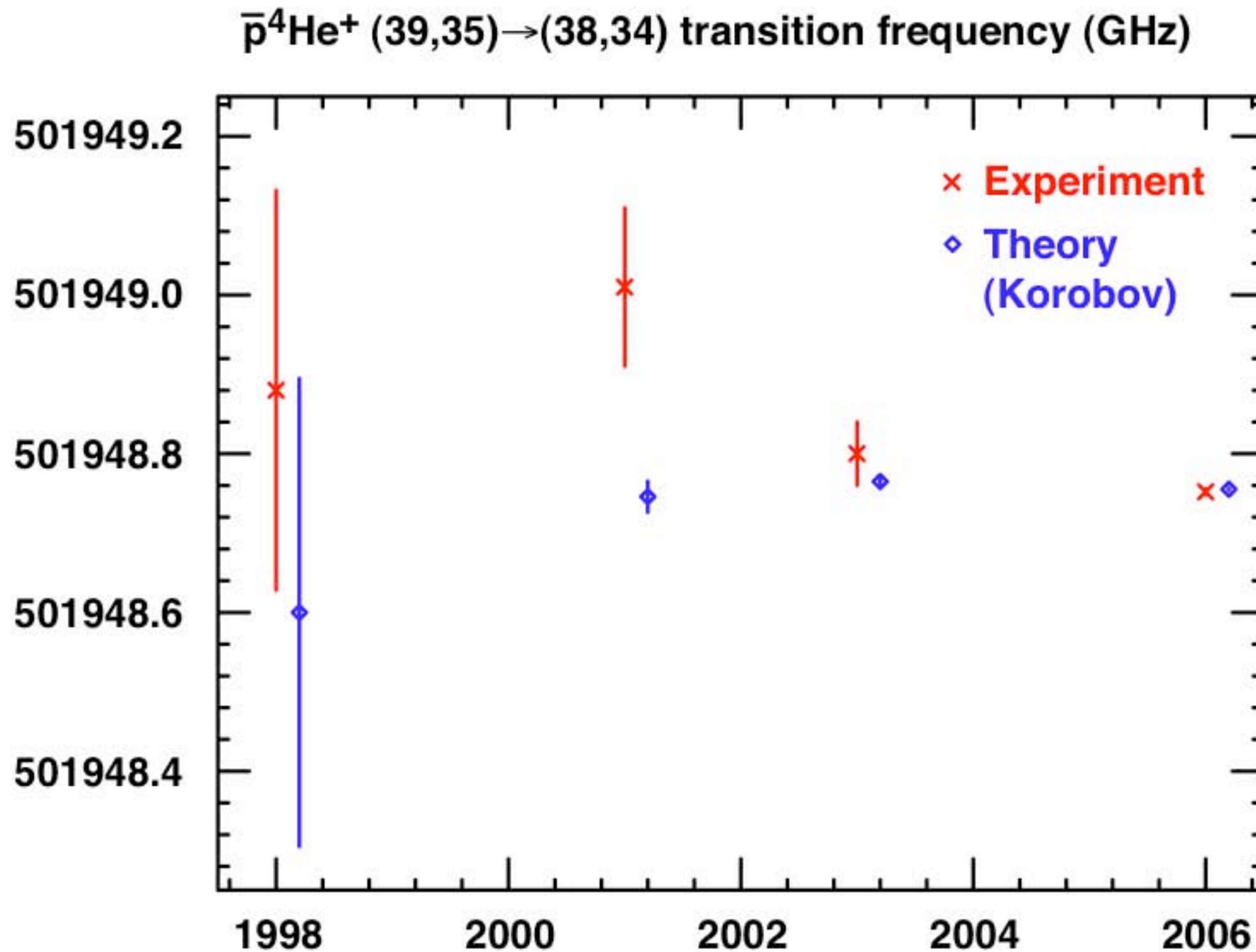
$$\Delta E_{\alpha^4} \approx -\alpha^4 \frac{\pi}{2} \delta(\mathbf{r}_1).$$

$$E_{total} = 501\,948\,755.6(1.3) \text{ MHz}$$

結果

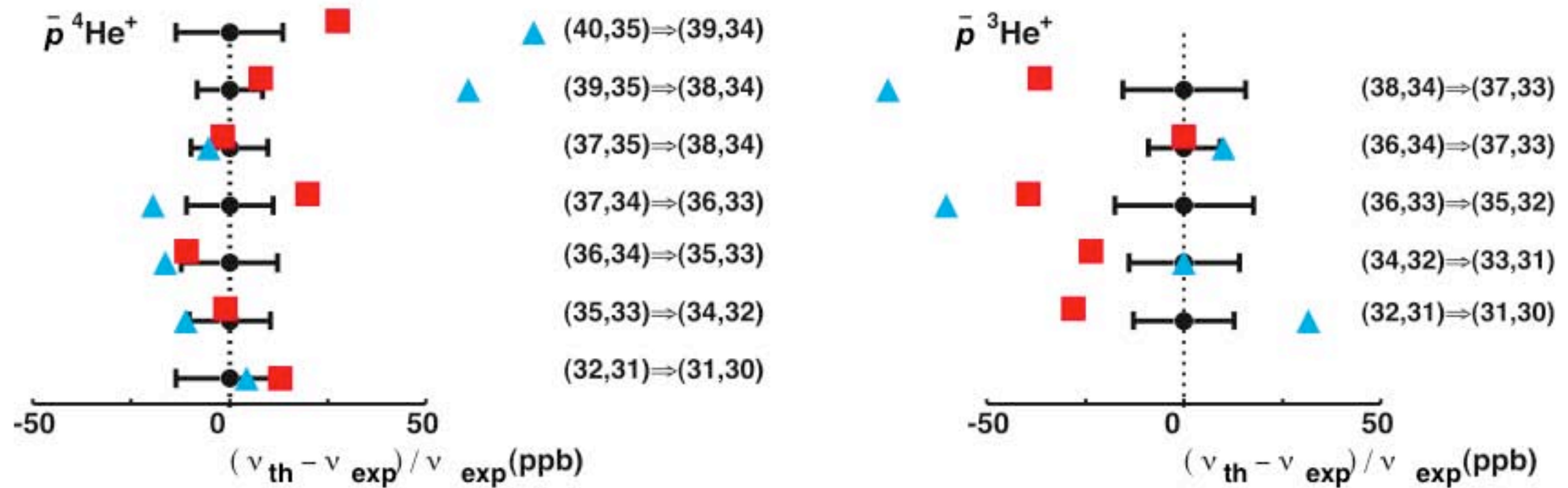
Results & Implications

Experimental & theoretical precisions improved



Exp vs Theory

Two theory calculations (▲ and ■)



- Up to ~50 ppb differences between the two theoretical calculations (▲ and ■) ; we now take ■ in view of the claimed accuracy
- Systematic shift of some 20 ppb in $\bar{p}^3\text{He}^+$

Errors

$$\sigma_{\text{exp}} = 4\text{-}15 \text{ MHz}$$

statistical 3-13 MHz,

systematic: chirp 2-4 MHz, collisional shifts 0.1-2 MHz,
harmonic generation 1-2 MHz

(and negligible AC-Stark)

$$\sigma_{\text{theory}} = 1\text{-}2 \text{ MHz (Korobov)}$$

$$m_{\bar{p}}/m_e = 1836.152674$$

$$\pm 0.000005$$

ASACUSA2006

PRL 96, 243401 (2006)

$$m_p/m_e = 1836.15267261$$

$$\pm 0.00000085$$

codata2002

2007

ongoing effort

幅の要因

自然幅	15MHz - 150kHz
Fourier幅	パルスレザ パルス長
衝突	RFQD
ドップラー幅	2光子分光
レザ単色性	パルスレザ CWレザ

シフトの要因

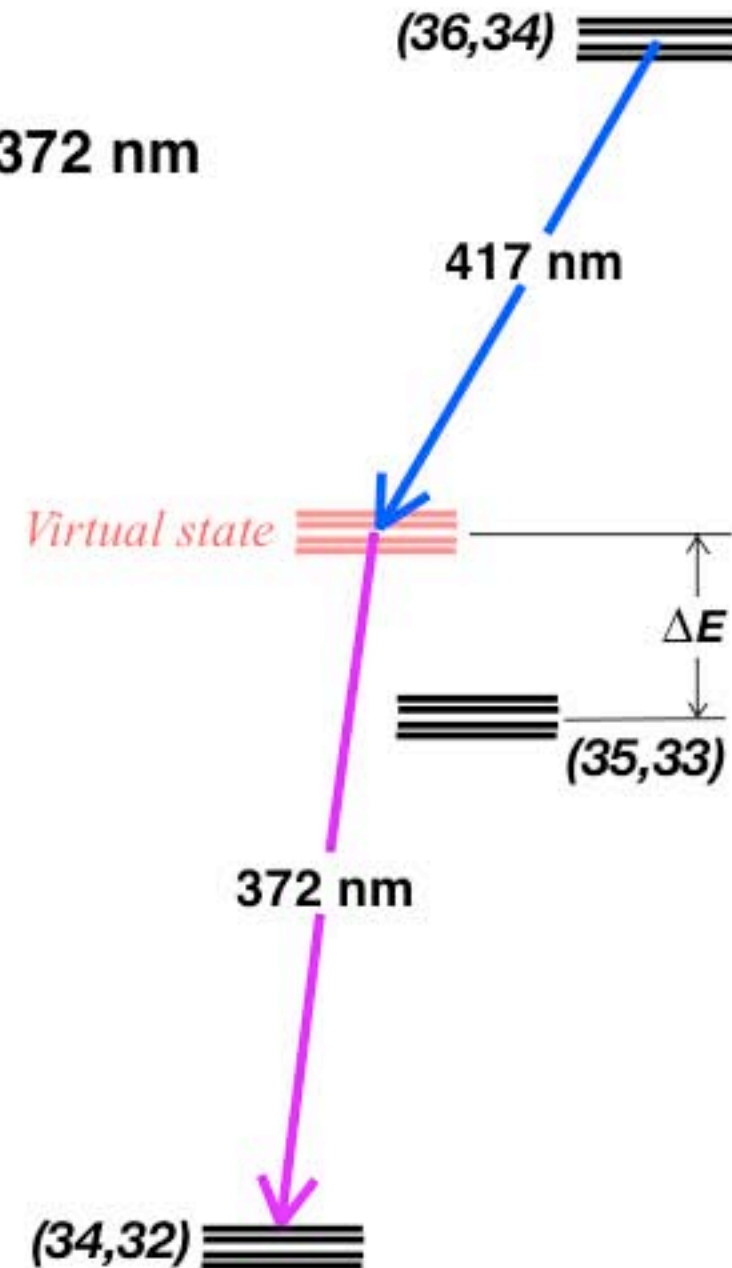
衝突	RFQD
チャープ	2MHz, パルスレザ不可避
周波数較正	光周波数comb
AC Stark	\propto Power
(理論)	~MHz?

Sub-Doppler two-photon laser spectroscopy

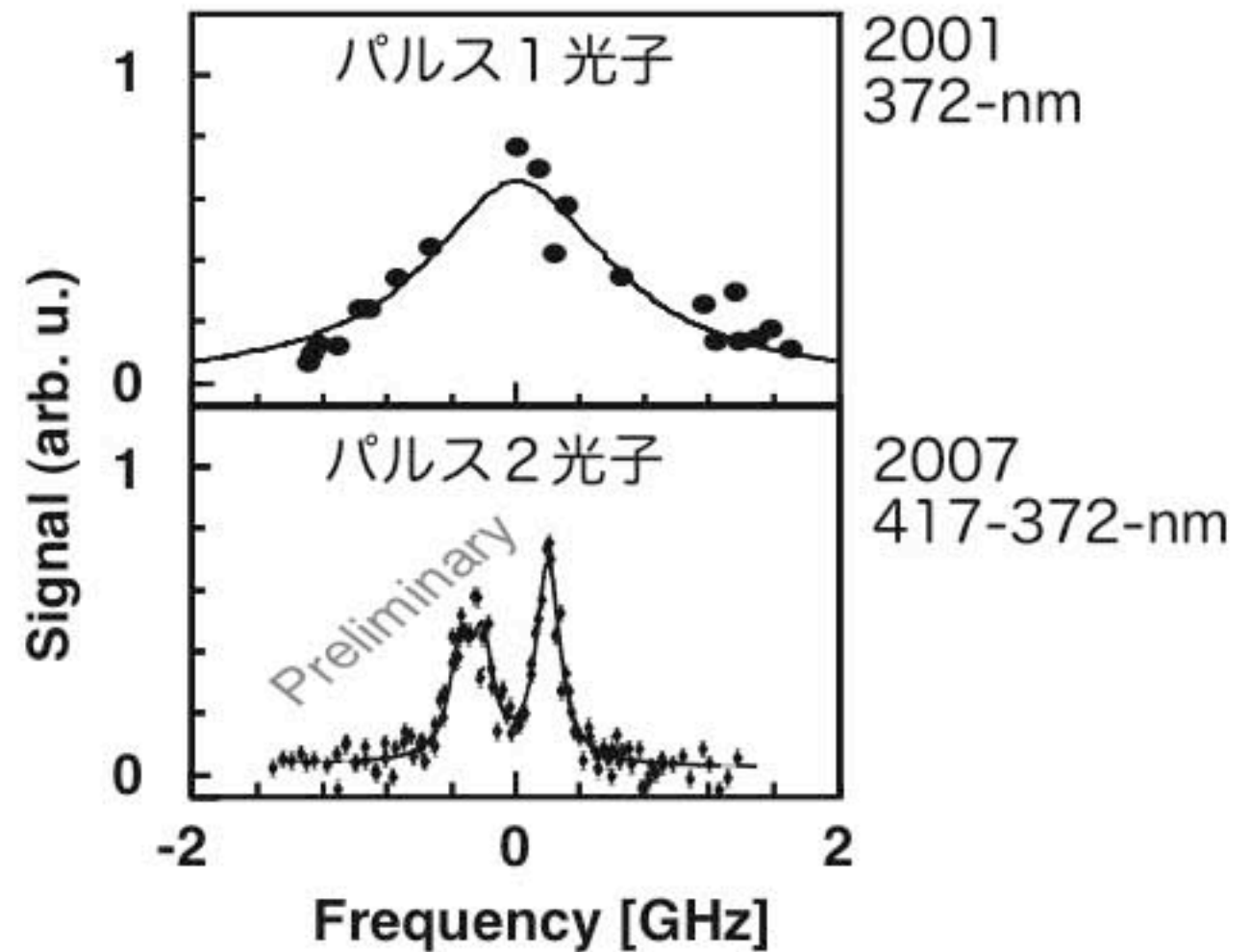
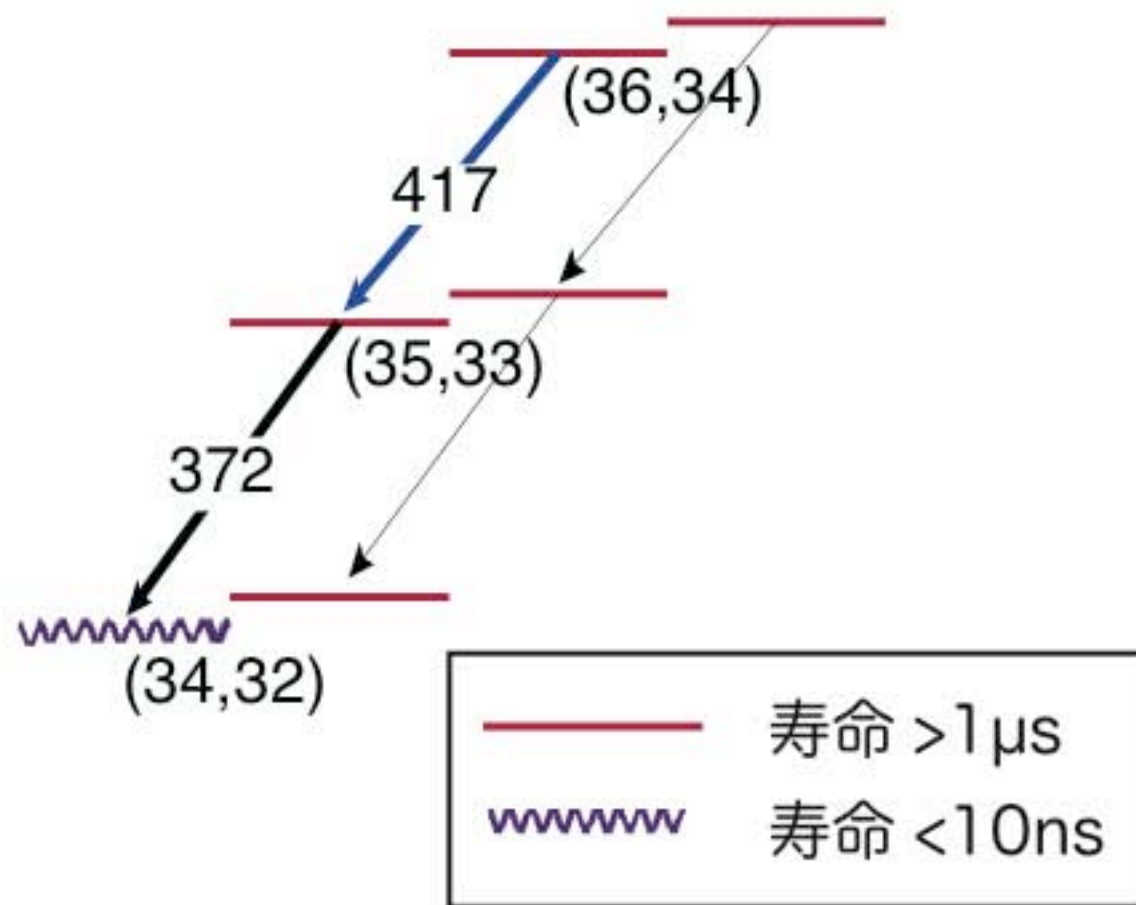


Doppler width decreased
from 1300 MHz to 70 MHz

$$\Gamma = \frac{|v_1 - v_2|}{v_1 + v_2} \times 2.35(v_1 + v_2) \sqrt{\frac{kT}{M}}$$



線幅大幅に減少




 CODATA 98

 CODATA 02

 ASACUSA 2006

being considered for the codata 06
adjustments

 Projected 2007?


6.5 7.0 7.5 x 10⁻⁴
mass ratio -1836.1526

パルスレーザーの限界に達した

次

まだまだまだやるぞ

パルスレーザーをやめるしかない

幅の要因

自然幅	15MHz - 150kHz
Fourier幅	パルスレザ パルス長
衝突	RFQD
ドップラ幅	2光子分光
レザ単色性	パルスレザ CWレザ

シフトの要因

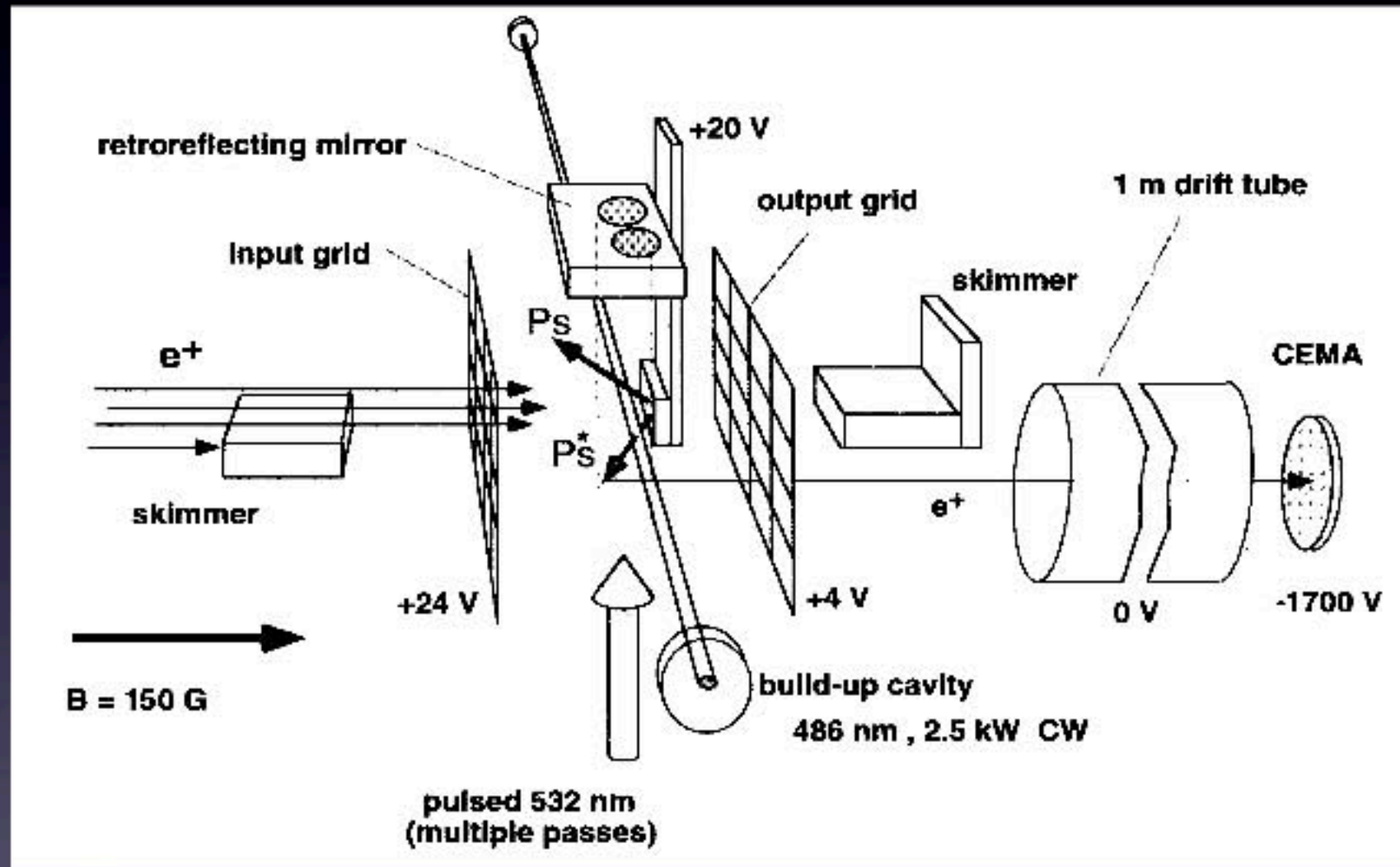
衝突	RFQD
チャープ	~2MHz, パルスレーザー不可避
周波数較正	光周波数comb
AC Stark	\propto Power
(理論)	~MHz?

エキゾチック原子のレーザー分光

μ^+e^-	meyer et al, PRL 84 (2000) 1136	pulse	2455528941.0(9.8)
e^+e^-	Danzmann et al, PRA 39 (1989) 5072	pulse	1233607218.9(10.7)
e^+e^-	Fee et al, PRA 48 (1993) 192	CW	1233607216.4(3.2)
μ^-p	PSI in progress	pulse	no signal yet
$(\mu^-He)^+$	Zavattini et al	pulse	questionable
$\bar{p}He$	ASACUSA	pulse, so far	2007 very preliminary 1553643100.0(5.0)

the only exotic atom studied by a CW laser system so far... e^+e^-

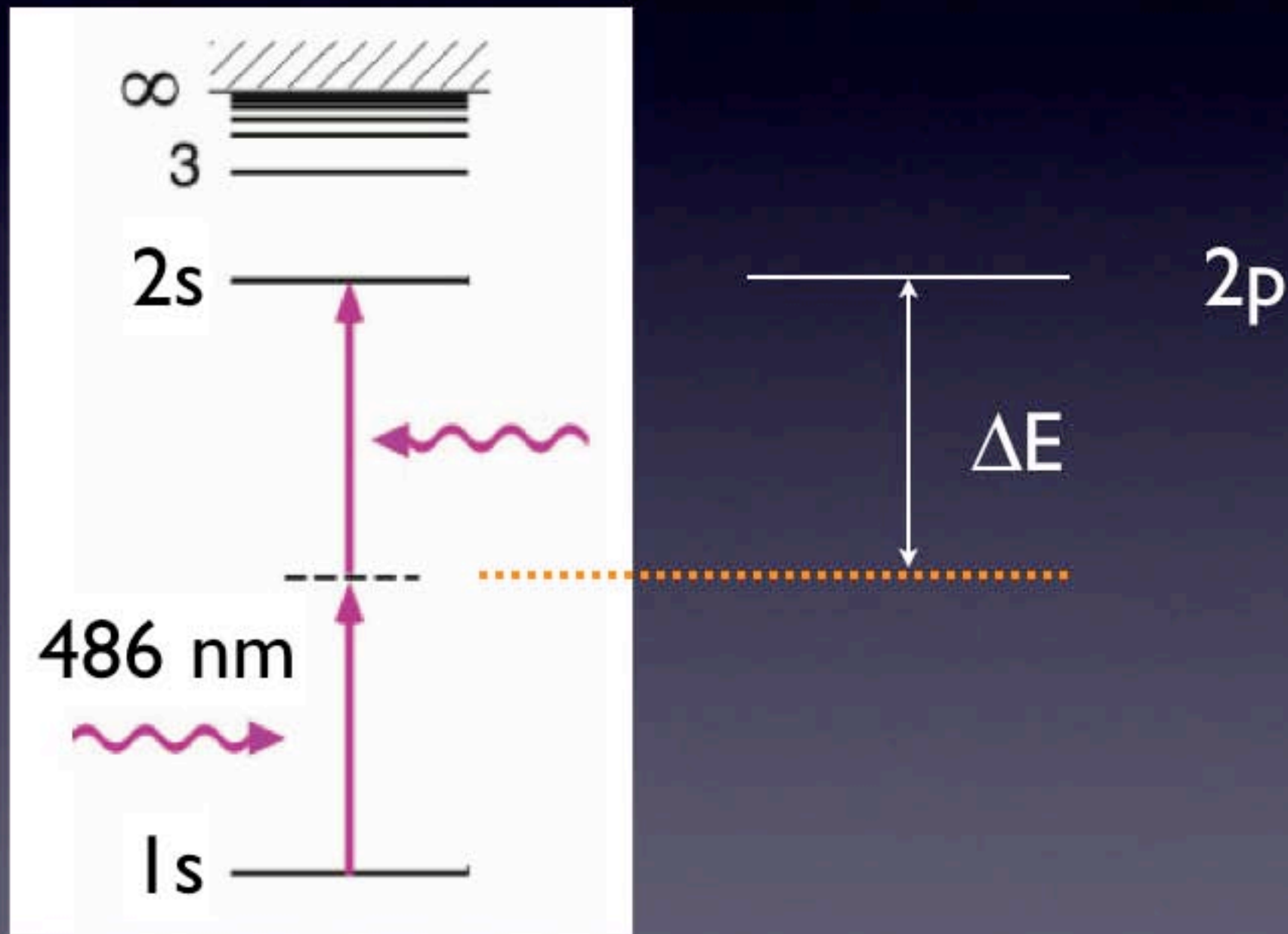
M.S. Fee et al, Phys. Rev. A 48 (1993) 192



2.5 kW CW laser power, power density 1.7 MW/cm^2
これはパルスレーザー顔負けの大強度だ...

巨大パワーが必要な理由

$$\text{power density} \propto \Delta E$$



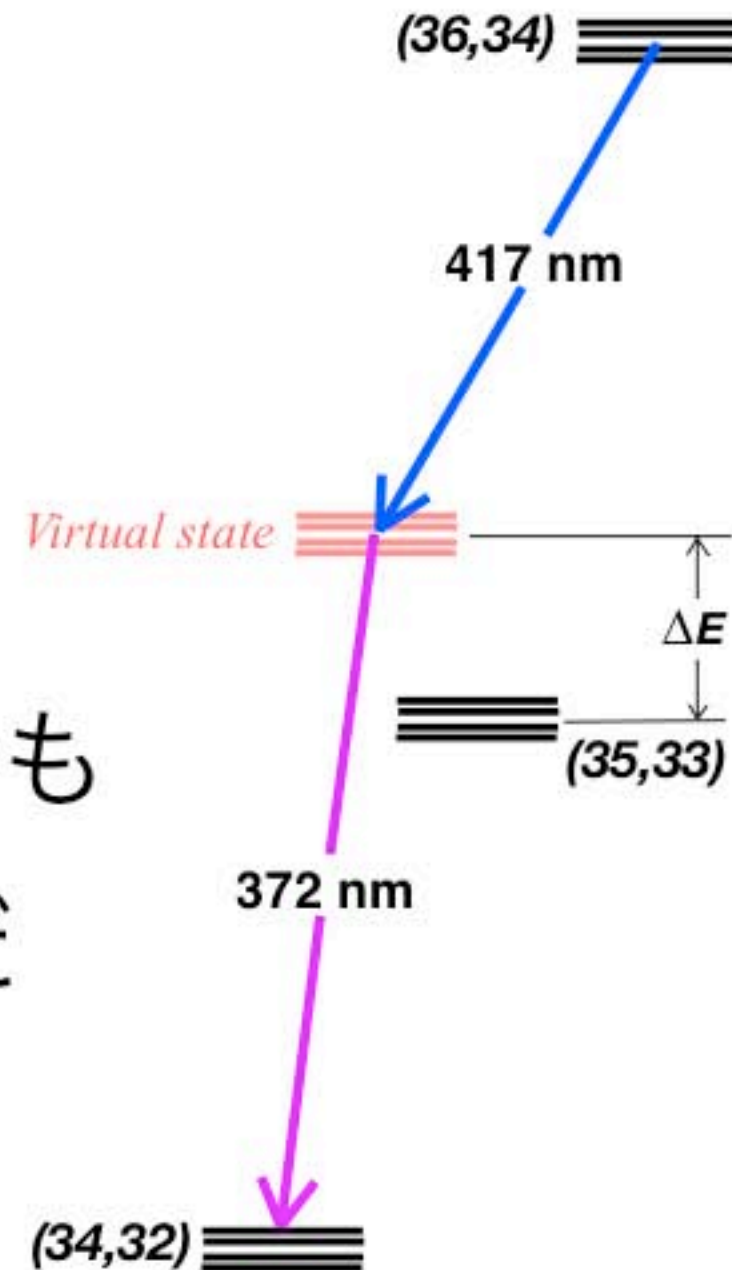
しかしluckyなことに我々は $\Delta E \rightarrow 0$ にできる

パワー密度 $\propto \Delta E$

$\Delta E \rightarrow 0$ とすると

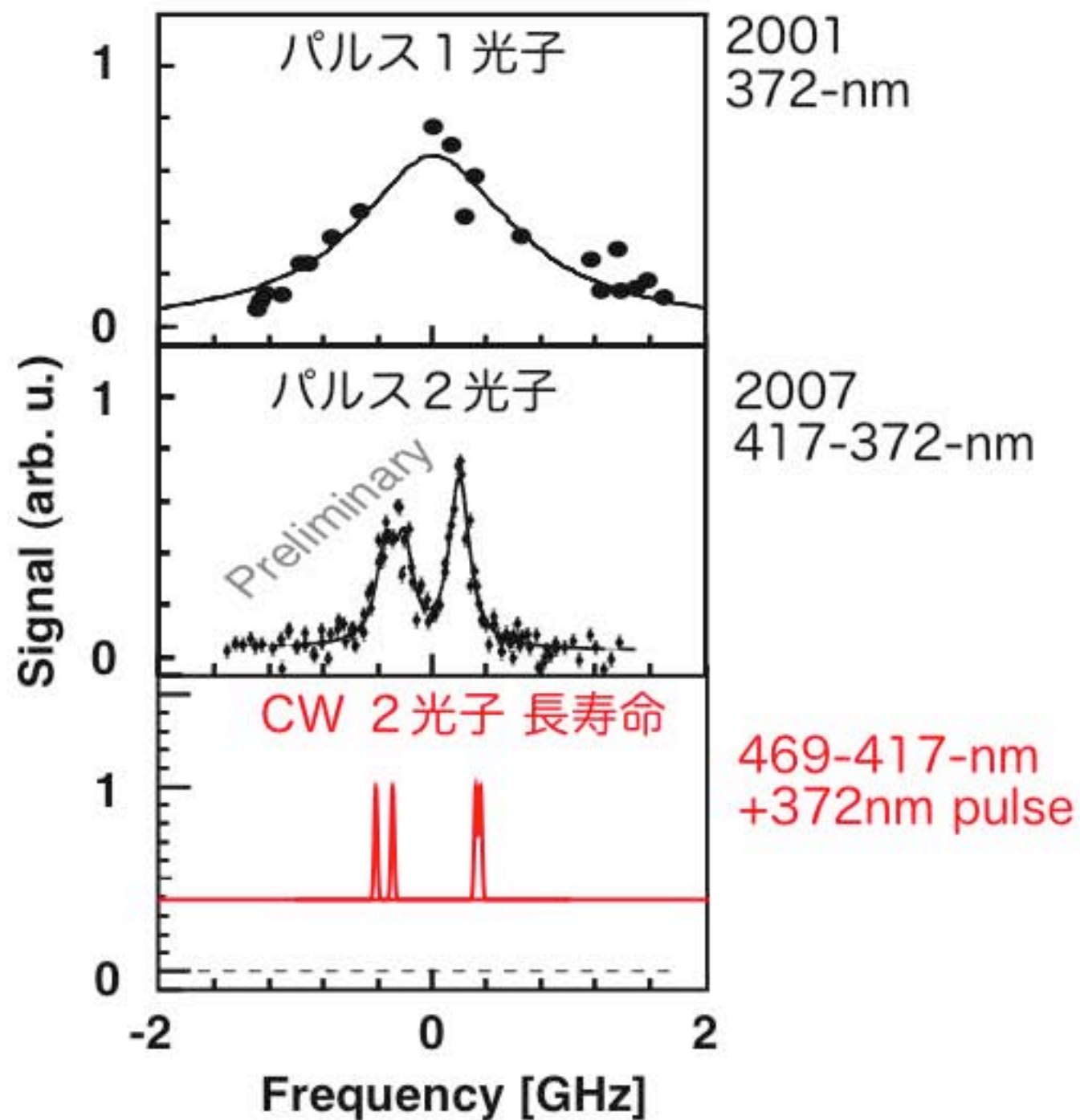
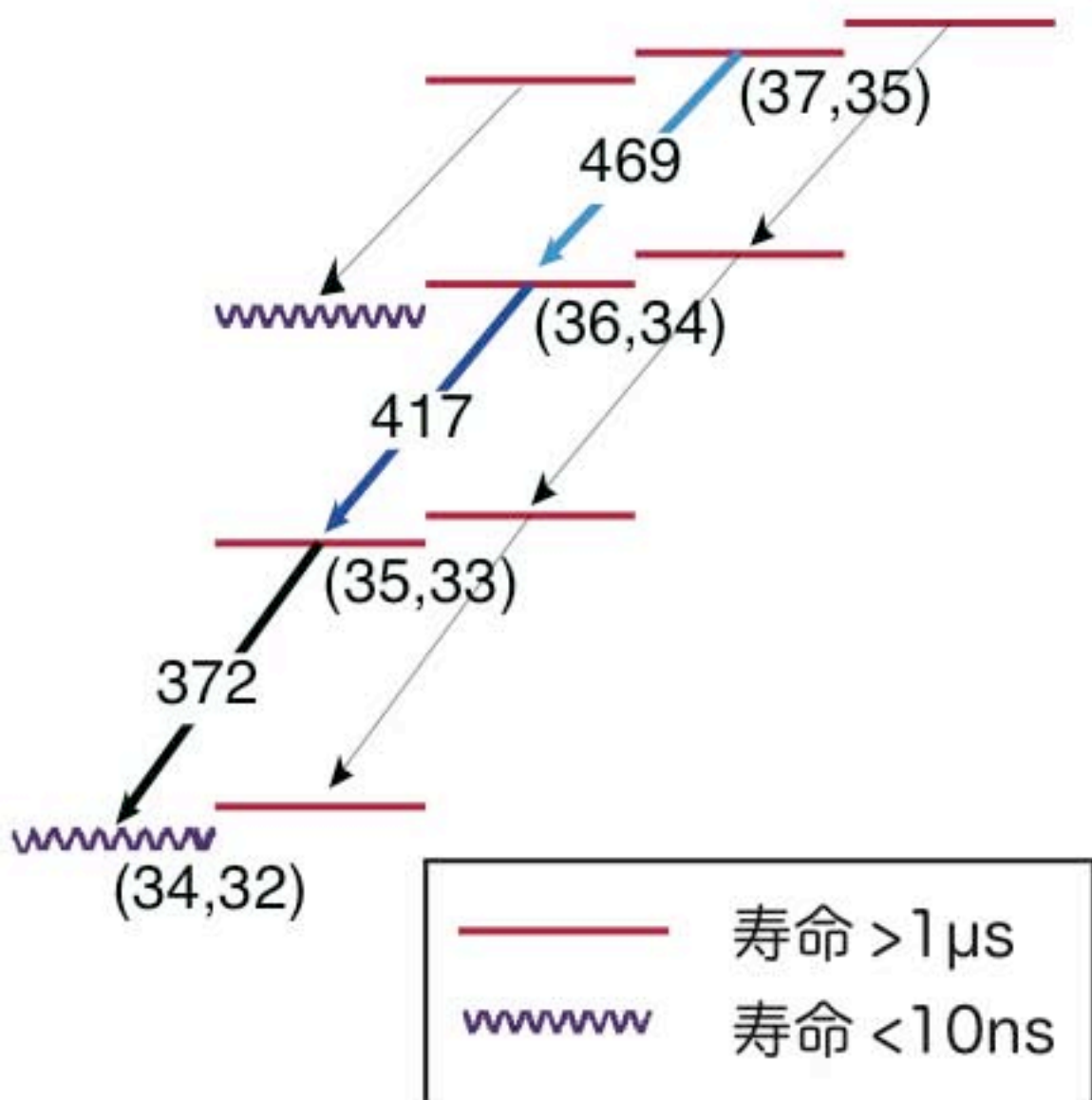
CWレーザーでも可能かも

$< 100 \text{ W/cm}^2$ でよさそうだ



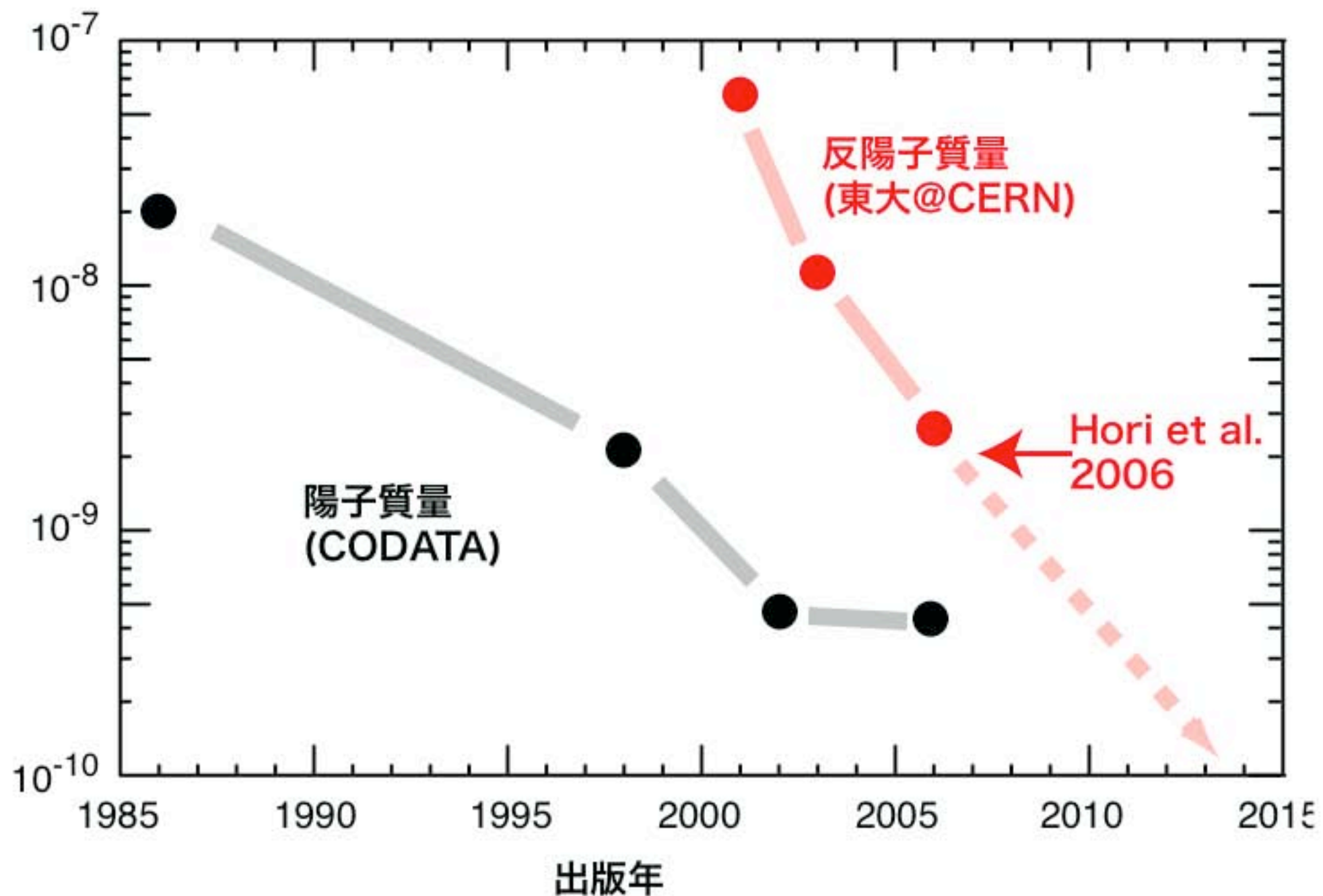
究極の実験

CW, 二光子, 準安定準位間遷移



antiproton mass may become better known

相对標準不確かさ



density shift

RFQD

Comb

2-photon
CW

結

summary

Serendipitous discovery

Precision of $\bar{p}\text{He}$ spectroscopy has reached 10^{-9}
(RFQ, Comb, ..., took us a long time)

$\times 100$ improvement possible (nontrivial but doable),

Update the fundamental constant (m_p/m_e)

but

Must better understand 3-body QED calculations

Masaki Hori, EURYI 受賞 (European Young Investigator Awards)



賞金 2億円で独立研究グループを作る