



Nuclear Astrophysics I. Hydrostatic stellar burning

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Nuclear Astrophysics

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Nuclear astrophysics aims at understanding the nuclear processes that take place in the universe. These nuclear processes generate energy in stars and contribute to the nucleosynthesis of the elements.



N. Grevesse and A. J. Sauval, Space Science Reviews 85, 161

Hoyle's cosmic cycle



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Nucleosynthesis processes

In 1957: Burbidge, Burbidge, Fowler, Hoyle, [Rev. Mod. Phys. **29**, 547 (1957)] suggested the synthesis of the elements in stars.



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Star formation



PRC95-44a · ST Scl OPO · November 2, 1995 J. Hester and P. Scowen (AZ State Univ.), NASA

- Stars are formed from the contraction of molecular clouds due to their own gravity.
- Contraction increases temperature and eventually nuclear fusion reactions begin. A star is born.
- Contraction time depends on mass: 10 millions years for a star with the mass of the Sun; 100,000 years for a star 11 times the mass of the Sun.

The evolution of a Star is governed by gravity

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What is a Star?



equilibrium: gravity \leftrightarrow pressure

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- A star is a self-luminous gaseous sphere.
- Stars produce energy by nuclear fusion reactions. A star is a self-regulated nuclear reactor.
- Gravitational collapse is balanced by pressure generated from nuclear reactions: $dF_{grav} = -G\frac{m(r)dm}{r^2} = dF_{press} = [(P(r + dr) - P(r))dA$
- Further, equation needed to describe the pressure as function of density, composition (nuclear reactions), temperature (heat transport) → Equation of State (EOS)
- Star evolution, lifetime and death depends on mass. Two groups:
 - Stars with masses less than 8 solar masses (white dwarfs)
 - Stars with masses greater than 8 solar masses (supernova explosions)

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Where does the energy come from?

Energy comes from nuclear reactions in the core.

 $4^1{\rm H} \rightarrow {}^4{\rm He} + {\rm neutrinos} + 26.7{\rm MeV}$





The Sun converts 600 million tons of hydrogen into 596 million tons of helium every second. The difference in mass is converted into energy. The Sun will continue burning hydrogen during 5 billions years. Energy relieased by H-burning: $6.45 \times 10^{18} \text{ erg g}^{-1}$ Solar Luminosity: $3.846 \times 10^{33} \text{ erg s}^{-1}$

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Transfer (strong interaction)

 $^{15}N(p, \alpha)^{12}C$, $\sigma \simeq 0.5 \text{ b at } E = 2.0 \text{ MeV}$

Capture (electromagnetic interaction)

$${}^{3}\mathrm{He}(\alpha,\gamma){}^{7}\mathrm{Be},\qquad\sigma\simeq10^{-6}~\mathrm{b~at}~E=2.0~\mathrm{MeV}$$

Weak (weak interaction)

$$p(p, e^+
u)d, \qquad \sigma \simeq 10^{-20} \text{ b at } E = 2.0 \text{ MeV}$$

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Stellar reaction rate

Consider N_a and N_b particles per cubic centimeter of particle types *a* and *b*. The rate of nuclear reactions is given by:

 $r = N_a N_b \sigma(v) v$

In stellar environment the velocity (energy) of particles follows a thermal distribution that depends on the type of particles.

• Nuclei (Maxwell-Boltzmann): $\phi(v) = N4\pi v^2 \left(\frac{m}{2\pi kT}\right)^{3/2} \exp\left(-\frac{mv^2}{2kT}\right)$

The product σv has to be averaged over the velocity distribution $\phi(v)$

$$\langle \sigma \mathbf{v} \rangle = \int_0^\infty \int_0^\infty \phi(\mathbf{v}_a) \phi(\mathbf{v}_b) \sigma(\mathbf{v}) \mathbf{v} d\mathbf{v}_a d\mathbf{v}_b$$

Changing to center-of-mass coordinates, integrating over the cm-velocity and using $\textit{E}=\mu\textit{v}^2/2$

$$\langle \sigma \mathbf{v} \rangle = \left(\frac{8}{\pi\mu}\right)^{1/2} \frac{1}{(kT)^{3/2}} \int_0^\infty \sigma(E) E \exp\left(-\frac{E}{kT}\right) dE$$

Charged-particle cross section

Stars' interior is a plasma made of charged particles (nuclei, electron). Nuclear reactions proceed by tunnel effect. For p + p reaction Coulomb barrier 550 keV, but the typical energy in the sun is only 1.35 keV.



cross section: $\sigma(E) = \frac{1}{E}S(E)e^{-2\pi\eta}$;

$$=)e^{-\pi \eta}; \quad \eta = -$$

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Astrophysical S factor



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Gamow window

Using definition of S factor:

$$\langle \sigma v \rangle = \left(\frac{8}{\pi\mu}\right)^{1/2} \frac{1}{(kT)^{3/2}} \int_0^\infty S(E) \exp\left[-\frac{E}{kT} - \frac{b}{E^{1/2}}\right] dE$$



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Gamow window

Assuming that S factor is constant over the Gamow window and approximating the integrand by a Gaussian one gets:

$$\langle \sigma \mathbf{v} \rangle = \left(\frac{2}{\mu}\right)^{1/2} \frac{\Delta}{(kT)^{3/2}} \mathcal{S}(E_0) \exp\left(-\frac{3E_0}{kT}\right)$$

$$E_0 = 1.22 [\text{keV}] (Z_1^2 Z_2^2 \mu T_6^2)^{1/3}$$

$$\Delta = 0.749 [\text{keV}] (Z_1^2 Z_2^2 \mu T_6^5)^{1/6}$$

 $(T_x \text{ measures the temperature in } 10^x \text{ K.})$ Examples for solar conditions:

reaction	<i>E</i> ₀ [keV]	$\Delta/2$ [keV]	I Imax	T dependence of $\langle \sigma \mathbf{v} \rangle$	
p+p	5.9	3.2	1.1 × 10 ⁻⁶	$T^{3.9}$	
p+ ¹⁴ N	26.5	6.8	$1.8 imes 10^{-27}$	T ²⁰	
α + ¹² C	56.0	9.8	$3.0 imes 10^{-57}$	T ⁴²	
¹⁶ O+ ¹⁶ O	237.0	20.2	$6.2 imes 10^{-239}$	T^{182}	

It depends very sensitively on temperature!

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The ppl chain

Step 1: $p + p \rightarrow^{2}$ He (not possible) $p + p \rightarrow d + e^+ + \nu_e$ Step 2: $d + p \rightarrow {}^{3}He$ $d + d \rightarrow {}^{4}\text{He}$ (d abundance too low) Step 3: ${}^{3}He + \rho \rightarrow {}^{4}Li$ (${}^{4}Li$ is unbound) ${}^{3}He + d \rightarrow {}^{4}He + n$ (d abundance too low) ³He $+^3$ He \rightarrow^4 He + 2p

d + d is not going, because Y_d is extremely small and d + p leads to rapid destruction.

 ${}^{3}He + {}^{3}He$ works, because Y_{3He} increases as nothing destroys it.

The relevant S-factors

 $p(p, e^+ \nu_e)d:$ $S_{11}(0)$ calculation $S_{12}(0)$ $p(d, \gamma)^3$ He: $S_{12}(0)$

³He(³He,2p)⁴He:

$$S_{11}(0) = (4.00 \pm 0.05) \times 10^{-25} \text{ MeV}$$

calculated
 $S_{12}(0) = 2.5 \times 10^{-7} \text{ MeVb}$
measured at LUNA
 $S_{33}(0) = 5.4 \text{ MeVb}$

measured at LUNA



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Deuterons are burnt by the reaction $d(p, \gamma)^3$ He:

$$\frac{dD}{dt} = r_{11} - r_{12}$$
$$= \frac{H^2}{2} \langle \sigma v \rangle_{11} - HD \langle \sigma v \rangle_{12}$$

In equilibrium $\left(\frac{dD}{dt} = 0\right)$ one has

$$\left(\frac{D}{H}\right)_{e} = \frac{\langle \sigma v \rangle_{11}}{2 \langle \sigma v \rangle_{12}}$$
$$(D/H)_{e} = 5.6 \times 10^{-18} \text{ for } T_{6} = 5$$

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⁴He can act as catalyst initializing the ppII and ppIII chains. With which nucleus will ⁴He fuse?

protons:

the fusion of ⁴He and protons lead to ⁵Li which is unbound.

deuterons:

the fusion of deuterons with ⁴He can make stable ⁶Li; however, the deuteron abundance is too low for this reaction to be significant

• ³He:

³He and ⁴He can fuse to ⁷Be. This is indeed the break-out reaction from the ppl chain.

Once ⁷Be is produced, it can either decay by electron capture or fuse with a proton. Thus, the reaction sequence branches at ⁷Be into the ppll and pplll chains.

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The solar pp chains



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The other hydrogen burning: CNO cycle



requires presence of ¹²C as catalyst

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Hydrogen burning: pp-chains vs CNO cycle

Slowest reaction determines efficiency (energy production) of chain:

pp-chains:

p+p fusion, mediated by weak interaction

CNO cycle:

 14 N+p, largest Coulomb barrier, mediated by electromagnetic interaction (in contrast to strong interaction in 15 N+p)

Temperature dependence quite different: $\langle \sigma v \rangle \sim T^{(\tau-2)/3}$ with $\tau = \frac{3E_0}{kT}$; $E_0 = 1.22[keV](Z_1^2 Z_2^2 \mu T_6^2)^{1/3}$

At $T_6=$ 15 (solar core): $\langle \sigma v \rangle \sim T^{3.9}$ (pp); $\langle \sigma v \rangle \sim T^{20}$ (CNO)

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Energy generation: CNO cycle vs pp-chains



- stars slightly heavier than the Sun burn hydrogen via CNO cycle
- this goes significantly faster; such stars have much shorter lifetimes

mass [M_{\odot}]	timescale [y]		
0.4	2 × 10 ¹¹		
0.8	$1.4 imes 10^{10}$		
1.0	1 × 10 ¹⁰		
1.1	9 × 10 ⁹		
1.7	$2.7 imes10^9$		
3.0	$2.2 imes 10^8$		
5.0	6×10^{7}		
9.0	$2 imes 10^7$		
16.0	1 × 10 ⁷		
25.0	$7 imes 10^{6}$		
40.0	1 × 10 ⁶		

hydrogen burning timescales depend strongly on mass. Stars slightly heavier than the Sun burn hydrogen by CNO cycle.

Future Sun will burn hydrogen by CNO cycle

- by continuous hydrogen burning, the Sun reduces its hydrogen reservoir in the core
- at some point in the future energy production by the pp-chains will not suffice to balance the solar energy household
- to gain sufficient energy the solar core will gravitationally contract and thereby increase the temperature
- hydrogen core burning in the Sun then switches from pp-chains to CNO cycle

when a star changes from core pp-burning to CNO cycle, its evolutionary track leaves main sequence in HR-diagram

MINOSITY (ENERGY OUTPUT)

RD.

COOL

CNO bi-cvs

GLOBULAR CLUSTER ME

- COLOR ----

TEMPERATURE ----(K)

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Solar neutrino fluxes and detector thresholds

Solar hydrogen burning produces neutrinos (Bahcall)



Depending on material, the detectors are blind for neutrinos with energies smaller than a threshold.

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Neutrino astronomy

- In the 1950s, Ray Davis (2002 Nobel Prize Laureate) decided to measure the solar neutrinos. (Every second, 10 billion neutrinos pass through every square cm on Earth).
- In 1967, the detector (615 tons of C₂Cl₄) was installed at Homestake Gold Mine, South Dakota (1,500 m depth).
- In 1968, the first measurement was a factor 3 smaller than predictions. Similar results by other experiments.

Super-Kamiokande, Japan (50,000 tons pure water)



Sudbury Neutrino Observatory, Canada (1,000 tons heavy water)



Detecting solar neutrinos

- Homestake:
 - first observation of solar neutrinos
 - detection ν_e + ${}^{37}\text{Cl} \rightarrow e^-$ + ${}^{37}\text{Ar}$
 - blind for $E_{\nu} < 814 \text{ keV}$
- Kamiokande, Super-Kamiokande:
 - proof that neutrinos are from Sun
 - detection $\nu_e + e^- \rightarrow \nu_e + e^{-'}$ (Cerenkov)
 - blind for $E_{\nu} < 5000 \text{ keV}$
- GALLEX:
 - observation of pp neutrinos, in agreement with luminosity
 - detection ν_e + ⁷¹Ga $\rightarrow e^-$ + ⁷¹Ge
 - blind for $E_{\nu} < 233 \text{ keV}$
- Sudbury SNO:
 - proof of solar neutrino oscillations
 - detection ν_e + d \rightarrow p + p + e^- (charged current)
 - detection ν_x + d \rightarrow p + n + ν_x (neutral current)
 - neutral current reaction detects all neutrino flavors
 - blind for $E_{\nu} <$ 2224 keV

Observed solar neutrino deficit





The SNO proof of neutrino oscillations



Observed TOTAL neutrino flux agrees with solar model predictions!

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When the hydrogen fuel in the core gets exhausted, an isothermal core of about 8% of the stellar mass can develop in the center. Continuus hydrogen burning adds to the core mass which eventually rises over the Schönberg-Chandrasekhar mass limit. Then the core's temperature (and density) rise. Finally the central temperature is high enough ($T_c \approx 10^8$ K) to ignite helium core burning.

Hydrogen burning continues in a shell outside the helium core. This (hydrogen shell burning) occurs at higher temperatures than hydrogen core burning.

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Consider a supply of protons and ⁴He.

We first note again that ⁵Li is unbound. Although this nucleus is continuously formed by $p+^4$ He reactions, the scattering is elastic and the formed ⁵Li nuclei decay within 10^{-22} s.

As a consequence ⁴He 'survives' in the core until sufficiently large temperatures are achieved to overcome the larger Coulomb barrier between ⁴He nuclei. Unfortunately the ⁸Be ground state, formed by elastic ⁴He+⁴He scattering, is a resonance too and decays within 10^{-16} s back to two ⁴He nuclei.

In 1952 Salpeter pointed out that the ⁸Be lifetime might be sufficiently large that there is a chance that it captures another ⁴He nucleus. This *triple-alpha reaction*

$$3 {}^{4}\text{He} \rightarrow {}^{12}\text{C} + \gamma$$

can then form ¹²C and supply energy. However, the simultaneous collision of 3 ⁴He (α -particles) is too rare to give the burning rate necessary in stellar models. So Hoyle predicted a resonance in ¹²C to speed up the collision. And indeed, this *Hoyle state* was experimentally observed shortly after its prediction. ¹²C can then react with another ⁴He nucleus forming ¹⁶O via

$$^{12}C + \alpha \rightarrow {}^{16}O + \gamma$$

These two reactions make up helium burning.

Helium burning reactions



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Influence of alpha+¹²C on nucleosynthesis



Nucleosynthesis yields from stars may be divided into production by stars above or below $9M_{\odot}$.

• stars with $M \lesssim 9 M_{\odot}$

the stars are expected to shed their envelopes during helium burning and become white dwarfs. Most of the matter returned to the ISM is unprocessed.

• stars with $M > 9M_{\odot}$

these stars will ignite carbon burning under non-degenerate conditions. The subsequent evolution proceeds in most cases to core collapse. These stars make the bulk of newly processed matter that is returned to the ISM.

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Burning conditions:

for stars > 8 M_o (solar masses) (ZAMS)

T~ 600-700 Mio ρ ~ 10⁵-10⁶ g/cm³

Major reaction sequences:

$$\overset{12}{\longrightarrow} C + \overset{24}{\longrightarrow} Mg^* \rightarrow \overset{23}{\longrightarrow} Mg + n - 2.62 \text{ MeV}$$

$$\overset{20}{\longrightarrow} \overset{20}{\longrightarrow} Ne + \alpha + 4.62 \text{ MeV}$$

$$\overset{\text{dominates}}{\longrightarrow} \overset{\text{by far}}{\longrightarrow} y \text{ far}$$

of course p's, n's, and a's are recaptured ... ²³Mg can b-decay into ²³Na

Composition at the end of burning:

mainly ²⁰Ne, ²⁴Mg, with some ^{21,22}Ne, ²³Na, ^{24,25,26}Mg, ^{26,27}Al of course ¹⁶O is still present in quantities comparable with ²⁰Ne (not burning ... yet) ₂₁

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Neon burning is very similar to carbon burning.

Burning conditions:

for stars > 12 M_o (solar masses) (ZAMS) T~ 1.3-1.7 Bio K ρ ~ 10^6 g/cm^3

Why would neon burn before oxygen ???

Answer:

Temperatures are sufficiently high to initiate photodisintegration of ²⁰Ne

$$\left. \begin{array}{c} {}^{20}\text{Ne}+\gamma \rightarrow {}^{16}\text{O}+\alpha \\ {}^{16}\text{O}+\alpha \rightarrow {}^{20}\text{Ne}+\gamma \end{array} \right\} \quad \text{equilibrium is established}$$

this is followed by (using the liberated helium)

 20 Ne+ $\alpha \rightarrow ^{24}$ Mg + γ

so net effect: $2 {}^{20}Ne \rightarrow {}^{16}O + {}^{24}Mg + 4.59 MeV.$

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Burning conditions:

T~ 2 Bio
$$\rho \sim 10^7 \text{ g/cm}^3$$

Major reaction sequences:

$${}^{16}\text{O} + {}^{16}\text{O} \rightarrow {}^{32}\text{S}^* \rightarrow {}^{31}\text{S} + n + 1.45 \text{ MeV}$$
 (5%)

$$\rightarrow^{31}P + p + 7.68 \text{ MeV}$$
 (56%)

$$\rightarrow {}^{30}\text{P} + d - 2.41 \text{ MeV}$$
 (5%)

$$\rightarrow^{28}\text{Si} + \alpha + 9.59 \text{ MeV}.$$
 (34%)

plus recapture of n,p,d,a

Main products:

28Si, 32S (90%) and some 33, 34S, 35, 37Cl, 36. 38Ar, 39, 41K, 40, 42Ca

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Silicon Burning

Silicon burning is very similar to oxygen burning.

Burning conditions:

T~ 3-4 Bio ρ ~ 10⁹ g/cm³

Reaction sequences:

- · Silicon burning is fundamentally different to all other burning stages.
- Complex network of fast (γ ,n), (γ ,p), (γ ,a), (n, γ), (p, γ), and (a, γ) reactions
- The net effect of Si burning is: 2 ²⁸Si --> ⁵⁶Ni,

need new concept to describe burning:

Nuclear Statistical Equilibrium (NSE)

Quasi Statistical Equilibrium (QSE)

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Nuclear burning stages (e.g., 20 solar mass star)

Fuel	Main Product	Secondary Product	T (10 ⁹ K)	Time (yr)	Main Reaction
н	He	¹⁴ N	0.02	10 ⁷	4 H → ^{CNO} 4He
He	0, C	¹⁸ O, ²² Ne s-process	0.2	10 ⁶	3 He ⁴ → ¹² C ¹² C(α,γ) ¹⁶ O
C 🖌	Ne, Mg	Na	0.8	10 ³	¹² C + ¹² C
Ne	O, Mg	AI, P	1.5	3	²⁰ Ne(γ,α) ¹⁶ O ²⁰ Ne(α,γ) ²⁴ Mg
O	Si, S	CI, Ar, K, Ca	2.0	0.8	¹⁶ O + ¹⁶ O
Si	Fe	Ti, V, Cr, Mn, Co, Ni	3.5	0.02	²⁸ Si(γ,α)

A (10) > A (10) > A (10)

Kippenhahn diagram for a 22 M_{\odot} star

(A. Heger and S. Woosley)



Karlheinz Langanke (GSI & TU Darmstadt)

Nuclear Astrophysics

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